

# Intercomparison of methods of coupling between convection and large-scale circulation

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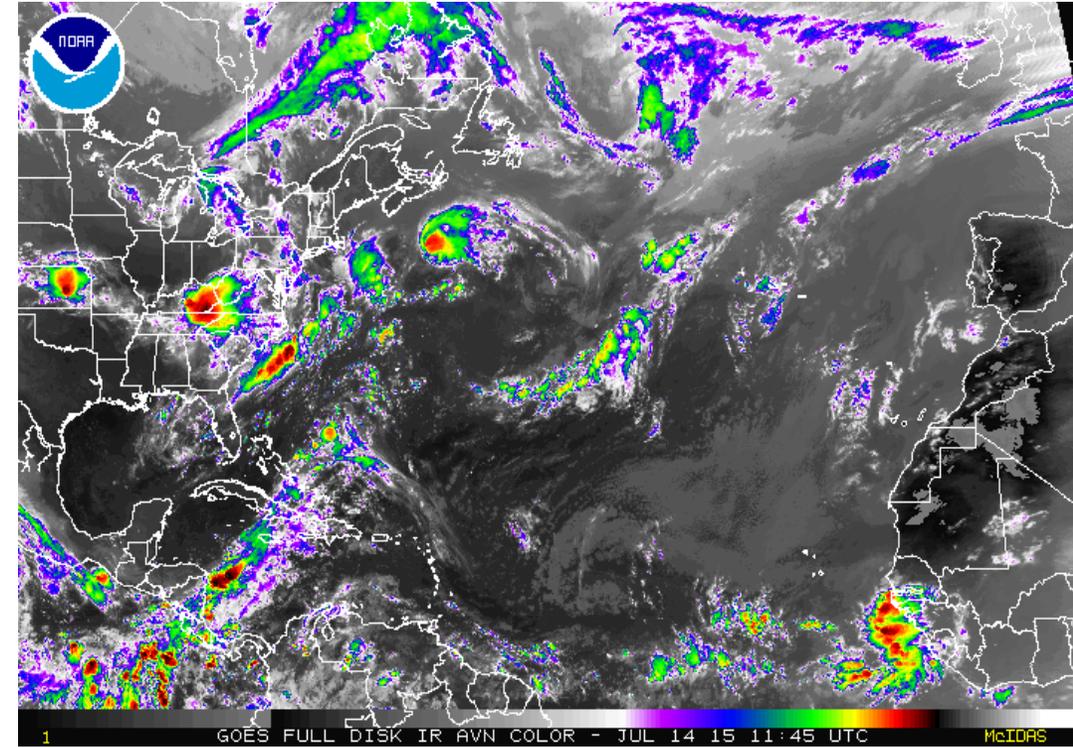
- Background
- Different methods of coupling between convection and large-scale circulation
- Motivation
- Models that participated in this project
- Experimental setup
- Results
- Conclusion

# Background

## Understand tropical climate and its variability

Science questions:

- What initiates tropical convection?
- What conditions favour moist convection?
- How is moist convection interacts with the large-scale tropical environment?
- Why is tropical convection often organized in clusters?
- what conditions favour and what intensifies the aggregation of convection?

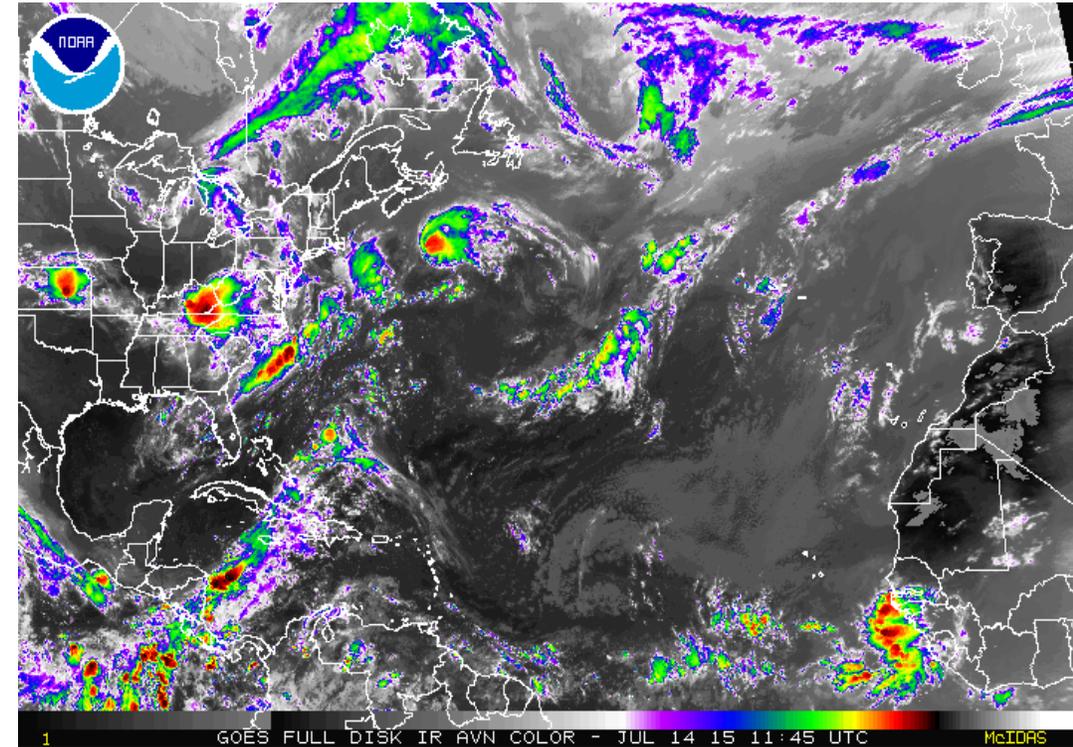


Snapshot of clouds taken on July 15<sup>th</sup> 2015 at 11:00 UTC.  
[http://www.ssd.noaa.gov/PS/TROP/Basin\\_Atlantic.html](http://www.ssd.noaa.gov/PS/TROP/Basin_Atlantic.html)

# Background

## Understand tropical climate and its variability

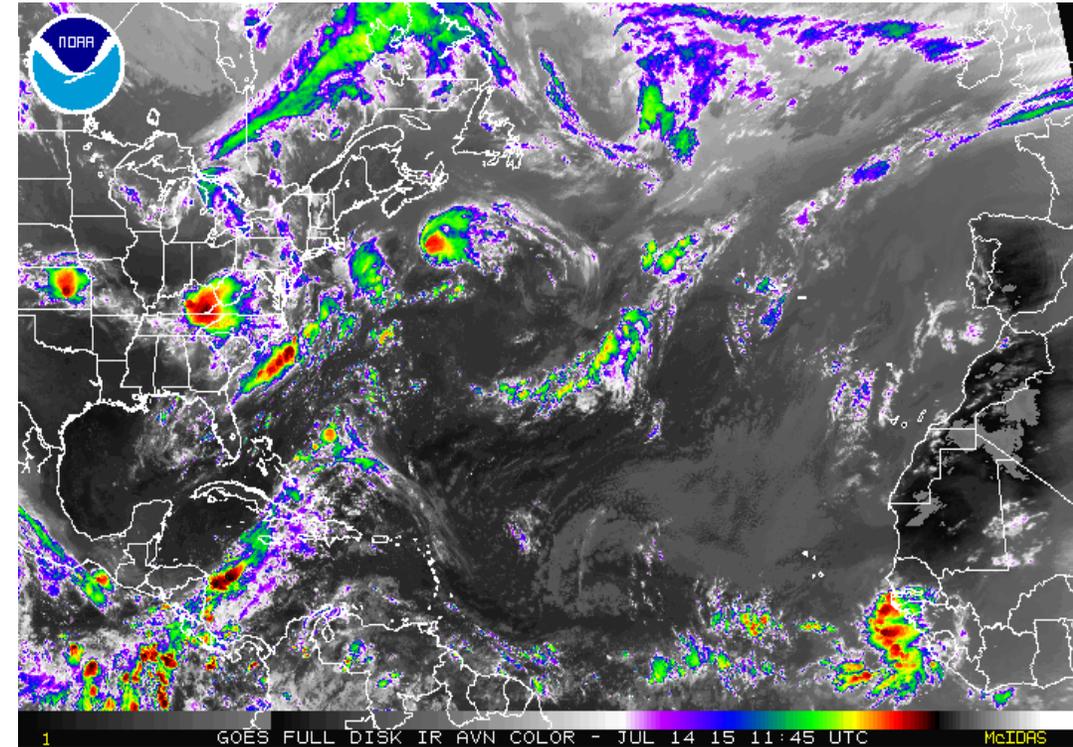
- Option 1: observations
- Option 2: modelling



