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## LETTER

## Transatlantic flight times and climate change

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## Abstract

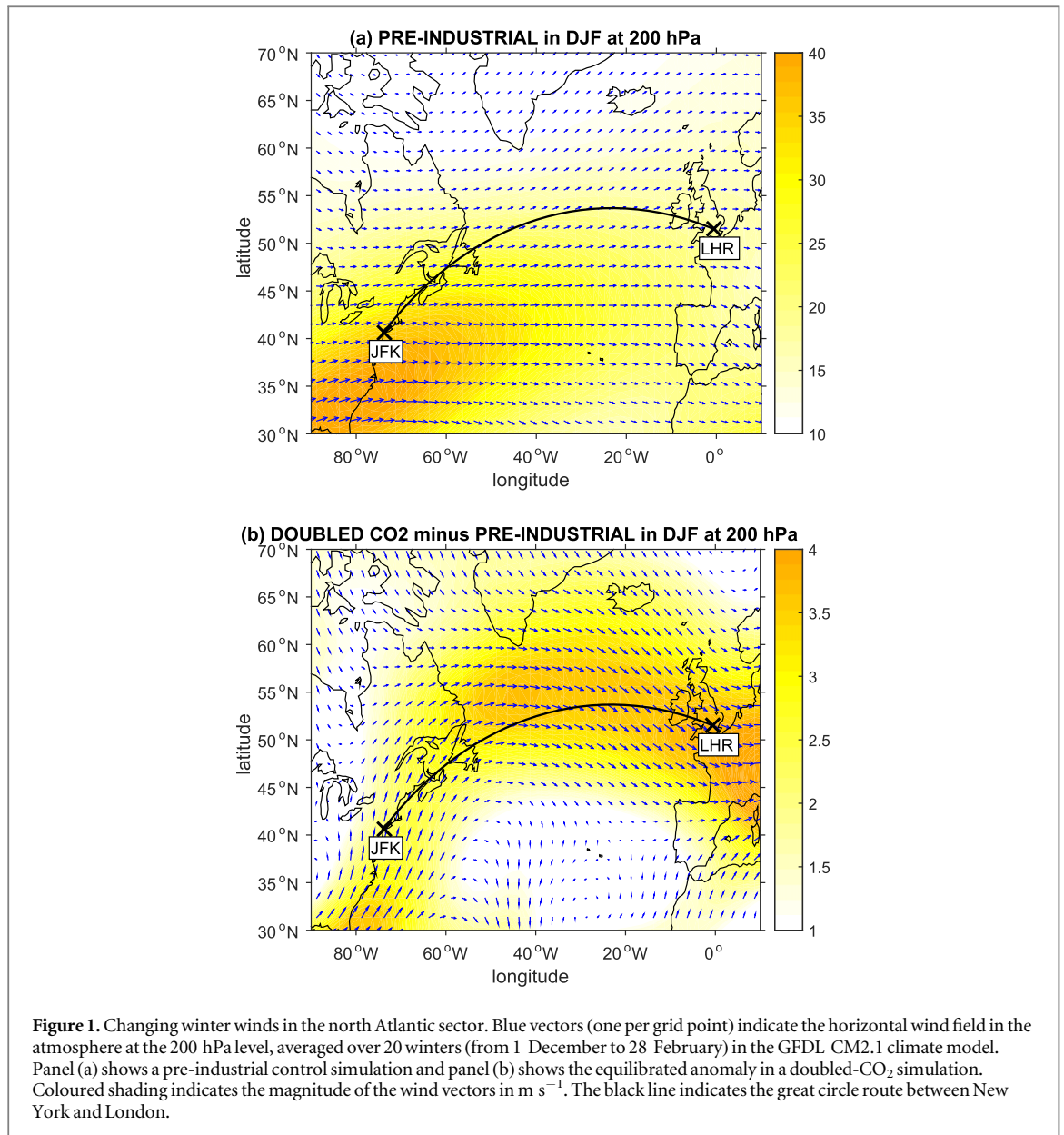
Aircraft do not fly through a vacuum, but through an atmosphere whose meteorological characteristics are changing because of global warming. The impacts of aviation on climate change have long been recognised, but the impacts of climate change on aviation have only recently begun to emerge. These impacts include intensified turbulence and increased take-off weight restrictions. Here we investigate the influence of climate change on flight routes and journey times. We feed synthetic atmospheric wind fields generated from climate model simulations into a routing algorithm of the type used operationally by flight planners. We focus on transatlantic flights between London and New York, and how they change when the atmospheric concentration of carbon dioxide is doubled. We find that a strengthening of the prevailing jet-stream winds causes eastbound flights to significantly shorten and westbound flights to significantly lengthen in all seasons. Eastbound and westbound crossings in winter become approximately twice as likely to take under 5 h 20 min and over 7 h 00 min, respectively. For reasons that are explained using a conceptual model, the eastbound shortening and westbound lengthening do not cancel out, causing round-trip journey times to increase. Even assuming no future growth in aviation, the extrapolation of our results to all transatlantic traffic suggests that aircraft will collectively be airborne for an extra 2000 h each year, burning an extra 7.2 million gallons of jet fuel at a cost of US\$ 22 million, and emitting an extra 70 million kg of carbon dioxide, which is equivalent to the annual emissions of 7100 average British homes. Our results provide further evidence of the two-way interaction between aviation and climate change.

