

# Thermobaric control of gravitational potential energy generation by diapycnal mixing in the deep ocean

K. I. C. Oliver<sup>1</sup> and R. Tailleux<sup>2</sup>

Sources and sinks of gravitational potential energy (GPE) play a rate-limiting role in the large scale ocean circulation. A key source is turbulent diapycnal mixing, whereby irreversible mixing across isoneutral surfaces is enhanced by turbulent straining of these surfaces. This has motivated international observational efforts to map diapycnal mixing in the global ocean. However, in order to accurately relate the GPE supplied to the large scale circulation by diapycnal mixing to the mixing energy source, it is first necessary to determine the ratio,  $\xi$ , of the GPE generation rate to the available potential energy dissipation rate associated with turbulent mixing. Here, the link between GPE and hydrostatic pressure is used to derive the GPE budget for a compressible ocean with a nonlinear equation of state. The role of diapycnal mixing is isolated and from this a global climatological distribution of  $\xi$  is calculated. It is shown that, for a given source of mixing energy, typically three times as much GPE is generated if the mixing takes place in bottom waters rather than in the pycnocline. This is due to GPE destruction by cabbeling in the pycnocline, as opposed to thermobaric enhancement of GPE generation by diapycnal mixing in the deep ocean.

## 1. Introduction

The ocean's global meridional overturning circulation (MOC) influences climate through the large scale transport of heat, carbon and nutrients. Intrinsic to this circulation is the formation and downwelling of dense water at high latitudes which, if balanced by the upwelling of more buoyant water elsewhere, constitutes a sink of gravitational potential energy (GPE). Two principal mechanisms supply the GPE required for a steady state MOC to exist: (a) downwelling of buoyancy by turbulent diapycnal mixing [e.g. Munk and Wunsch, 1998]; (b) wind-driven upwelling of dense water and downwelling of more buoyant water, chiefly in the Antarctic Circumpolar Current [e.g. Toggweiler and Samuels, 1998]. The former mechanism is required to sustain Antarctic overturning, since the downwelling Antarctic Bottom Water source is denser than the water that upwells in the Antarctic Circumpolar Current. This, together with the finding that mixing in the ocean has a highly heterogeneous distribution, has motivated much work to understand and to map turbulent diapycnal mixing in the global ocean [e.g. Kunze *et al.*, 2006; St. Laurent and Simmons, 2006].

<sup>1</sup>National Oceanography Centre, Southampton, University of Southampton, UK.

<sup>2</sup>Department of Meteorology, University of Reading, Reading, UK.

Turbulent diapycnal mixing describes the combined effect of finescale advection and irreversible mixing across isoneutral surfaces, which dissipates mechanical energy at the rate  $\varepsilon_K + \varepsilon_P$ . Here,  $\varepsilon_K$  is the viscous dissipation rate and  $\varepsilon_P = \kappa_v N^2$ , where  $N$  is the buoyancy frequency, is the available potential energy (APE) dissipation rate that defines the effective turbulent diapycnal diffusivity  $\kappa_v$ . APE dissipation corresponds to the irreversible conversion of mechanical energy to internal energy through molecular diffusion, and has a signature in the irreversible entropy production rate [Tailleux, 2012a]. The concept of mixing efficiency,  $\Gamma$ , is commonly used to measure the relative importance of viscous versus non-viscous dissipation, defined either as  $\varepsilon_P/\varepsilon_K$  [e.g. Oakey, 1982], as adopted here, or as  $\Gamma = \varepsilon_P/(\varepsilon_P + \varepsilon_K)$  [e.g., Peltier and Caulfield, 2003]. As discussed by Tailleux [2009b, 2012b], the two possible definitions for  $\Gamma$  are each generalisable to a non-linear equation of state because, although  $\varepsilon_P$  depends on the thermal expansion coefficient  $\alpha$ , it does not depend on the derivatives of  $\alpha$  with respect to temperature and pressure and is hence unaffected by cabbeling or thermobaricity. Physically, the turbulent fluxes for the materially conserved quantities (salinity and conservative temperature) are unaffected by a nonlinear equation of state, unlike the turbulent flux of buoyancy. Following Osborn [1980], oceanographers often assume that  $\Gamma$  has an upper bound of 0.2 in the case of mechanically-driven mixing (buoyancy-driven mixing can be much more efficient [Scotti and White, 2011]). Turbulent diapycnal mixing results in the reversible generation of GPE at the expense of internal energy at the rate  $\xi\varepsilon_P = \xi\Gamma\varepsilon_K$ , where  $\xi$  is the ratio of the rate of GPE generation by diapycnal mixing to the mixing energy transfer rate  $\varepsilon_P$ .