# Background

## Understand tropical climate and its variability

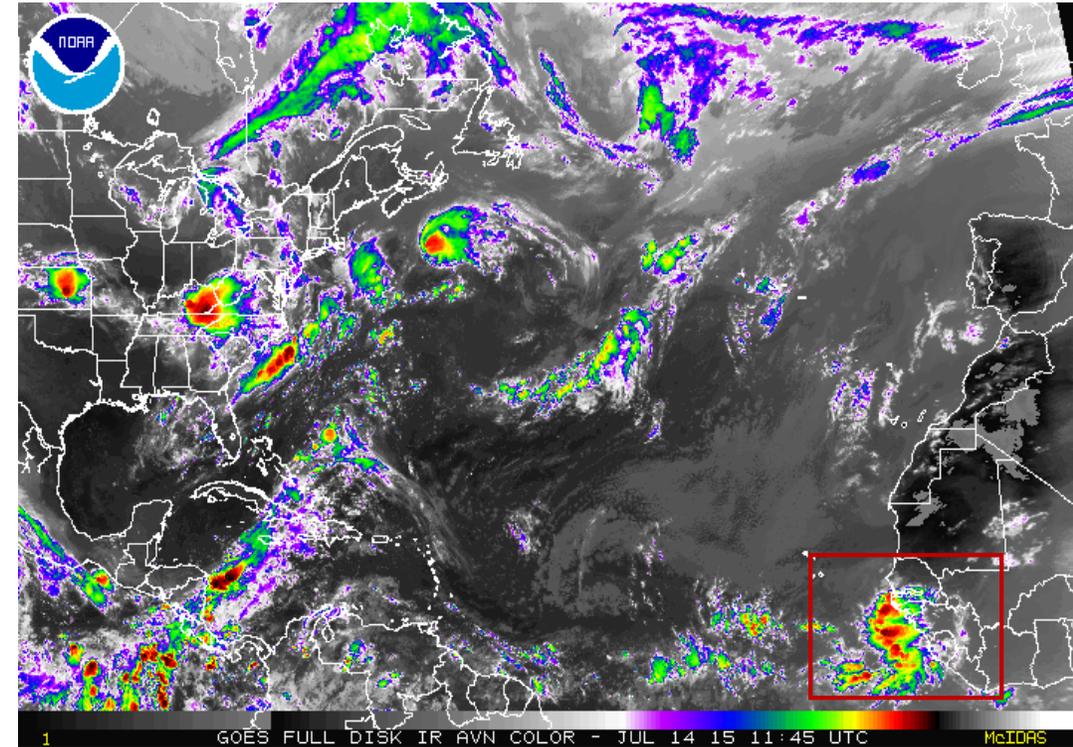
- Option 1: observations
  - Field campaign with the appropriated meteorological instruments is very expensive
  - The real atmosphere is complicated
- Option 2: modelling
  - Discrepancies between observations and numerical simulations
  - Numerical models lack the representation of many real phenomena



# Background

## Understand tropical climate and its variability

- Option 2.1: modelling- Entire tropic
- Option 2.2: modelling- Limited area



# Background

## Understand tropical climate and its variability

- Option 2.1: modelling- Entire tropic  
individual convective cell  $\sim 100\text{m}-10\text{ km}$   
large-scale circulation  $\sim 10\ 000\text{ km}$

Large range of spatial scales between

**convective cells and large-scale circulation:**

Large domain CRMs ( $\sim 10000\text{km}$ ) or GCMs with  
very high horizontal resolution

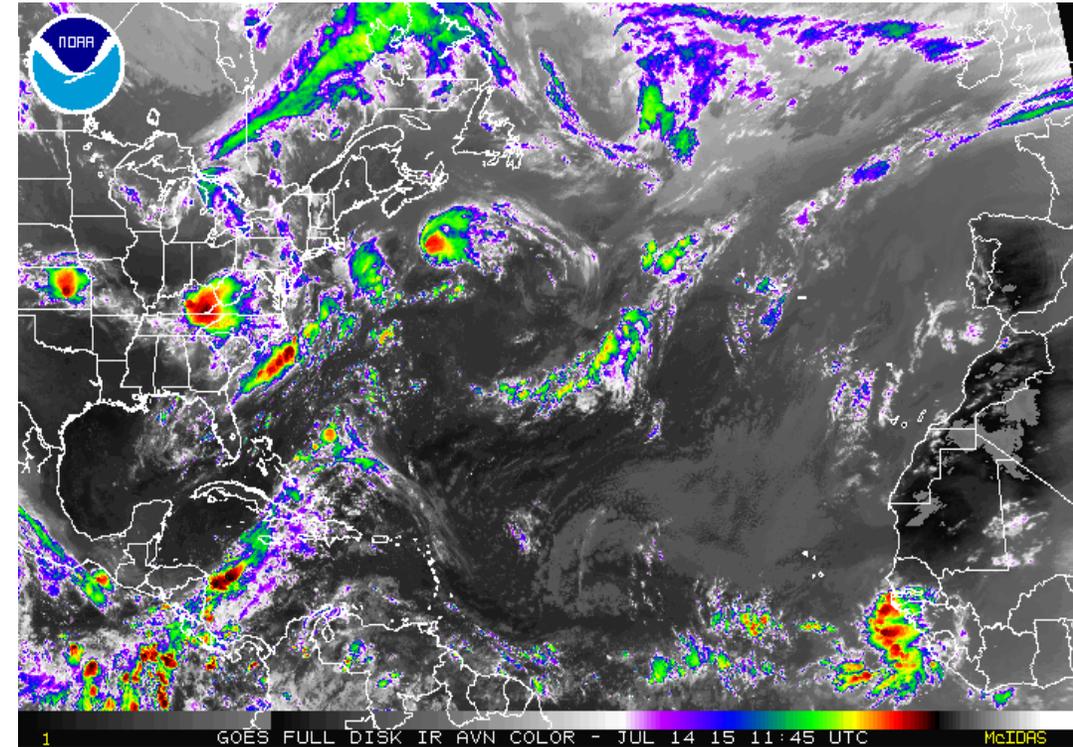
Large-domain, high-resolution experiments:

Cascade project (*Holloway et al., 2012*)