## 1. Introduction

It has long been recognised that aviation affects the climate, through the radiative forcing associated with greenhouse-gas emissions and contrails (Stuber *et al* 2006, Lee *et al* 2009). However, it is becoming increasingly clear that the interaction is two-way and that climate change has important consequences for aviation. For example, stronger mid-latitude wind shears in the upper troposphere and lower stratosphere appear to be destabilising the atmosphere and causing clear-air turbulence to intensify (Williams and Joshi 2013). At ground level, warmer air reduces the lift force on the wings of departing aircraft and appears to be increasing the likelihood of take-off weight restrictions (Coffel and Horton 2015). Here we investigate the influence of climate change on flight

routes and journey times. This subject has received relatively little attention, but is potentially important because of the acute sensitivity of the commercial aviation sector to fuel costs (Karnauskas *et al* 2015).

The route between two airports that minimises the distance travelled is the great circle, which is the spherical equivalent of a straight line. However, it is more economical to minimise the journey time than the distance travelled. For this reason, aircraft routinely deviate from the great circle route in a carefully optimised manner, to benefit from tailwinds or avoid headwinds (Lunnon and Marklow 1992). The day-to-day variability of flight routes and journey times is therefore dictated by the horizontal wind field in the atmosphere (Palopo *et al* 2010). The inter-annual variability of flight routes and journey times between Hawaii and the continental USA has been found to be caused



predominantly by anomalous wind patterns associated with the El Niño Southern Oscillation and Arctic Oscillation (Karnauskas *et al* 2015). Although the North Atlantic flight corridor between Europe and North America is one of the world's busiest, with approximately 600 crossings each day (Irvine *et al* 2013), little is known about the long-term response of transatlantic flight routes and journey times to the wind changes associated with global warming.

The average wintertime jet-stream winds in the upper troposphere and lower stratosphere of the north Atlantic sector are generally projected to become stronger in response to greenhouse-gas forcing, as shown in figure 1. This strengthening is consistent across the current generation of climate models, although the magnitudes and structures of the strengthening vary in detail from one model to

another (Woollings and Blackburn 2012, Haarsma *et al* 2013). The strengthening is composed partly of changes to the zonal wind field, which are the thermal wind response to upper tropospheric warming separated by a latitudinally sloping tropopause from lower stratospheric cooling (Lorenz and DeWeaver 2007). The strengthening is also composed partly of changes to the meridional wind field, which are a consequence of changes to the stationary planetary wave structure (Haarsma and Selten 2012, Simpson *et al* 2016). By projecting the wind vectors in figure 1 onto the great circle route from New York to London, we calculate that the average along-track (tailwind) component of the wind field at typical flight cruising altitudes increases by 14.8% from 21.4 to 24.6 m s<sup>-1</sup> when the carbon dioxide (CO<sub>2</sub>) concentration is doubled. The early stages of this strengthening perhaps contributed to a well-publicised transatlantic crossing from New York

to London on 8 January 2015, which took a record time of only 5 h 16 min because of a strong tailwind from an unusually fast jet stream (Crilly 2015).