Under a linear equation of state (EOS), buoyancy is a conservative quantity, so  $\xi = 1$ . However, buoyancy may be created or destroyed under a nonlinear EOS, enhancing or reducing GPE generation for a given amount of mixing, and allowing for values of  $\xi$  greater and lower than unity. The seminal study of Munk and Wunsch [1998] provided an estimate for the mechanical energy source required to sustain the MOC under the assumption of a linear EOS. More recent studies have indicated that accounting for a nonlinear EOS would lead to a significant correction to this estimate, but have focused either on the role of isoneutral mixing [Klocker and McDougall, 2010] or have not isolated the role of diapycnal mixing [e.g. Gnanadesikan *et al.*, 2005]. Fofonoff [1998, 2001] did focus on diapycnal mixing, although not within the context of the energetics of the large scale circulation, and showed that it is possible for diapycnal mixing to cause a net loss of GPE (i.e.  $\xi < 0$ ) due to loss of buoyancy through cabbeling. Here, we advance upon this work by exploiting the link between GPE and the compressible work to express the GPE budget exactly for a compressible ocean, in a form that allows us to isolate the role of diapycnal mixing and derive an expression for  $\xi$  (Section 2). We then use climatological data to show that, over most of the ocean,  $\xi$  differs significantly from the linear-EOS value of 1 (Section 3). We show that GPE generation by diapycnal mixing is suppressed by cabbeling throughout the pycnocline, but that thermobaric buoyancy generation associated with the flux of heat to high pressures dominates over cabbeling in the abyssal ocean, leading to values of  $\xi$  greater than 1 at depths greater than about 1500 m. Finally, we explore the implications of the observed distribution of  $\xi$  for the energetics of the global MOC (Section 4).

## 2. Gravitational potential energy in a nonlinear compressible ocean

The gravitational potential energy budget in the compressible ocean is given by

$$\frac{d\text{GPE}}{dt} = \frac{d}{dt} \int_V \rho g z dV = \int_V \rho g w dV, \quad (1)$$

where  $\rho$  is *in situ* density,  $g$  is acceleration due to gravity, and  $w$  is vertical velocity. Gnanadesikan *et al.* [2005] were perhaps the first to seek to generalize this idea to the fully nonlinear case, by proposing to regard the density flux  $\rho g w$  as being made up of different physical processes, which are represented by different physical parameterizations in general circulation models. We instead distinguish between adiabatic and diabatic processes by linking the GPE budget with the thermodynamic  $Pv$  work (compressible work), where  $P$  is the hydrostatic pressure and  $v = 1/\rho$  is the specific volume. This link is made by manipulating the expression for GPE using integration by parts, yielding the classical result

$$\text{GPE} = \int_V P' v dm - M_o g \bar{H}, \quad (2)$$

where  $dm = \rho dV$  is the elementary mass of a fluid parcel, and  $\bar{H}$  is a mean ocean depth defined by the relation

$$M_o g \bar{H} = \int_S (P_b - P_a) H dx dy,$$

where  $M_o = \int_S (P_b - P_a) g^{-1} dx dy$  is the mass of the ocean. Here,  $P_b$  is bottom pressure,  $P_a$  is surface atmospheric pressure, and  $P' = P - P_a$ .

The GPE budget is therefore

$$\frac{d\text{GPE}}{dt} = \int_V P' \frac{Dv}{Dt} dm + \int_V v \frac{DP'}{Dt} dm - g \frac{d(M_o \bar{H})}{dt}. \quad (3)$$

The first term in the r.h.s of (3) states that expansion increases GPE. The conceptual link with (1) is that expansion is associated with an isobaric upwelling of overlying water. The greater the hydrostatic pressure at which such expansion occurs, the greater the mass of overlying water that upwells and gains GPE. The second term represents the conversion between kinetic energy and APE. A negative correlation between  $v$  and  $\frac{DP'}{Dt}$  would imply the upwelling of buoyant water and downwelling of dense water, which would act to decrease GPE. The final term arises because tendencies in the depth-integrated hydrostatic pressure and GPE of a water column are identical only at constant mass; any change of mass of the global ocean, or a net horizontal redistribution of mass across isobaths, leads to a correction. This term vanishes at steady state.