Computationally expensive

Alternative approach

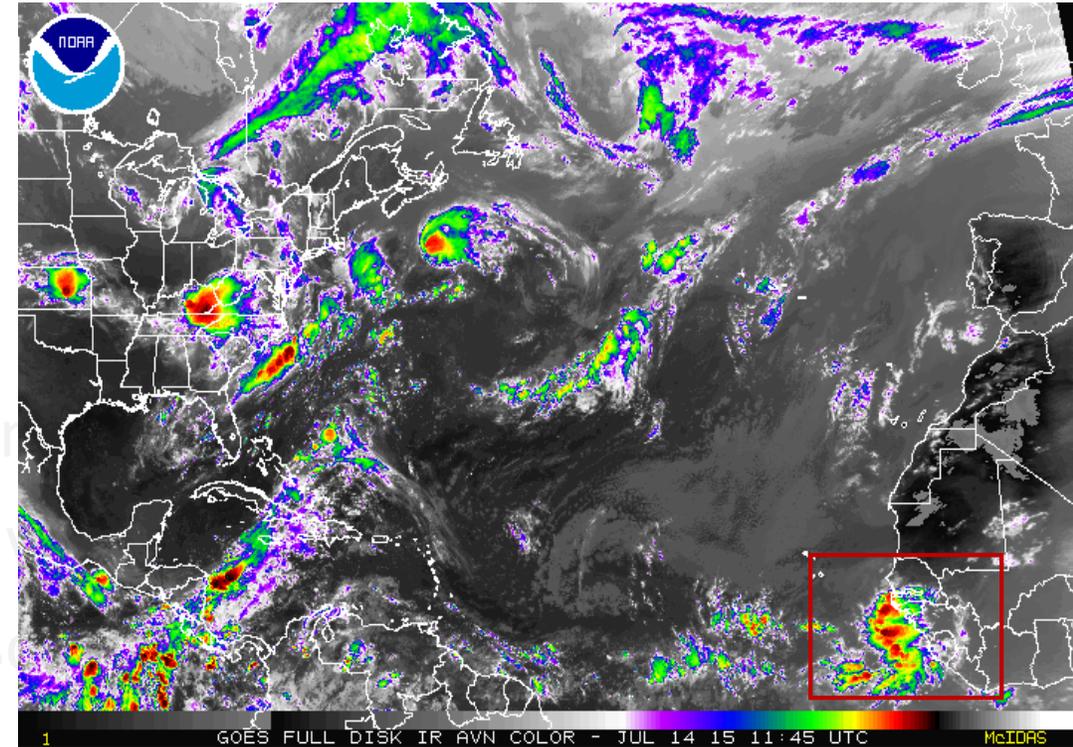
GCMs, but convection is parameterized.



# Background

## Understand tropical climate and its variability

- Option 2.1: modelling- Entire tropic GCMs, but convection is parameterized. Only few studies have simulated both convection
- Large domain CRMs (~ 10000km) or GCMs with
- Large-domain, high-resolution experiments: Cas



- Option 2.2: modelling- Limited area  
Computationally cheap compared to option 2.1  
CRMs are powerful tools to simulate tropical convection

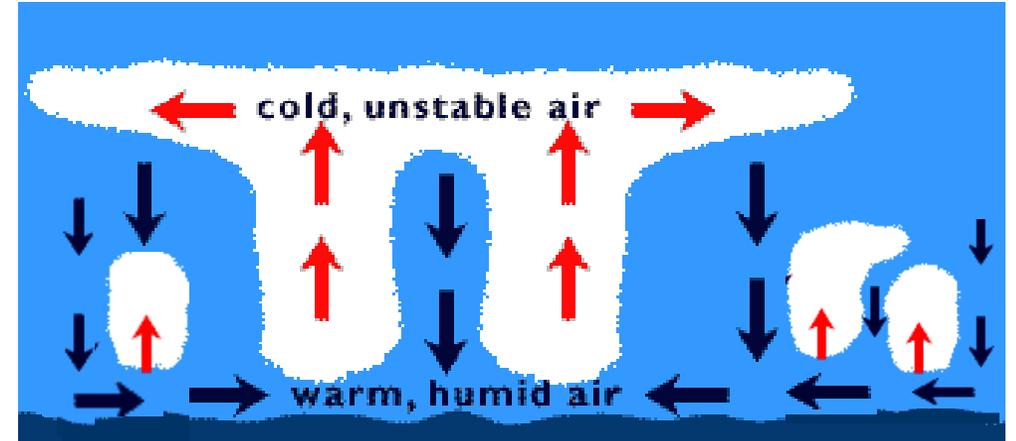
## Understand tropical climate and its variability

- Option 2.2: modelling- Limited area
  - CRMs are often run in RCE mode
  - Convection generates  $T'$
  - $T'$  drives a circulation
  - Cyclic BCs=winds turn inward
  - $T'$  cannot escape from the box

$$Evap - Precip = 0$$

and

$$LHF + SHF + Rad = 0$$



convection is disconnected from the influence of the large-scale flows

## Understand tropical climate and its variability

- Option 2.2: modelling- Limited area  
In the real world we need the influence of the surrounding environment

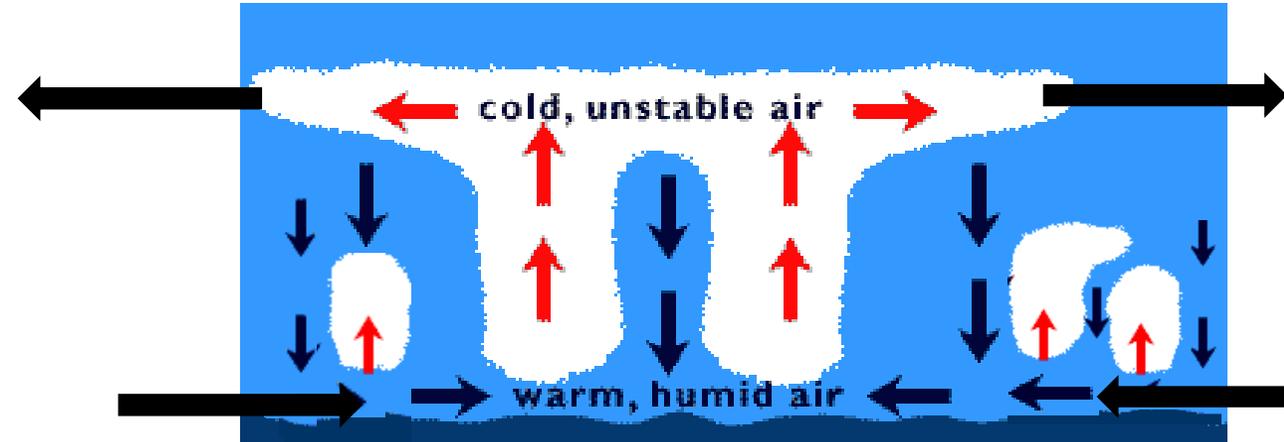
$(\bar{u}_e, \bar{v}_e, \bar{w}_e)$

$$Evap - Precip + \mathbf{M}_e = 0$$

And

$$LHF + SHF + Rad + \mathbf{H}_e = 0$$

The environmental large-scale flow  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$  has been shown to modulate convection (Daleu et al 2015)



Representation of the large-scale flow in limited area models

# Background

## Understand tropical climate and its variability

- Option 2.2.1: modelling- Limited area-Imposed  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$   
 $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$  idealized profiles or defined from observations

- Large horizontal temperature gradients over the tropics (compared to observations over the tropics)
- convection does not feedback on the large-scale flow



- The rain rate is too much constrained

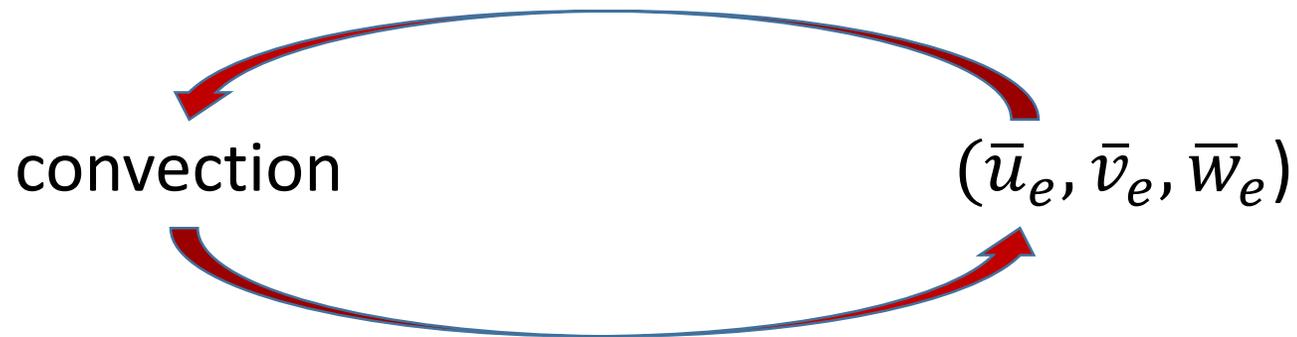
“what controls large-scale variations of tropical deep convection?”