The aim of the present study is to perform a detailed investigation of the influence of climate change on flight routes and journey times. The focus is on transatlantic flights between London and New York, and how they change when the atmospheric concentration of CO<sub>2</sub> is doubled. Section 2 illustrates the important concepts in a simple model, which is approximate but has the benefit of yielding analytic predictions. Section 3 pursues a more comprehensive treatment, by feeding synthetic atmospheric wind fields generated from climate model simulations into a routing algorithm of the type used operationally by flight planners. Section 4 concludes the paper with a statistical analysis and discussion.

## 2. Conceptual model

The following conceptual model illustrates the influence of wind changes on flight times. Suppose that a constant horizontal wind of speed  $w$  blows along the great circle from a western airport to an eastern airport a distance  $d$  away. Truncated Taylor series expansions show that an aircraft travelling with air speed  $U \gg w$  will incur an eastbound journey time of:

$$t_{\text{east}} = \frac{d}{U + w} \approx \frac{d}{U} \left( 1 - \frac{w}{U} + \frac{w^2}{U^2} \right) \quad (1)$$

and a westbound journey time of:

$$t_{\text{west}} = \frac{d}{U - w} \approx \frac{d}{U} \left( 1 + \frac{w}{U} + \frac{w^2}{U^2} \right). \quad (2)$$

Note that the amount by which the westbound journey is lengthened by the headwind exceeds the amount by which the eastbound journey is shortened by the tailwind. Therefore, the round-trip journey time of:

$$t_{\text{round}} = t_{\text{east}} + t_{\text{west}} \approx \frac{2d}{U} \left( 1 + \frac{w^2}{U^2} \right) \quad (3)$$

in the wind field is longer than the round-trip journey time of  $2d/U$  in still air. This result accounts for the robust round-trip residual that has been documented in flight-time data but has previously been unexplained (Karnauskas *et al* 2015).

Now suppose that global warming causes the wind speed to increase by a small amount  $dw$ . Differentiation of (3) shows that the corresponding increase  $dt_{\text{round}}$  in the round-trip journey time is given by:

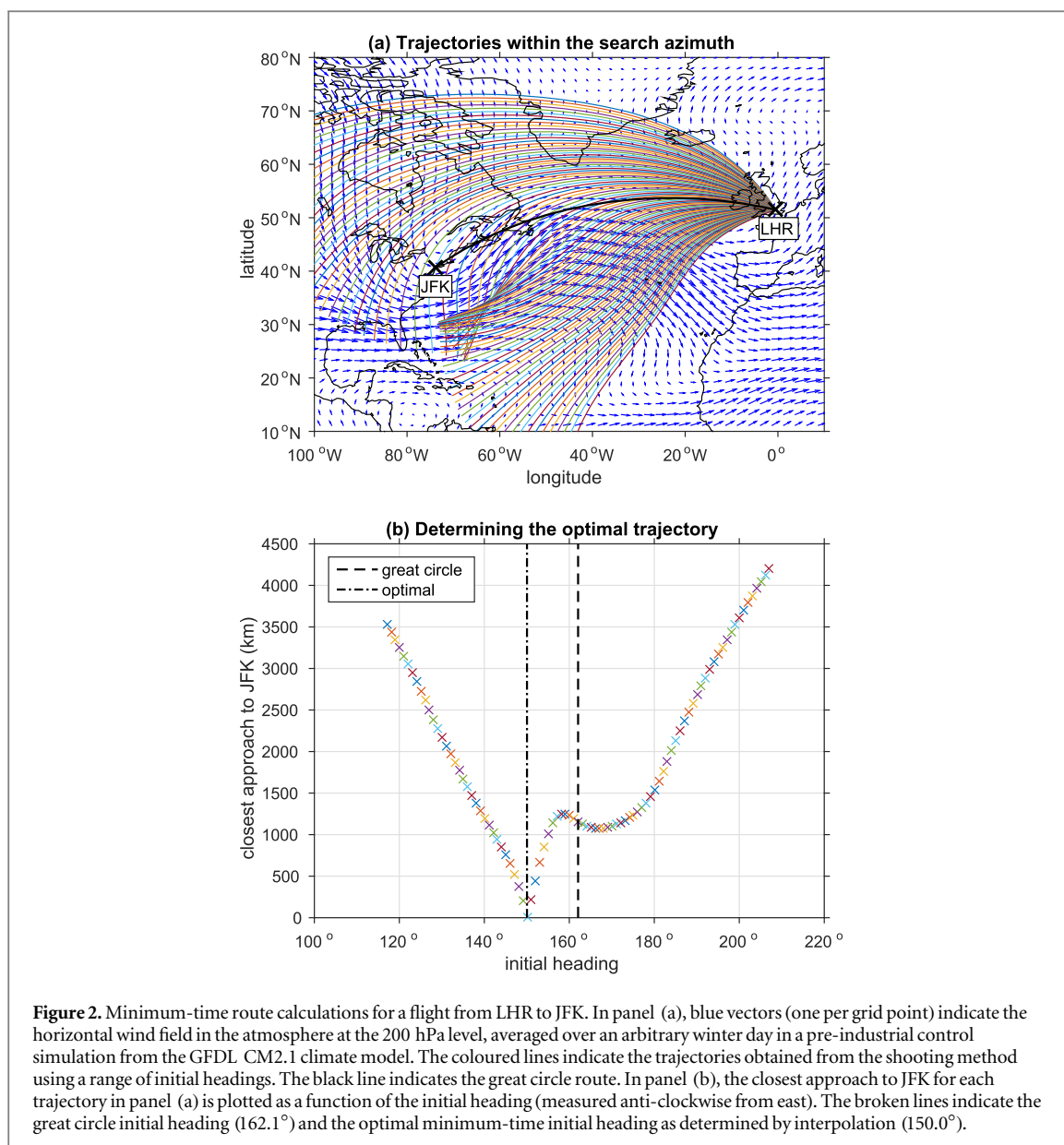
$$\frac{dt_{\text{round}}}{t_{\text{round}}} \approx 2 \left( \frac{w}{U} \right)^2 \frac{dw}{w}. \quad (4)$$