Here, we are interested in the effect of mixing. We have

$$\frac{Dv}{Dt} = \frac{1}{\rho} \left[ \alpha \frac{D\Theta}{Dt} - \beta \frac{DS}{Dt} \right] - \frac{1}{\rho^2 c_s^2} \frac{DP}{Dt}, \quad (4)$$

where  $\alpha$  and  $\beta$  are the thermal expansion and haline contraction coefficients defined relative to the variables  $(\Theta, S, P)$ ,  $\Theta$  is McDougall [2003]'s conservative temperature and  $S$  is salinity, and  $c_s$  is the speed of sound. The integral effect of mixing is usually regarded as an isobaric process [e.g. IOC *et al.*, 2010], i.e.  $\frac{DP}{Dt} \Big|_{\text{mixing}} = 0$ , so we can write

$$\frac{d\text{GPE}}{dt} \Big|_{\text{mixing}} = \int_V P' \left[ \alpha \frac{D\Theta}{Dt} - \beta \frac{DS}{Dt} \right] dV \Big|_{\text{mixing}}, \quad (5)$$

We use the turbulent parameterization

$$\frac{D\Theta}{Dt} \Big|_{\text{mixing}} = \nabla \cdot (\mathbf{K} \nabla \Theta), \quad \frac{DS}{Dt} \Big|_{\text{mixing}} = \nabla \cdot (\mathbf{K} \nabla S),$$

where  $\mathbf{K}$  is a turbulent diffusive tensor encapsulating the net effect of fine-scale advection and molecular diffusion. Using the condition of no diffusion through boundaries, so  $\int_V \nabla \cdot (\mathbf{K} \mathbf{C}) dV = 0$  for arbitrary  $\mathbf{C}$ , (5) can be rewritten as

$$\begin{aligned} \frac{d\text{GPE}}{dt} \Big|_{\text{mixing}} &= - \int_V \mathbf{K} \nabla \Theta \cdot \nabla (P' \alpha) dV \\ &\quad + \int_V \mathbf{K} \nabla S \cdot \nabla (P' \beta) dV, \end{aligned}$$

which may be further rearranged to yield

$$\begin{aligned} \frac{d\text{GPE}}{dt} \Big|_{\text{mixing}} &= \int_V \mathbf{K} (\beta \nabla S - \alpha \nabla \Theta) \cdot \nabla P' dV \\ &\quad + \int_V P' [\mathbf{K} \nabla S \cdot \nabla \beta - \mathbf{K} \nabla \Theta \cdot \nabla \alpha] dV. \end{aligned} \quad (6)$$

The first term in the r.h.s. of (6) represents GPE gain due to the downward flux of buoyancy associated with diapycnal mixing, and is positive wherever there is vertical mixing across stable stratification. With reference to (3), this entails expansion at high pressure and contraction at low pressure, indicating isobaric upwelling at intermediate pressures. The second term in (6) represents GPE gain due to the net generation of buoyancy associated with mixing. This term may either be positive or negative due to spatial variability in  $\beta$  and especially  $\alpha$ . For a linear EOS,  $\beta$  and  $\alpha$  are uniform so this term vanishes, and the rate of GPE gain due to mixing is equal to the mixing energy transfer rate,  $\Gamma \varepsilon_K$ :

$$\begin{aligned} \frac{d\text{GPE}}{dt} \Big|_{\text{mixing}}^{\text{linear}} &= \int_V \mathbf{K} (\beta \nabla S - \alpha \nabla \Theta) \cdot \nabla P' dV \\ &= \int_V \kappa_v \rho N^2 dV = \int_V \Gamma \varepsilon_K dV, \end{aligned} \quad (7)$$

where  $\kappa_v$  is the vertical diapycnal diffusivity and  $N = \sqrt{g[\alpha \Theta_z - \beta S_z]}$ , where  $z$  subscripts indicate differentiation with respect to height. This is the formula considered by Munk and Wunsch [1998]. In the presence of nonlinearity in the EOS, both the diapycnal and isoneutral components of the second term in (6) make important contributions to the GPE budget. Here, we focus on the role of the diapycnal component in order to explore the relationship between mixing energy and GPE generation. This is given by

$$\begin{aligned} \frac{d\text{GPE}}{dt} \Big|_{\kappa_v} &= \frac{d\text{GPE}}{dt} \Big|_{\text{mixing}}^{\text{linear}} + \frac{d\text{GPE}}{dt} \Big|_{\kappa_v}^{\text{nonlin}} \\ &= \int_V \xi \Gamma \varepsilon_K dV. \end{aligned} \quad (8)$$