## Understand tropical climate and its variability

- Option 2.2.1: modelling- Limited area- Imposed  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$

To understand “what controls large-scale variations of tropical deep convection?”

There is a need of frameworks which allow:

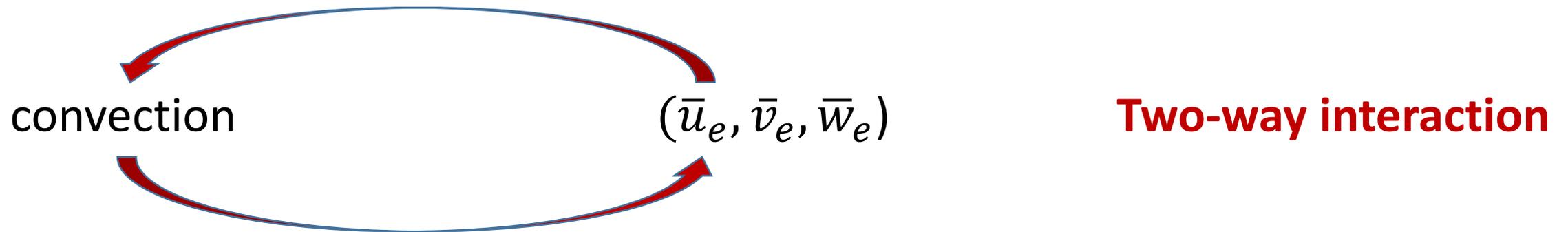


## Understand tropical climate and its variability

- Option 2.2.1: modelling- Limited area- Imposed  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$

To understand “what controls large-scale variations of tropical deep convection?”

There is a need of frameworks which allow:



- Option 2.2.2: modelling- Limited area-parameterized  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$

Let  $(\bar{u}_e, \bar{v}_e, \bar{w}_e)$  be parameterized by the model itself

## Understand tropical climate and its variability

- Option 2.2.2: modelling- Limited area- parameterized ( $\bar{u}_e, \bar{v}_e, \bar{w}_e$ )
  - Parameterization of the large-scale dynamics in SCMs and CRMs
  - Simplified circulation models
  - Parameterized environment using
- Weak-Temperature Gradient (WTG) / Spectral WTG (SWTG)
- Damped Gravity waves (DGW) / Weak Pressure gradient (WPG)

## Understand tropical climate and its variability

- Option 2.2.2: Modelling- Limited area- parameterized ( $\bar{u}_e, \bar{v}_e, \bar{w}_e$ )

Parameterization of the large-scale dynamics in SCMs and CRMs

Different methods as well as different models of convection are used in different studies.

Previous results show **both similarities and discrepancies in model behaviour**

Can we attribute differences in the published results to either **large-scale parameterization method or model of convection?**

**Time for an intercomparison !**

Proposed at the 1<sup>st</sup> Pan-GASS meeting in Sept 2012. Launched in February 2014.

- We performed a systematic comparison of the behaviour of a set of CRMs and SCMs under the same large-scale parameterization method; the **WTG method and the DGW method**
- We performed a systematic comparison of the WTG and DGW methods with a consistent implementation in a set of models with different physics and numerics.

Our points of interest are:

**Q1:** Can a large-scale circulation develop over uniform SST?

**Q2:** Can given SST and  $T$  profile support both a rainy and dry state, depending on initial moisture conditions?

**Q3:** How sensitive is a model (under the WTG/DGW method) to changes in the SST?

# The weak temperature gradient

$$\frac{\partial \theta}{\partial t} + \vec{U}_h \cdot \nabla_h \theta + W \frac{\partial \theta}{\partial z} = Q_d \text{ (diabatic heating)}$$

In the tropics, gravity waves redistribute  $\theta'$ . Thus,  $\nabla_h \theta$  is very small

At equilibrium  $\frac{\partial \theta}{\partial t} \sim 0$

# The weak temperature gradient

$$\cancel{\frac{\partial \theta}{\partial t}} + \cancel{\vec{U}_h \cdot \nabla_h \theta} + W \frac{\partial \theta}{\partial z} = Q_d$$

## Strict WTG method

*Sobel and Bretherton (2000)*

- $\frac{\partial \theta}{\partial t} = 0$
- $\nabla_h \theta = \mathbf{0}$
- $W_{wtg} \frac{\partial \theta}{\partial z} = Q_d$

# The weak temperature gradient

$$\cancel{\frac{\partial \theta}{\partial t}} + \cancel{\vec{U}_h \cdot \nabla_h \theta} + W \frac{\partial \theta}{\partial z} = Q_d$$

## **Strict** WTG method

*Sobel and Bretherton (2000)*

- $\frac{\partial \theta}{\partial t} = 0$
- $\nabla_h \theta = \mathbf{0}$
- $W_{wtg} = Q_d / \frac{\partial \theta}{\partial z}$

versus

## **Relaxed** WTG method

*Raymond and zeng 2005*

$$\frac{\partial \theta}{\partial t} = 0$$

$\nabla_h \theta$  is small

$$W_{wtg} = (\bar{\theta} - \theta_{Ref}) / \left( \tau \frac{\partial \theta}{\partial z} \right)$$

$\tau$  is the adjustment time scale

Small but  $\neq 0$

# The damped gravity wave

- Anelastic linearized perturbation equations of momentum:

$$\bar{\rho} \frac{\partial u'}{\partial t} = -\frac{\partial p'}{\partial x} - \epsilon \bar{\rho} u' \quad , \quad \bar{\rho} \frac{\partial v'}{\partial t} = -\frac{\partial p'}{\partial y} - \epsilon \bar{\rho} v'$$

- Continuity:  $\frac{\partial \bar{\rho} u'}{\partial x} + \frac{\partial \bar{\rho} v'}{\partial y} + \frac{\partial \bar{\rho} w'}{\partial z} = 0$

- Hydrostatic balance:  $\frac{\partial p'}{\partial z} = \bar{\rho} g \frac{T'}{\bar{T}}$

# The damped gravity wave

- Anelastic linearized perturbation equations of momentum:

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- Hydrostatic balance:  $\frac{\partial p'}{\partial z} = \bar{\rho} g \frac{T'}{\bar{T}}$

- Solution, single horizontal wave number  $k$ :  $\frac{\partial}{\partial z} \left\{ \left( \frac{\partial}{\partial t} + \epsilon \right) \frac{\partial \bar{\rho} w'}{\partial z} \right\} = -k^2 \frac{\bar{\rho} g}{\bar{T}} T'$

- At equilibrium  $\frac{\partial}{\partial t} \sim 0$  and  $\frac{\partial}{\partial z} \left\{ \epsilon \frac{\partial \bar{\rho} w'}{\partial z} \right\} = -k^2 \frac{\bar{\rho} g}{\bar{T}} T'$

$$\bar{\omega} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial p} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau}$$