For flights between New York and London, we substitute  $w = 21.4 \text{ m s}^{-1}$  and  $dw = 3.2 \text{ m s}^{-1}$  (see section 1) together with  $U = 250 \text{ m s}^{-1}$  and  $t_{\text{round}} = 12 \text{ h}$  to yield a predicted round-trip journey-time increase of 1 min 35 s. We will return to this analytic result in section 4, to compare it with the predictions of an alternative approach that is more rigorous but computationally expensive.

## 3. Minimum-time routes

The conceptual model presented in section 2 is a simplification, because in reality the atmospheric winds vary in space and time. Determining the fastest route between two points in a given wind field is a mathematical problem in the calculus of variations. The Euler–Lagrange equation reduces to a two-point boundary value problem in time, which was derived in the 1930s for motion in two and three Cartesian dimensions (Zermelo 1930, 1931, Levi-Civita 1931) and in the 1940s for motion on the surface of a sphere (Arrow 1949). Various algorithms have been developed to solve the problem (Bijlsma 2009, Jardin and Bryson 2012). The resulting minimum-time (or wind-optimal) route deviates from the great circle and therefore covers a greater distance, but the increased ground speed resulting from faster tailwinds or slower headwinds more than compensates. The minimum-time route is optimal in the sense that it would be flown in a completely unrestrained system without adverse weather, turbulence (Kim *et al* 2015), climate impact considerations (Sridhar *et al* 2011, Irvine *et al* 2013), or air traffic control constraints. Despite these restrictions, the evidence is that actual filed flight routes do lie reasonably close to the minimum-time routes (Palopo *et al* 2010), which also minimise the fuel cost.

Here we calculate minimum-time routes in spherical geometry by numerically integrating the three ordinary differential equations for the time evolution of an aircraft's latitude, longitude, and heading (Jardin and Bryson 2012, Ng *et al* 2014, Kim *et al* 2015). The latitude and longitude equations are simply the two horizontal components of the vector equation for the relative motion, which states that the velocity of the aircraft relative to the ground is equal to the velocity of the aircraft relative to the air plus the velocity of the air relative to the ground. The heading equation is more complicated, but in essence it states that the aircraft turns at a prescribed, flow-dependent rate toward the side with the stronger headwinds or weaker tailwinds (Arrow 1949). We focus on transatlantic flights between Heathrow Airport in London (LHR; 0.4614°W, 51.4775°N) and John F Kennedy International Airport in New York (JFK; 73.7789°W, 40.6397°N). Because this is a long-haul route, we neglect the ascent and