The vertical diapycnal component of the second term in (6) is

$$\frac{d\text{GPE}}{dt} \Big|_{\kappa_v}^{\text{nonlin}} = \int_V P' \kappa_v (S_z \beta_z - \Theta_z \alpha_z) dV. \quad (9)$$

This yields

$$\xi = 1 + \xi^{\text{nonlin}}, \quad \xi^{\text{nonlin}} = \frac{P' (S_z \beta_z - \Theta_z \alpha_z)}{\rho N^2}. \quad (10)$$

A positive value of  $\xi^{nonlin}$  would imply that nonlinearity in the EOS leads to an enhancement of GPE generation.  $\xi^{nonlin}$  may be further decomposed  $\xi^{nonlin} = \xi^{cab} + \xi^{therm}$ , where  $\xi^{cab}$  and  $\xi^{therm}$  are cabbelling and thermobaric components, respectively:

$$\xi^{cab} = \frac{P'(\beta_S(S_z)^2 - 2\alpha_S S_z \Theta_z - \alpha_\Theta (\Theta_z)^2)}{\rho N^2}, \quad (11)$$

$$\xi^{therm} = \frac{gP'(-\beta_P S_z + \alpha_P \Theta_z)}{N^2}, \quad (12)$$

where  $\Theta$ ,  $S$  and  $P$  subscripts indicate differentiation with respect to conservative temperature, salinity and pressure, respectively, and  $\beta_\Theta = -\alpha_S$  by definition. The cabbelling component is dominated by the final term in (11), and is negative in seawater because buoyancy, and therefore GPE, is destroyed by the mixing of waters of different temperatures ( $\alpha_\Theta > 0$ ). The thermobaric component is dominated by the final term in (12), and is positive where the vertical temperature gradient is positive. This is because warm water is less compressible than cold water ( $\alpha_P > 0$ ), so buoyancy is generated by fluxing heat to higher pressures.

The formula for  $\xi$ , derived above for a non-Boussinesq ocean, is also valid under the Boussinesq approximation applied in ocean models. In Boussinesq fluids, the rate of GPE generation by mixing is represented by the term  $\int_V g z \frac{D\rho}{Dt} dV$ , which is also the Boussinesq approximation to the compressible work [Nycander *et al.*, 2007; Tailleux, 2012a], and an equivalent formula for  $\xi$  arises from the duality between the non-Boussinesq and Boussinesq equations at hydrostatic equilibrium [de Szoeke and Samelson, 2000].

### 3. Application to global hydrography

Having derived expressions for  $\xi$  and its components, we now calculate climatological values for these terms throughout the global ocean using WOA 2005 practical salinities [Antonov *et al.*, 2006] and *in situ* temperatures [Locarnini *et al.*, 2006] and TEOS-10 calculations for absolute salinity, conservative temperature, and EOS variables  $\alpha$ ,  $\beta$  and  $\rho$  [IOC *et al.*, 2010].

The distributions of  $\xi$  and its components in the Atlantic and Pacific oceans are illustrated in Figure 1. Cabbelling associated with diapycnal mixing leads to loss of GPE throughout the global ocean, and is the dominant nonlinearity in the pycnocline. Where  $\xi^{cab} < -1$ , this GPE loss is greater than GPE gain due to the downward buoyancy flux associated with diapycnal mixing. This is the case in parts of the lower pycnocline and near the Mediterranean outflow, both locations where strong vertical temperature and salinity gradients lead to relatively weak vertical density gradients, so a small downward buoyancy flux can be associated with strong cabbelling. At greater depths, the cabbelling term decreases in relative importance due to reduced temperature stratification.

