

Predicting Mesh Density for Adaptive Modelling of the Atmosphere

Motivation

- Adaptive meshing for improved resolution of important features without the expense of high resolution globally. Features such as:
 - Tropical cyclones
 - Extratropical fronts
 - Deep convection
- But mesh adaptation is expensive and can introduce errors
- So can it be done less frequently?
- How to predict in advance where resolution will be needed?

OpenFOAM

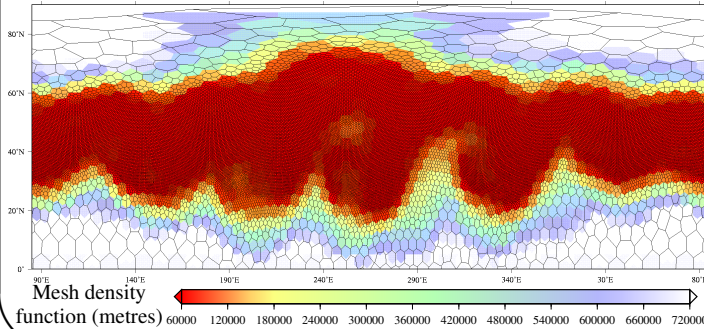
- Open source, free software library released by OpenCFD
www.opencfd.co.uk
- Finite-volume on 3D polyhedral meshes in parallel

AtmosFOAM

- Currently global shallow water model written using OpenFOAM
- Quadratic and cubic differencing schemes explicit correction on implicit linear differencing
- Quadratic interpolation onto new meshes

Voronoi Meshes based on a Given Density Function

- Points are added and removed so that the point density conforms approximately to a given density function
- Points are Delaunay triangulated (using CGAL)
- Triangle edges are treated as springs with un-stretched edge length equal to given density function
- Springs are relaxed
- Voronoi dual used as mesh for AtmosFOAM



Outcomes

- At day 6 the adaptive model uses 21% of the cells of the mesh with uniform resolution as fine as the finest adaptive resolution.
- Remeshing every 12 hours (72 time steps) rather than every 1 or 20 minutes (St-Cyr et al, 2008) or every time step (Läuter et al, 2007).
- Power et al (2006) used one adjoint step to estimate where to refine for the following 40 time steps. But non-linear interactions cannot be predicted.
- Refined region of mesh does not lag behind regions of intense activity.
- Refinements based on $|\nabla \sqrt{\zeta^2 + \delta^2}|$ more efficient than based on $\sqrt{\zeta^2 + \delta^2}$.
- Technique could be used with convection parameterisation on coarse mesh to predict where high resolution will be needed to resolve deep convection before it breaks out.

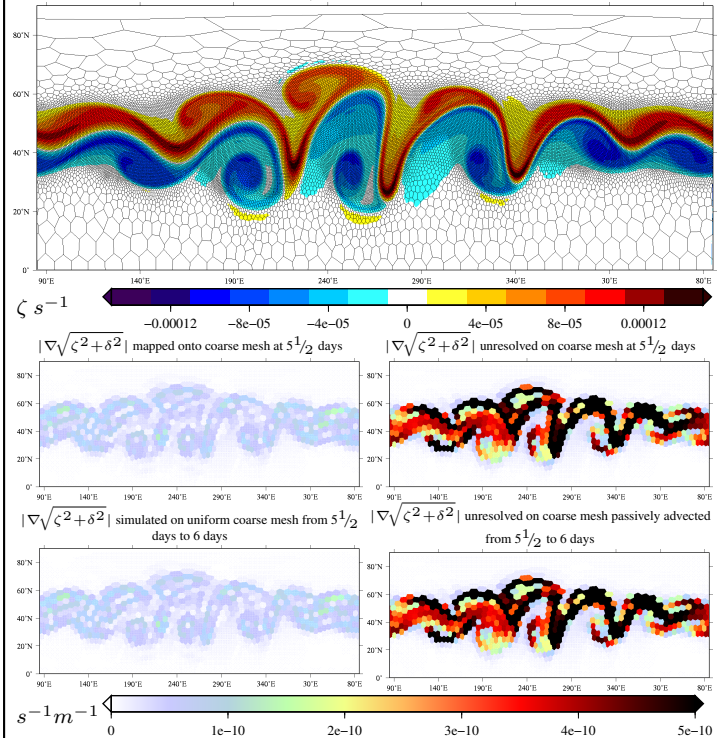
References

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- Läuter, M. et al, 2007 *J. Comp. Phys* 223:609-628
- Power, P.W. et al, 2006 *Ocean Modelling* 15:3-38
- St-Cyr, A. et al, 2008 *Mon. Wea. Rev.* 136:1898-1922
- Hilary Weller, and H.G. Weller. 2007. *Int. J. Num. Meth. Fluids* 56:1589-1596
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Adaptation Procedure

- Barotropically unstable jet test case of Galesky et al (2004).
- Mesh adaptation every 12 hours

Vorticity (ζ) and mesh at $5\frac{1}{2}$ days, before remeshing (31,467 cells)



Based on coarse mesh results (2,562 cells) over 12 hours, calculate required mesh density function and remesh

If δx = mesh density function

$$1/\delta x = 1/\delta x_{\max} + (1/\delta x_{\min} - 1/\delta x_{\max})$$

$$\max \left(\max(R_{rc}, \max_{12 \text{ hours}} R_r) / R_{rc}, \max(R_{uc}, \max_{12 \text{ hours}} R_u) / R_{uc} \right)$$

where $R_r = |\nabla \sqrt{\zeta^2 + \delta^2}|$ resolved on the coarse mesh

$R_u = |\nabla \sqrt{\zeta^2 + \delta^2}|$ unresolved and advected on the coarse mesh

R_{rc} = critical value for $R_c = 1 \times 10^{-10} \text{ s}^{-1} \text{ m}^{-1}$

R_{uc} = critical value for $R_u = 4 \times 10^{-10} \text{ s}^{-1} \text{ m}^{-1}$

$\delta x_{\max} = 960 \text{ km}$

$\delta x_{\min} = 60 \text{ km}$

Vorticity and mesh at $5\frac{1}{2}$ days, after remeshing (34,601 cells)