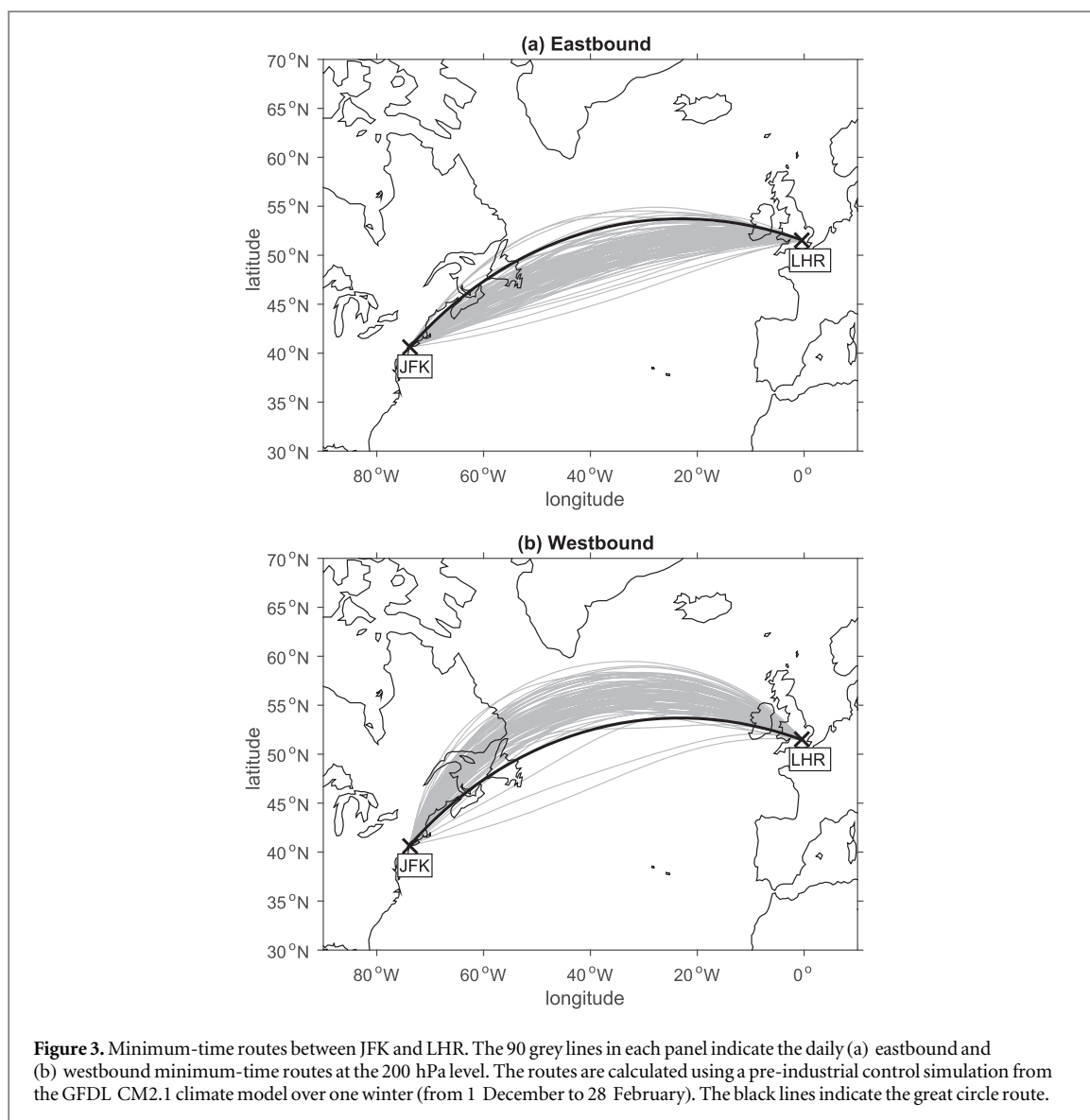


descent phases and consider only the cruise phase. We assume that cruising flights maintain a constant air speed of  $250 \text{ m s}^{-1}$  and a constant pressure altitude of 200 hPa for the duration of the crossing, which are both reasonable assumptions (Irvine *et al* 2013).