The thermobaric term leads to GPE gain associated with diapycnal mixing throughout the global ocean except where there is a negative vertical conservative temperature gradient (e.g. below Winter Water in the Southern Ocean). The mass of overlying water raised due to local expansion, associated with thermobaricity, increases with depth, explaining the increased importance of this term with depth. This also applies to the cabbelling term, but unlike  $\xi^{cab}$ ,  $\xi^{therm}$  is insensitive to the vertical conservative temperature gradient wherever temperature stratification dominates over salinity stratification. Where  $\xi^{therm} > 1$ , as is observed regionally

at depths greater than  $\sim 4500$  m, this GPE gain is greater than GPE gain due to the downward buoyancy flux associated with diapycnal mixing.

In summary,  $\xi$  deviates strongly from 1, the value that would be consistent with a linear EOS. The global mean at a depth of 500 m is 0.5, with negative values in parts of the tropical pycnocline.  $\xi$  exceeds 2 in some bottom waters, for which 1.5 is a representative value. This indicates that diapycnal mixing is typically three times as effective at generating GPE if it occurs in bottom waters rather than the pycnocline.

### 4. Discussion

Our results indicate that, in the low latitude pycnocline, diapycnal mixing results in a loss of GPE through cabbelling that is typically about 50% as great as the GPE gain due to the downward buoyancy flux associated with diapycnal mixing. Therefore, the nonlinearity in the EOS approximately doubles the mixing energy required to maintain a given GPE source here. However, the wind-driven circulation provides an adiabatic GPE source to the pycnocline, and the relative importance of diapycnal mixing in the GPE budget likely increases with depth. The canonical estimate of Munk and Wunsch [1998], of a mixing energy transfer rate of approximately  $\int_V \varepsilon_P = 0.4$  TW ( $\varepsilon_P = \Gamma \varepsilon_K$ , with  $\Gamma = 0.2$  and  $\int_V \varepsilon_K = 2.1$  TW) required to maintain the abyssal stratification, was made for depths of 1000-4000 m. At these depths, the effect of cabbelling on the ratio,  $\xi$ , of the rate of GPE generation to the mixing energy transfer rate is small because of weak vertical temperature gradients (the region of the Mediterranean outflow is a notable exception), and thermobaricity dominates. Therefore, nonlinearity in the EOS does not reduce GPE generation by diapycnal mixing as is often assumed, but enhances GPE generation by  $\sim 20\%$  (the mean value of  $\xi$  from 1000-4000 m is 1.2), increasing to  $\sim 100\%$  in bottom waters.

Previous studies have emphasised the role of cabbelling but not thermobaricity in ocean energetics. For example, Gnanadesikan *et al.* [2005] found that cabbelling is a leading order sink of GPE in the global ocean, whereas Tailleux [2009a] explored the regime  $\xi < 1$ , which typically arises due to cabbelling, but did not consider the regime  $\xi > 1$  which can only arise due to thermobaric effects. Such an approach may be justifiable in studies that focus on a subset of vertically-integrated quantities dominated by the upper ocean, such as ocean heat transport [Gnanadesikan *et al.*, 2005]. However, the importance of cabbelling in the vertical integral masks its near-negligible role, in comparison with thermobaricity, in the abyssal ocean.

The distinct roles of cabbelling and thermobaricity have been explicitly examined in the context of isoneutral mixing. Klocker and McDougall [2010] estimated the dianeu- tral transports that result from the nonlinear EOS due to a uniform isoneutral diffusivity, where a downward dianeu- tral transport corresponds to a loss of GPE. Thermobaric effects dominated over cabbelling in deep waters (isoneutral density greater than  $\sim 27.4 \text{ kg m}^{-3}$ ) in their study. Since isoneutral mixing entails mixing of waters of different temperatures, it invariably leads to a GPE sink associated with cabbelling. However, the thermobaric effect of isoneutral mixing term opposes the thermobaric effect of diapycnal mixing, leading to a globally integrated GPE sink. This may be understood if we consider that the thermobaric effect is dominated by the dependence of the compressibility of seawater on tem- perature, so that a flux heat of heat to greater pressures generates buoyancy and therefore GPE. Diapycnal mixing typically fluxes heat to higher pressures because vertical temperature gradients are positive over most of the ocean. However, the vertical temperature gradient along isoneutral