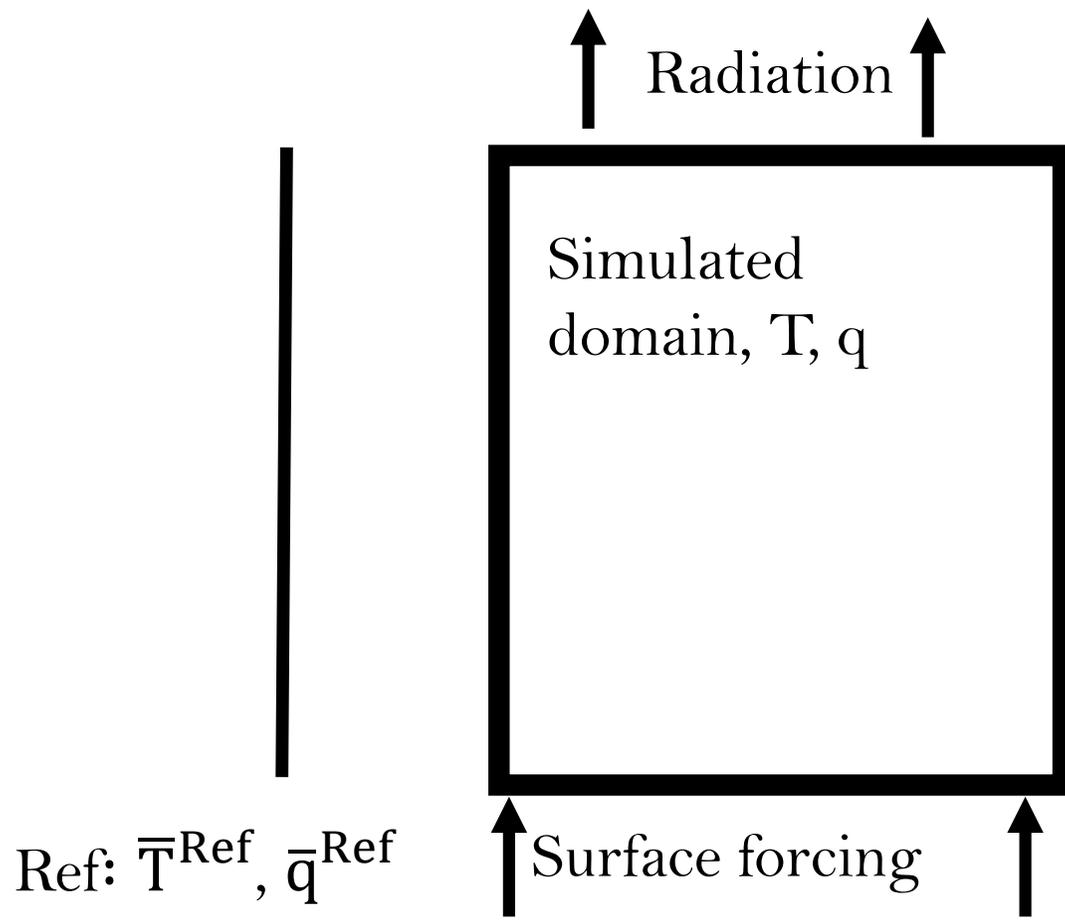
$$\frac{\partial}{\partial p} \left( \varepsilon \frac{\partial \bar{\omega}}{\partial p} \right) = \frac{k^2 R_d}{\bar{p}^{\text{Ref}}} (\bar{T}_v - \bar{T}_v^{\text{Ref}})$$

How do we implement the WTG and DGW methods

$$\bar{\omega} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial p} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau}$$

$$\frac{\partial}{\partial p} \left( \varepsilon \frac{\partial \bar{\omega}}{\partial p} \right) = \frac{k^2 R_d}{\bar{p}^{\text{Ref}}} \left( \bar{T}_v - \bar{T}_v^{\text{Ref}} \right)$$

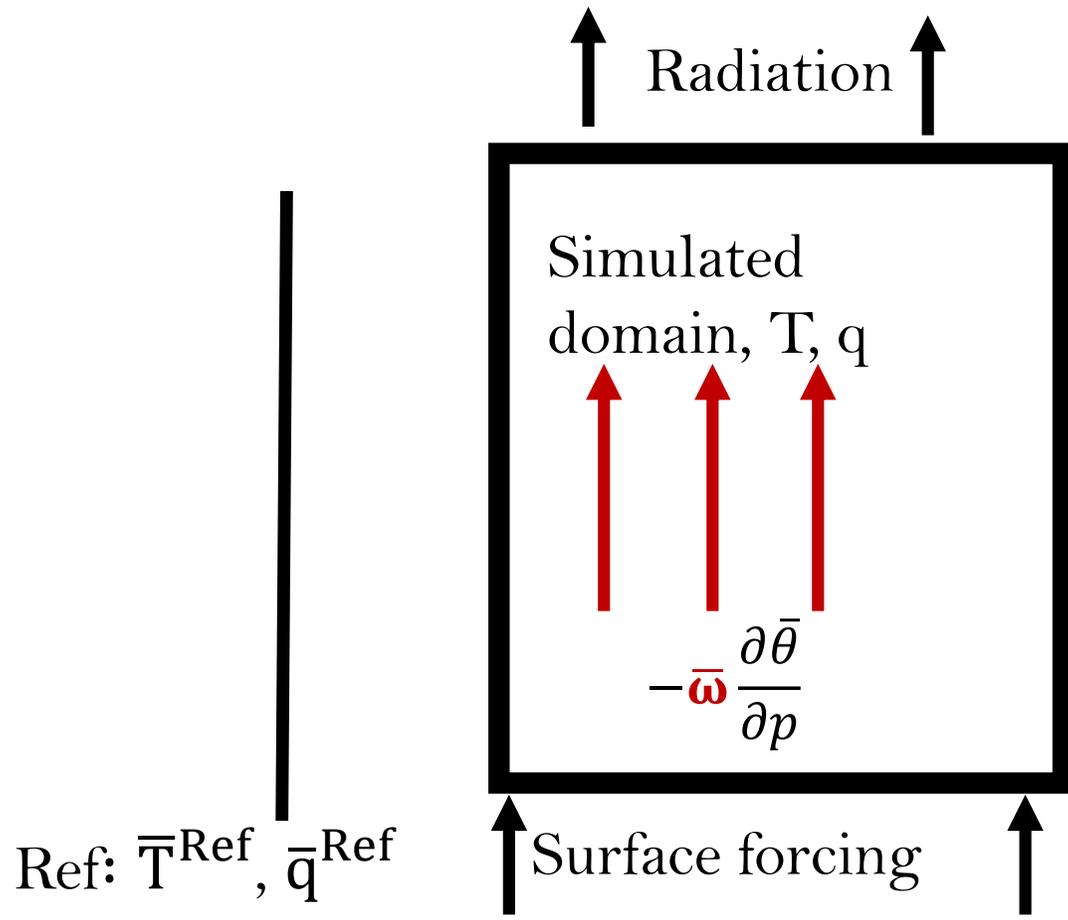
How do we implement the WTG and DGW methods



$\bar{\omega}$  is used to advect  $\theta$  and water vapour

# WTG method

$$\bar{\omega} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial p} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau}$$



# DGW method

$$\frac{\partial}{\partial p} \left( \varepsilon \frac{\partial \bar{\omega}}{\partial p} \right) = \frac{k^2 R_d}{\bar{p}^{\text{Ref}}} (\bar{T}_v - \bar{T}_v^{\text{Ref}})$$