Because the optimal initial heading is unknown *a priori*, we convert the two-point boundary value problem in time into an initial value problem by using the shooting method (Kim *et al* 2015). We shoot with initial headings ranging from  $45^\circ$  clockwise of the great circle initial heading to  $45^\circ$  anticlockwise of it, in increments of  $1^\circ$ . For each initial heading in this search azimuth, we integrate the equations of motion forward in time from the departure airport, using the Euler method with a time-step size of 60 s. To allow for strong headwinds, the integration period is chosen to be 40% longer than the great circle journey time in still air. From the resulting family of trajectories, we use interpolation to calculate the initial heading of the

route that would exactly encounter the arrival airport, together with its corresponding flight time. An example of the shooting method is shown in figure 2. On rare occasions in very nonlinear wind fields, more than one trajectory in the search azimuth may encounter the arrival airport, in which case we select the fastest. Sensitivity experiments with double the time-step size and heading increment confirm that the above algorithm produces results that are converged.

The integrations are driven by simulated horizontal wind data from the Geophysical Fluid Dynamics Laboratory (GFDL) CM2.1 climate model (Delworth *et al* 2006, Gnanadesikan *et al* 2006, Stouffer *et al* 2006, Wittenberg *et al* 2006). The upper-level atmospheric winds in this model are consistent with reanalysis data (Delworth *et al* 2006, Reichler and Kim 2008) and their response to global warming is consistent with other climate models (Stouffer *et al* 2006). GFDL CM2.1 is one of the third Coupled



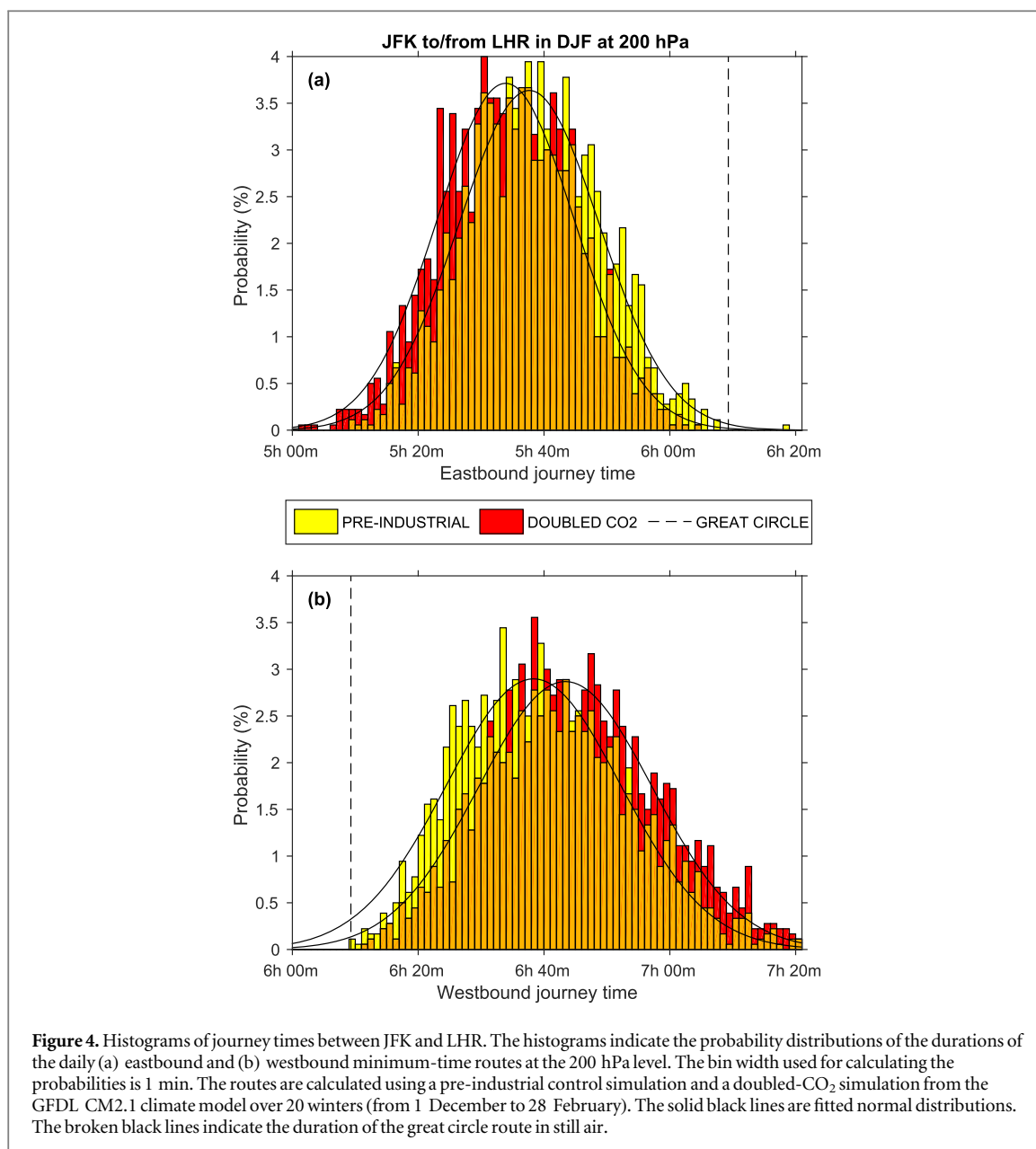
Model Intercomparison Project (CMIP3) models (Meehl *et al* 2007b), which have essentially the same ensemble-mean zonal wind response to greenhouse-gas forcing (Haarsma *et al* 2013, Manzini *et al* 2014) as the CMIP5 models (Taylor *et al* 2012). We compute the eastbound and westbound minimum-time flight routes from the modelled wind fields every day for a period of 20 years. Daily mean wind fields are used for this purpose, because of the relatively slow evolution of the large-scale atmospheric circulation. The calculations are performed using winds from the equilibrium phase of a climate change simulation in which the atmospheric CO<sub>2</sub> concentration is held constant at twice its pre-industrial value. This CO<sub>2</sub> level is projected to be reached later this century, according to the A1B emissions scenario (Meehl *et al* 2007a). For comparison, the calculations are repeated using 20 years of daily winds from a pre-industrial control simulation.