surfaces is negative over much of the ocean, most notably the Antarctic Circumpolar Current (ACC), where pressure and conservative temperature on an isoneutral surface both increase as one moves equatorward. Therefore, eddies in the ACC flux heat to lower pressures, destroying buoyancy and therefore decreasing GPE. Klocker and McDougall [2010] estimated that isoneutral mixing leads to approximately 6 Sv of dianeutral downwelling, in addition to the downwelling resulting from surface buoyancy exchange at high latitudes, which they suggested would be balanced by GPE input from diapycnal mixing. However, the heat that is fluxed upwards by isoneutral mixing must, at steady state, be returned to the deep ocean by a combination of diapycnal mixing and advection, thus tending to negate the destruction of buoyancy by isoneutral mixing in the abyssal ocean. Therefore, much of the GPE lost due to isoneutral mixing is likely to be balanced by thermobaric GPE gain associated with diapycnal mixing and/or advection, without the requirement for an additional mixing energy source.

Finally, we consider the impact of  $\xi$  on ocean dynamics. Fofonoff [1998, 2001] argued that diapycnal mixing would destabilise hydrographic structures with  $\xi < 0$  by converting GPE to kinetic energy, resulting in further mixing. This mechanism is unlikely to be seen in practice, since energy conversions associated with cabbeling/thermobaricity are typically between GPE and internal energy, as opposed to kinetic energy [McDougall *et al.*, 2003], and indeed our climatology indicates that the  $\xi < 0$  regime is stable over significant regions of the ocean. A more straightforward link to dynamics is through the effect of diapycnal mixing on horizontal pressure gradients. From Eqn (2), we see that processes that do not alter the mass of a water column, such as diapycnal mixing, yield identical responses in vertically integrated hydrostatic pressure and in GPE. (More generally, GPE tendencies are proportional to depth-integrated steric height tendencies.) Modelling studies indicate that the steady state meridional overturning circulation within each ocean basin is approximately proportional to the vertically integrated meridional pressure gradient above an intermediate scale depth, with upper ocean flow from high to low pressure [de Boer *et al.*, 2010, and references therein]. Provided that  $\xi > 0$ , this implies that regionally strengthened diapycnal mixing at low- or mid-latitudes should, at steady state, lead to enhanced upwelling in that region and a strengthened global MOC, a conclusion that is supported for the North Atlantic and for the Indo-Pacific basins by the linear-EOS experiments of Oliver and Edwards [2008]. However, where  $\xi < 0$ , diapycnal mixing tends to decrease local vertically-integrated pressure, leading to the possibility that mixing at such locations tends to weaken the MOC.