At each time step of the trajectory calculations, we interpolate from the gridded model wind data to find the local wind components at the position of the

aircraft using a two-dimensional cubic spline in latitude and longitude with not-a-knot end conditions. We calculate the latitudinal and longitudinal wind gradients, which feature in the heading equation, using second-order centred differences. Although the GFDL CM2.1 model is coarser in resolution than the models that are used operationally in flight planning, minimum-time routes have been found to display no significant dependence on the horizontal resolution of the ingested wind data, with flight times changing by less than 1 s for a typical transatlantic flight when the resolution is doubled (Lunnon and Mirza 2007). A winter climatology of the minimum-time routes calculated by the algorithm for the pre-industrial control simulation is shown in figure 3.

#### 4. Statistical analysis and discussion

The journey-time statistics for the minimum-time routes in winter are summarised as histograms in figure 4. In the pre-industrial control simulation,



westbound flights generally take longer than eastbound flights, as expected from the prevailing winds in figure 1(a). Although the great circle journey time in still air is 6 h 09 min, the mean eastbound journey time is around half an hour shorter at 5 h 38 min, and the mean westbound journey time is around half an hour longer at 6 h 40 min. It is also apparent from visual inspection of figure 4 that westbound journey times exhibit significantly more day-to-day variability than eastbound journey times, with pre-industrial standard deviations of 13 min 47 s and 10 min 30 s, respectively.

The effect of doubling CO<sub>2</sub> is to shift the eastbound distribution to shorter journey times and the westbound distribution to longer journey times. The mean eastbound journey time shortens by 4 min 00 s, with a 95% confidence interval ranging from 3 min 19 s to 4 min 41 s. An unpaired two-sample two-tailed t-test, assuming that the eastbound

histograms are both sampled from normal distributions and allowing for different variances, clearly rejects the null hypothesis that the underlying distributions have equal means ( $p \sim 10^{-30}$ ). Similarly, the mean westbound journey time lengthens by 5 min 18 s ( $p \sim 10^{-28}$ ), with a 95% confidence interval ranging from 4 min 21 s to 6 min 15 s. Note that the eastbound shortening and westbound lengthening are unequal and do not cancel out. Consequently, the mean round-trip journey time lengthens by 1 min 18 s ( $p \sim 10^{-7}$ ), with a 95% confidence interval ranging from 0 min 48 s to 1 min 48 s. This interval includes the 1 min 35 s increase predicted by the conceptual model in section 2.