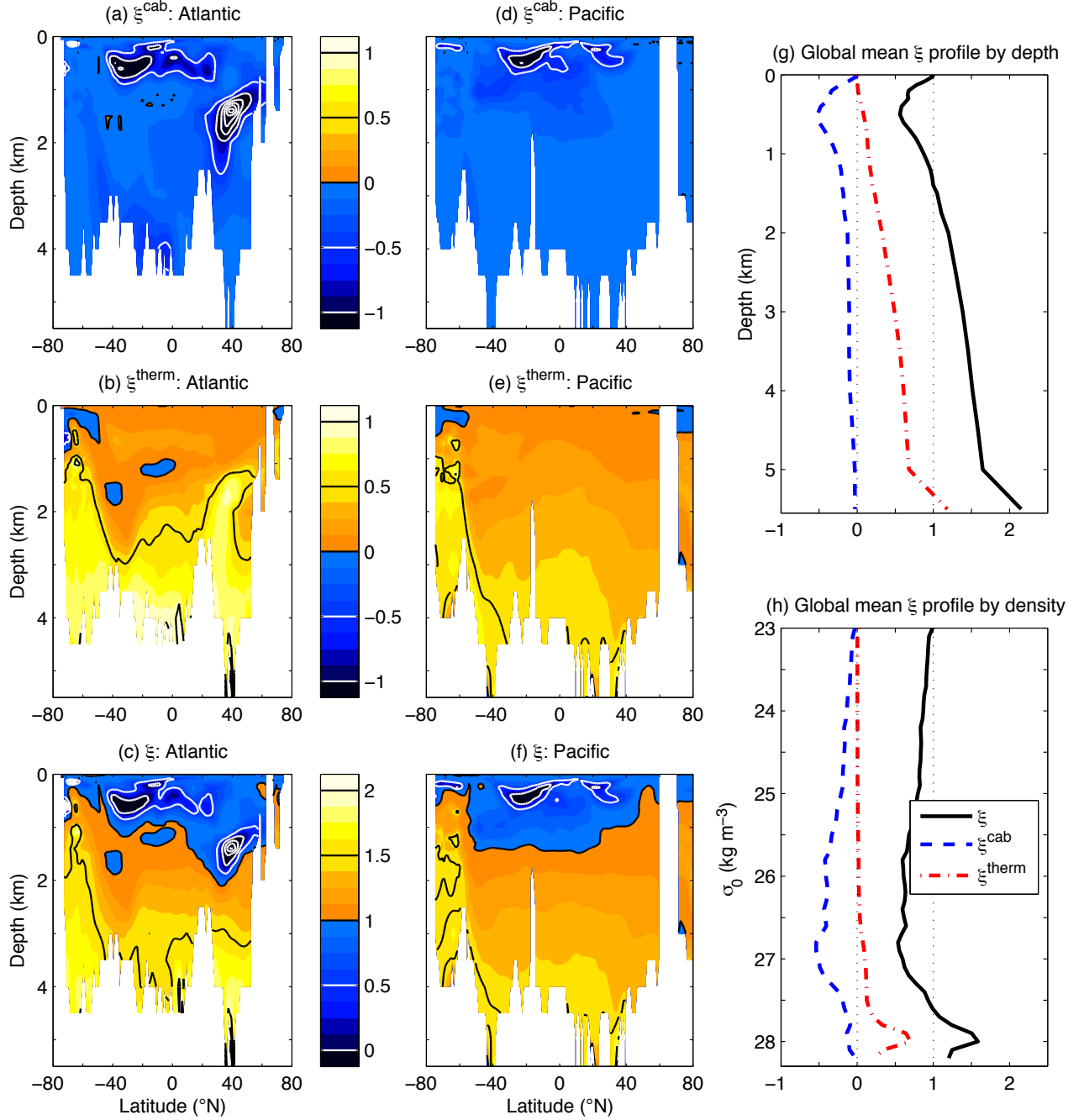
**Acknowledgments.** The Leverhulme Trust and the UK THCMIP RAPID programme are acknowledged for support.