By examining the tails of the distributions, we calculate that the probability of an eastbound crossing taking under 5 h 20 min more than doubles from 3.5% in the pre-industrial control simulation to 8.1% in the doubled-CO<sub>2</sub> simulation. We conclude that

**Table 1.** Average journey times between JFK and LHR. The mean durations of the eastbound and westbound minimum-time routes are tabulated for the specified season and pressure level. The routes are calculated using a pre-industrial control simulation (CTL) and a doubled-CO<sub>2</sub> simulation (2×CO<sub>2</sub>) from the GFDL CM2.1 climate model over 20 years. The seasons are winter (DJF; 1 December to 28 February), spring (MAM; 1 March to 31 May), summer (JJA; 1 June to 31 August), and autumn (SON; 1 September to 30 November). Raw times are shown in hours:minutes:seconds and time differences are shown in minutes:seconds.

| Season and pressure level | Eastbound |                   |                        | Westbound |                   |                        | Round-trip<br>2×CO <sub>2</sub> –CTL |
|---------------------------|-----------|-------------------|------------------------|-----------|-------------------|------------------------|--------------------------------------|
|                           | CTL       | 2×CO <sub>2</sub> | 2×CO <sub>2</sub> –CTL | CTL       | 2×CO <sub>2</sub> | 2×CO <sub>2</sub> –CTL |                                      |
| DJF at 200 hPa            | 5:38:22   | 5:34:22           | −4:00                  | 6:40:26   | 6:45:44           | +5:18                  | +1:18                                |
| MAM at 200 hPa            | 5:48:07   | 5:44:59           | −3:08                  | 6:28:28   | 6:32:18           | +3:50                  | +0:42                                |
| JJA at 200 hPa            | 5:41:55   | 5:40:24           | −1:31                  | 6:33:38   | 6:35:42           | +2:04                  | +0:33                                |
| SON at 200 hPa            | 5:35:53   | 5:30:52           | −5:01                  | 6:43:11   | 6:50:03           | +6:52                  | +1:51                                |
| DJF at 150 hPa            | 5:42:57   | 5:38:22           | −4:35                  | 6:37:12   | 6:43:05           | +5:53                  | +1:18                                |
| DJF at 250 hPa            | 5:35:38   | 5:32:19           | −3:19                  | 6:41:43   | 6:46:35           | +4:52                  | +1:33                                |

record-breaking eastbound transatlantic crossing times, like the one achieved on 8 January 2015 and discussed in section 1, will occur with increasing frequency in the coming decades. We also calculate that the probability of a westbound crossing taking over 7 h 00 min nearly doubles from 8.6% to 15.3%, suggesting that delayed arrivals in North America will become increasingly common.

Similar results are obtained when the above analysis is repeated by calculating minimum-time routes for the other seasons and pressure levels, as shown in table 1. All four seasons and all three pressure levels display a mean round-trip journey-time increase, which is largest in autumn and smallest in spring and summer. Averaged over the seasons, the increase at 200 hPa is 1 min 06 s. Even assuming no future growth in aviation, the extrapolation of this figure to all transatlantic traffic suggests that aircraft will collectively be airborne for an extra 2 000 h each year, burning an extra 7.2 million US gallons (gal) of jet fuel at a cost of US\$ 22 million, and emitting an extra 70 million kg of CO<sub>2</sub> into the atmosphere. These calculations assume 300 round trips each day (Irvine *et al* 2013), a fuel burn rate of 1 gal s<sup>−1</sup>, a long-term average jet-fuel cost of US\$ 3 gal<sup>−1</sup>, and CO<sub>2</sub> emissions of 9.6 kg gal<sup>−1</sup>. These extrapolated increases are relatively small when compared to the corresponding baseline figures for transatlantic traffic, but are large in absolute terms. For example, the extra CO<sub>2</sub> is equivalent to the annual emissions of 7100 average British homes (Hargreaves *et al* 2013).

Our results provide further evidence of the two-way interaction between aviation and climate change. Future work is needed to apply our methodology to other flight routes globally, such as transpacific, transpolar, and cross-equatorial routes. Future work should also quantify the model-dependent uncertainties by using atmospheric wind fields from other climate models. A major limiting factor is likely to be computational resources, because calculating the minimum-time routes is computationally demanding. Indeed, previous studies have stated that calculating the minimum-time route for each daily weather pattern is not feasible (Irvine *et al* 2013). Although this feat has in fact been achieved in the present study, the

calculations took several months of computational effort to complete. Finally, the route that minimises the journey time is generally not the route that minimises the turbulence potential or even the climate impact, because the latter depends on the radiative effects of contrails as well as emitted greenhouse gases. Future work should take these additional considerations into account.

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