## References

- Antonov, J. I., Locarnini, R. A., Boyer, T. P., Mishonov, A. V., and Garcia, H. E. (2006). *World Ocean Atlas 2005, Volume 2: Salinity*. Levitus, Ed. NOAA Atlas NESDIS 62, U.S. Government Printing Office, Washington, D.C., 182 pp.
- de Boer, A. M., Gnanadesikan, A., Edwards, N. R., and Watson, A. J. (2010). Meridional density gradients do not control the atlantic overturning circulation. *J. Phys. Oceanogr.*, **40**, 368–380.
- de Szoeke, R. A. and Samelson, R. M. (2000). The duality between the Boussinesq and non-Boussinesq hydrostatic equations of motion. *J. Phys. Ocean.*, **32**, 21942203.
- Fofonoff, N. P. (1998). Nonlinear limits to ocean thermal structure. *J. Marine Res.*, **56**, 793–811.
- Fofonoff, N. P. (2001). Thermal stability of the world ocean thermoclines. *J. Phys. Oceanogr.*, **31**, 2169–2177.
- Gnanadesikan, A., Slater, R. D., Swathi, P. S., and Vallis, G. F. (2005). The energetics of ocean heat transport. *J. Climate*, **18**, 2604–2616.
- IOC, SCOR, and IAPSO (2010). *The international thermodynamic equation of seawater 2010: Calculation and use of thermodynamic properties*. Intergovernmental Oceanographic Commission, Manuals and Guides No. 56, UNESCO (English), 196 pp.
- Klocker, A. and McDougall, T. J. (2010). Influence of the nonlinear equation of state on global estimates of dianeutral advection and diffusion. *J. Phys. Oceanogr.*, **40**, 1690–1709.
- Kunze, E., Firing, E., Hummon, J. M., Chereskin, T. K., and Thurnherr, A. M. (2006). Global abyssal mixing inferred from lowered ADCP shear and CTD strain profiles. *J. Phys. Oceanogr.*, **36**, 1553–1576.
- Locarnini, R. A., Mishonov, A. V., Antonov, J. I., Boyer, T. P., and Garcia, H. E. (2006). *World Ocean Atlas 2005, Volume 1: Temperature*. Levitus, Ed. NOAA Atlas NESDIS 61, U.S. Government Printing Office, Washington, D.C., 182 pp.
- McDougall, T. J. (2003). Potential enthalpy: A conservative oceanic variable for evaluating heat content and heat fluxes. *J. Phys. Oceanogr.*, **33**, 945963.
- McDougall, T. J., Church, J. A., and Jackett, D. R. (2003). Does the nonlinearity of the equation of state impose an upper bound on the buoyancy frequency? *J. Mar. Res.*, **61**, 745–764.
- Munk, W. and Wunsch, C. (1998). Abyssal recipes II: Energetics of tidal and wind mixing. *Deep-Sea Res. I*, **45**, 1977–2010.
- Nycander, J., Nilsson, J., Döös, K., and Broström, G. (2007). Thermodynamic analysis of ocean circulation. *J. Phys. Oceanogr.*, **37**, 20382052.
- Oakey, N. S. (1982). Determination of the rate of dissipation of turbulent energy from simultaneous temperature and velocity shear microstructure measurements. *J. Phys. Oceanogr.*, **12**, 256–271.
- Oliver, K. I. C. and Edwards, N. R. (2008). Location of potential energy sources and the export of dense water from the Atlantic Ocean. *Geophys. Res. Lett.*, **35**, 10.1029/2008GL035537.
- Osborn, T. R. (1980). Estimates of the local rate of vertical diffusion from dissipation measurements. *J. Phys. Oceanogr.*, **10**, 83–89.
- Peltier, W. R. and Caulfield, C. P. (2003). Mixing efficiency in stratified shear flows. *Rev. Fluid Mech.*, **35**, 135–167.
- Scotti, A. and White, B. (2011). Is horizontal convection really “non-turbulent?”. *Geophys. Res. Lett.*, **38**, L21609, doi:10.1029/2011GL049701.
- St. Laurent, L. and Simmons, H. (2006). Estimates of power consumed by mixing in the ocean interior. *J. Clim.*, **19**, 4877–4890.
- Tailleux, R. (2009). On the energetics of stratified turbulent mixing, irreversible thermodynamics, Boussinesq models and the ocean heat engine controversy. *J. Fluid Mech.*, **638**, 339–382.
- Tailleux, R. (2009b). Understanding mixing efficiency in the oceans: Do the nonlinearities of the equation of state matter? *Ocean Science*, **5**, 271–283.
- Tailleux, R. (2012a). Thermodynamics/dynamics coupling in weakly compressible turbulent stratified fluids. *ISRN Thermodynamics*, **2012**, 609701, doi:10.5402/2012/609701.
- Tailleux, R. (2012b). Irreversible compressible work and APE dissipation in turbulent stratified fluids. *Physica Scripta*, in press.
- Toggweiler, J. R. and Samuels, B. (1998). On the ocean’s large-scale circulation near the limit of no vertical mixing. *J. Phys. Oceanogr.*, **28**, 1832–1852.

K. I. C. Oliver, National Oceanography Centre Southampton, University of Southampton, Southampton SO14 3ZH, U.K. (K.Oliver@noc.soton.ac.uk)

R. Tailleux, Department of Meteorology, University of Reading, Earley Gate, PO Box 243, Reading, RG6 6BB, UK. (R.G.J.Tailleux@reading.ac.uk)



**Figure 1.** Distribution of the ratio,  $\xi$ , of the GPE generation rate to the mixing energy transfer rate in the Atlantic Ocean at 18.5°W (left panels), the Pacific Ocean at 145.5°W (middle panels), and for global mean profiles (right panels). The components associated with the non-linear EOS are GPE generation by cabbelling ( $\xi_{cab}$ , top row), which is negative, and GPE generation due to thermobaricity ( $\xi_{therm}$ , second row).  $\xi = 1 + \xi_{cab} + \xi_{therm}$  is presented in the bottom row. Contour intervals are 0.5, with white contours at  $\xi_{cab} < 0$ ,  $\xi_{therm} < 0$  or  $\xi < 1$ . Intervals in shading are 0.125.