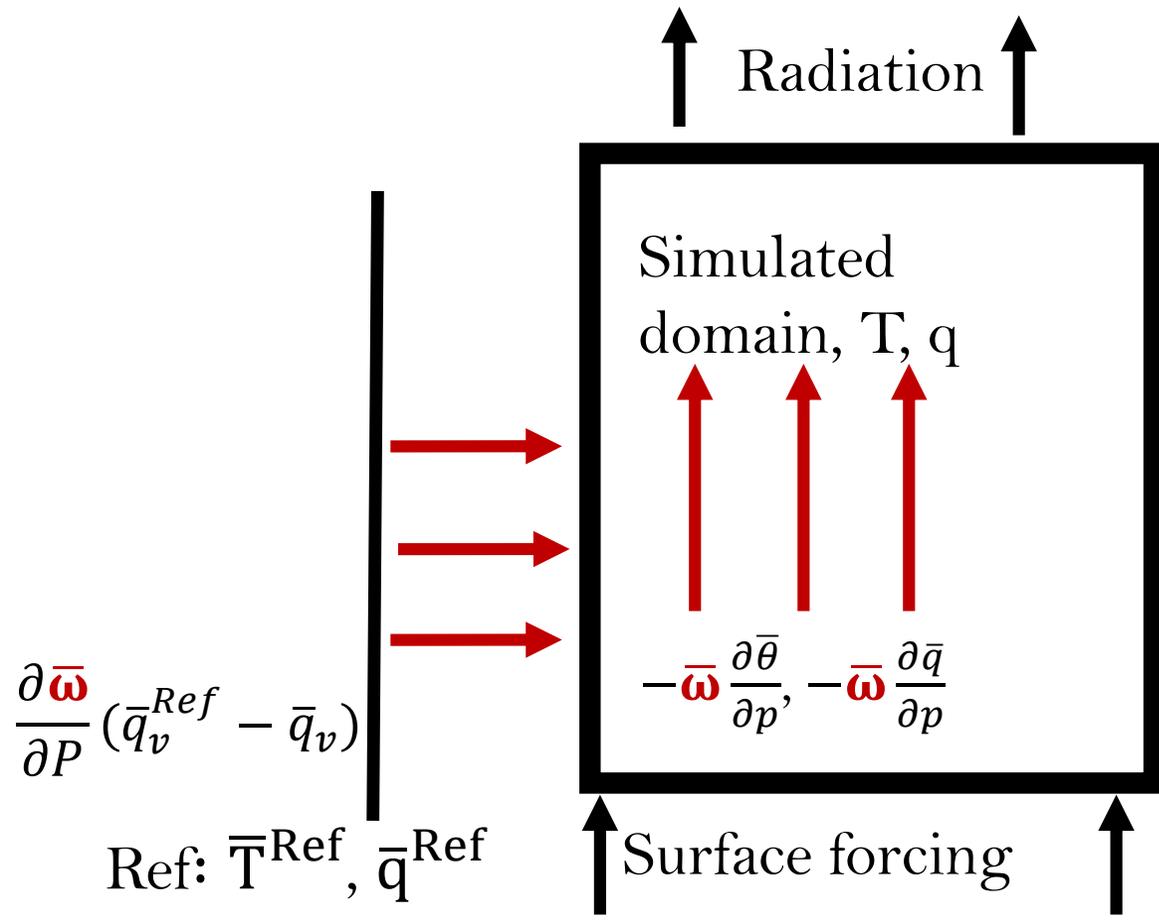
Temperature tendencies due to  $\bar{\omega}$

$$\frac{\partial \theta}{\partial t} = -\bar{\omega} \frac{\partial \bar{\theta}}{\partial p}$$

$\bar{\omega}$  cancels  $\theta'$  via adiabatic lifting

# WTG method

$$\bar{\omega} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial p} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau}$$



# DGW method

$$\frac{\partial}{\partial p} \left( \varepsilon \frac{\partial \bar{\omega}}{\partial p} \right) = \frac{k^2 R_d}{\bar{p}^{\text{Ref}}} (\bar{T}_v - \bar{T}_v^{\text{Ref}})$$

Temperature tendencies due to  $\bar{\omega}$

$$\frac{\partial \theta}{\partial t} = -\bar{\omega} \frac{\partial \bar{\theta}}{\partial p}$$

$\bar{\omega}$  cancels  $T'$  via adiabatic lifting

Moisture tendencies due to  $\bar{\omega}$

$$\frac{\partial q_v}{\partial t} = -\bar{\omega} \frac{\partial \bar{q}_v}{\partial p} + \underbrace{\max \left( \frac{\partial \bar{\omega}}{\partial P}, 0 \right) \times (\bar{q}_v^{\text{Ref}} - \bar{q}_v)}_{\text{Inflow only}}$$

**Inflow only**

# WTG method

$$\bar{\omega} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial p} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau}$$

- $\tau = 3\text{hr}$
- Prescribed BL top=850 hPa
- Apply WTG from BL top to 100hPa
- $\bar{\omega}(p > 850 \text{ hPa}) =$  linear interpolation in pressure from  $\bar{\omega}(p = 850 \text{ hPa})$  to 0 at the surface

# DGW method

$$\frac{\partial}{\partial p} \left( \varepsilon \frac{\partial \bar{\omega}}{\partial p} \right) = \frac{k^2 R_d}{\bar{p}^{\text{Ref}}} (\bar{T}_v - \bar{T}_v^{\text{Ref}})$$

$\varepsilon(\text{constant}) = 1/\text{day}$  and  
 $k = 10^{-6}/\text{km}$

apply DGW from the surface to 100hPa

$$\bar{\omega}(100 \text{ hPa}) = \bar{\omega}(\text{surface}) = 0$$

no BL treatment

# Models that participate in this project

	Models	Contributor	Dimension	Horizontal size(km)	Horizontal res (km)
<b>Cloud-Resolving Models</b>	WRF	S. Wang	3D	190 × 190	2 × 2
	MesoNH	P. Peyrille	3D	150 × 150	3 × 3
	LaRC_CRM	A. Cheng	2D	256	4
	MNTCMv3	M. J. Herman	2D	200	1
	LEMv2.4	C. Daleu	2D	128	0.5
<b>Single-Column Models</b>	<b>LMDzA</b>	<b>G. Bellon</b>	-	-	-
	<b>LMDzB</b>	<b>G. Bellon</b>	-	-	-
	GISS_SCM	D. Kim	-	-	-
	APRv6	G. Bellon	-	-	-
	<b>UMv7.8</b>	<b>C. Daleu</b>	-	-	-
	<b>EC-Earthv1</b>	<b>P. Siebesma</b>	-	-	-
	<b>EC-Earthv3</b>	<b>P. Siebesma</b>	-	-	-

-Time independent SST

-Fixed radiative cooling through most of the free troposphere

# Q1: Can a large-scale circulation develop over uniform SST?

## WTG and DGW simulations over uniform SST

- The Ref state of each model is defined with profiles from the RCE simulation of that model.
- For each model, we performed WTG and DGW simulations with the SST of the Ref state.
- The WTG and DGW simulations are initialized with profiles from the corresponding Ref state.
- Note that RC is fixed throughout most of the troposphere

The reference state and the simulated column have **same characteristics** at time=0

# Q1: Can a large-scale circulation develop over uniform SST?

To evaluate the WTG and DGW simulations

We used  $\Omega = \frac{\int \bar{\omega} dp}{\int dp}$  and the ratio  $\mathbf{P}/\mathbf{P}_{Ref}$

$\mathbf{P}$ : mean precipitation in the simulated column

$\mathbf{P}_{Ref}$ : mean precipitation of the Ref state.

A simulation reproduces the RCE conditions to a good approximation if:

$$\mathbf{0.9} < \mathbf{P}/\mathbf{P}_{Ref} < \mathbf{1.1} \text{ and } -\mathbf{0.4} \times \mathbf{10}^{-\mathbf{2}} < \Omega \left( \frac{\mathbf{Pa}}{\mathbf{s}} \right) < \mathbf{0.4} \times \mathbf{10}^{-\mathbf{2}}$$

The large-scale circulation is significant if:

$$\text{large-scale ascent: } \Omega \left( \frac{\mathbf{Pa}}{\mathbf{s}} \right) > \mathbf{0.4} \times \mathbf{10}^{-\mathbf{2}} \text{ and } \mathbf{P}/\mathbf{P}_{Ref} > \mathbf{1.1}$$

$$\text{large-scale descent: } \Omega \left( \frac{\mathbf{Pa}}{\mathbf{s}} \right) < -\mathbf{0.4} \times \mathbf{10}^{-\mathbf{2}} \text{ and } \mathbf{P}/\mathbf{P}_{Ref} < \mathbf{0.9}$$

Uniform SST (K)= **298, 300, 302**

WTG and DGW simulations which produce  **$0.9 < P/P_{Ref} < 1.1$**  and  **$|\Omega| < 0.4 \times 10^{-2} \text{ Pa/s}$**

Under both WTG and DGW, regardless of the SST:

● WRF and ◁ LMDzA

Under WTG/DGW,

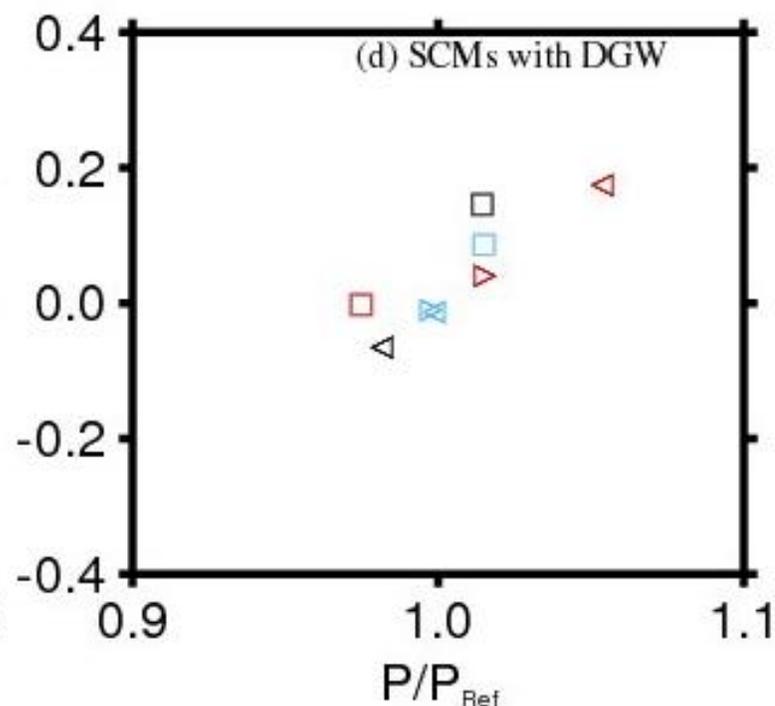
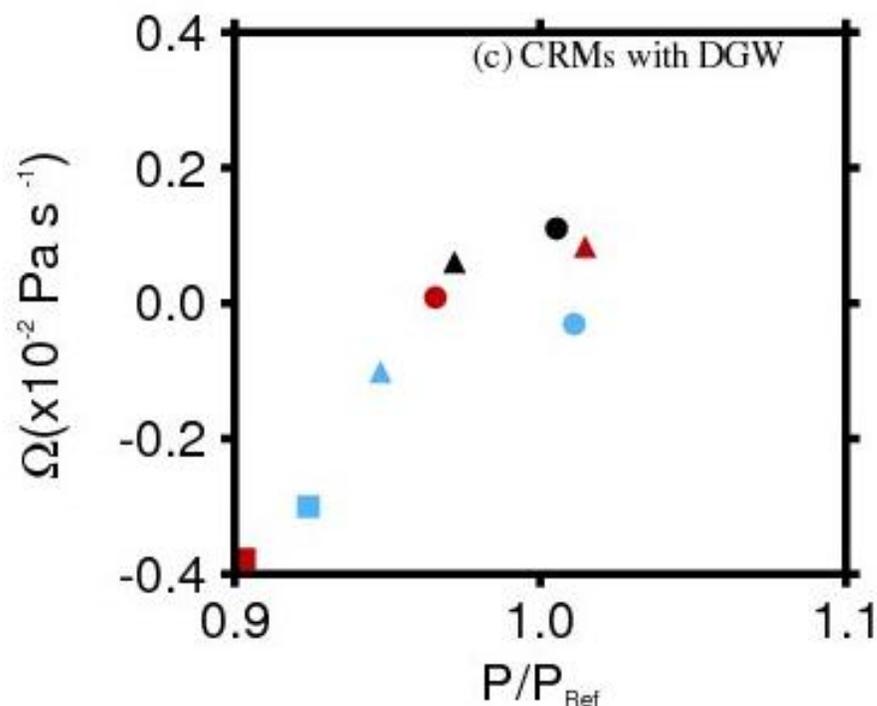
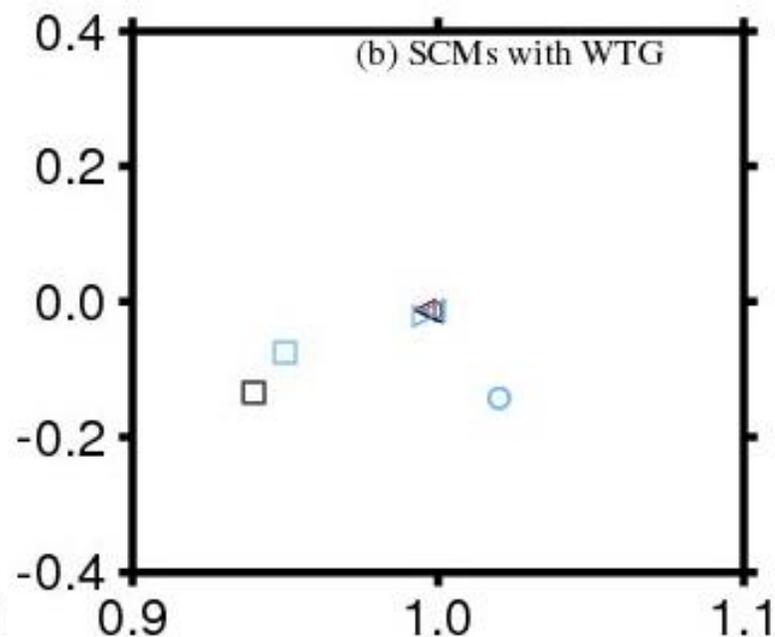
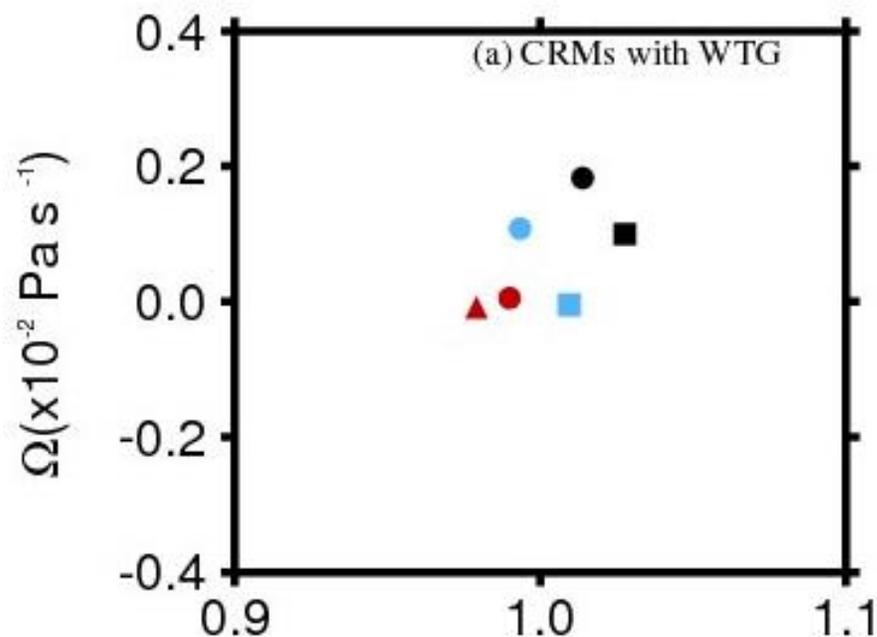
for some SSTs only:

▲ MesoNH, ■ NMTCMv3

▷ LMDzB, ○ GISS-SCM and

□ EC-Earthv3

Not for model like ☆ UMv7.8



**Q1:** Can a large-scale circulation develop over uniform SST? **YES**

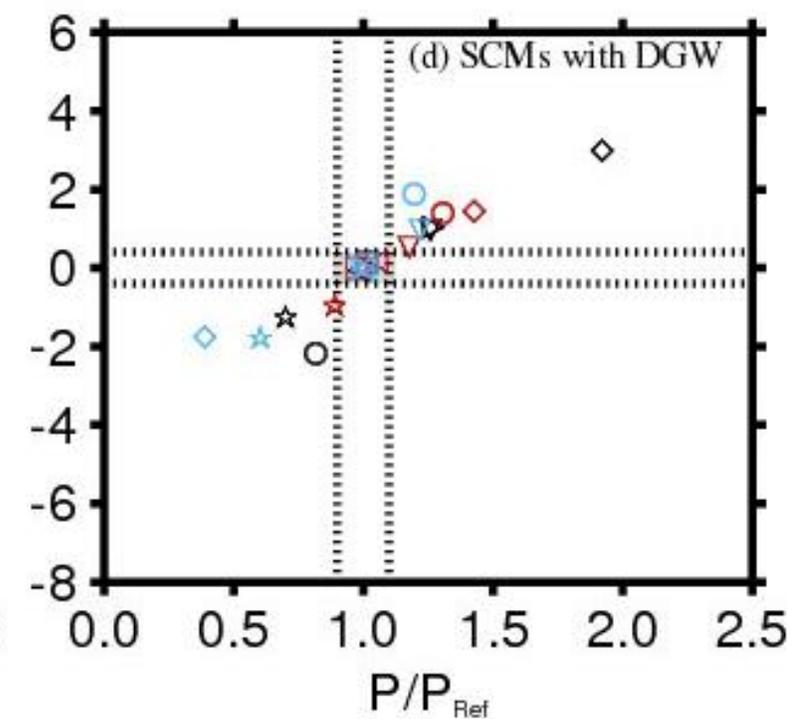
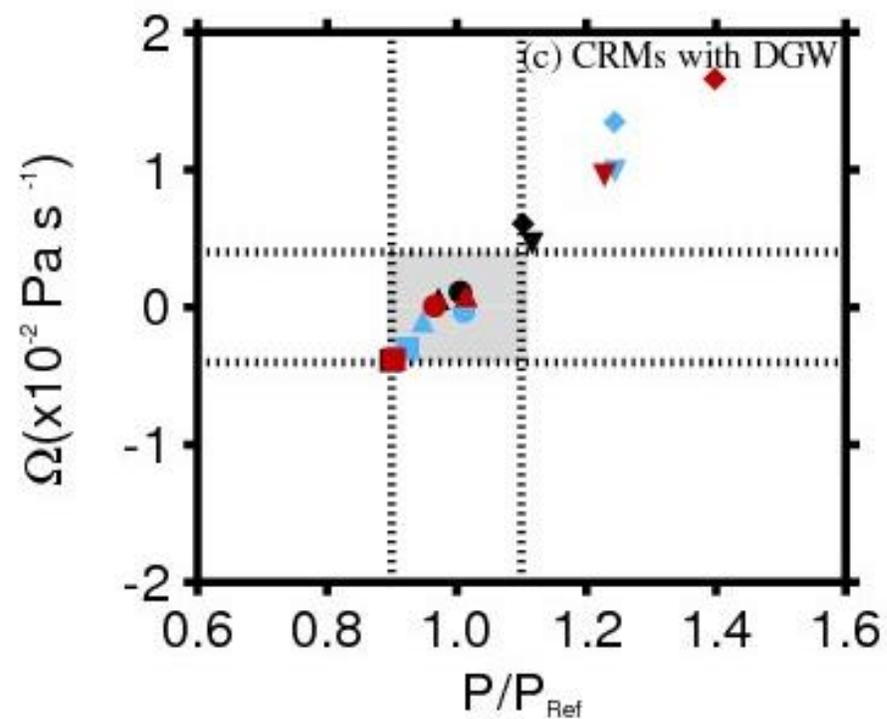
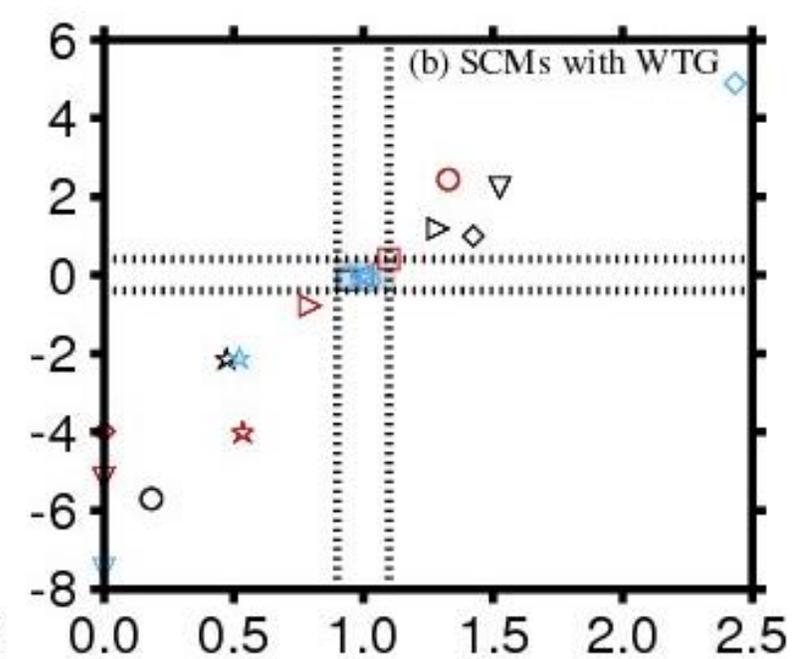
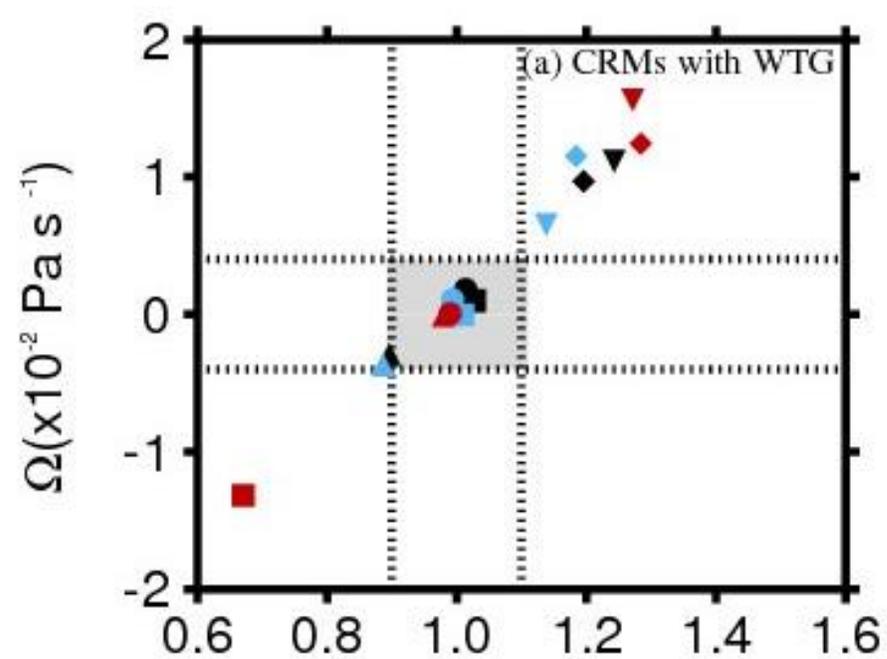
SSTs of **298, 300, 302 K**

### Symbol definitions

- |            |              |
|------------|--------------|
| ● WRF      | ◁ LMDzA      |
| ▲ MesoNH   | ▷ LMDzB      |
| ◆ LaRC_CRM | ○ GISS_SCM   |
| ■ NMTCMv3  | ▽ ARPe6      |
| ▼ LEMv2.4  | ★ UMv7.8     |
|            | ◇ EC-Earthv1 |
|            | □ EC-Earthv3 |

CRMs show a **fairly linear relationship between  $P$  and  $\Omega$ .**

SCMs show deviations from this relationship

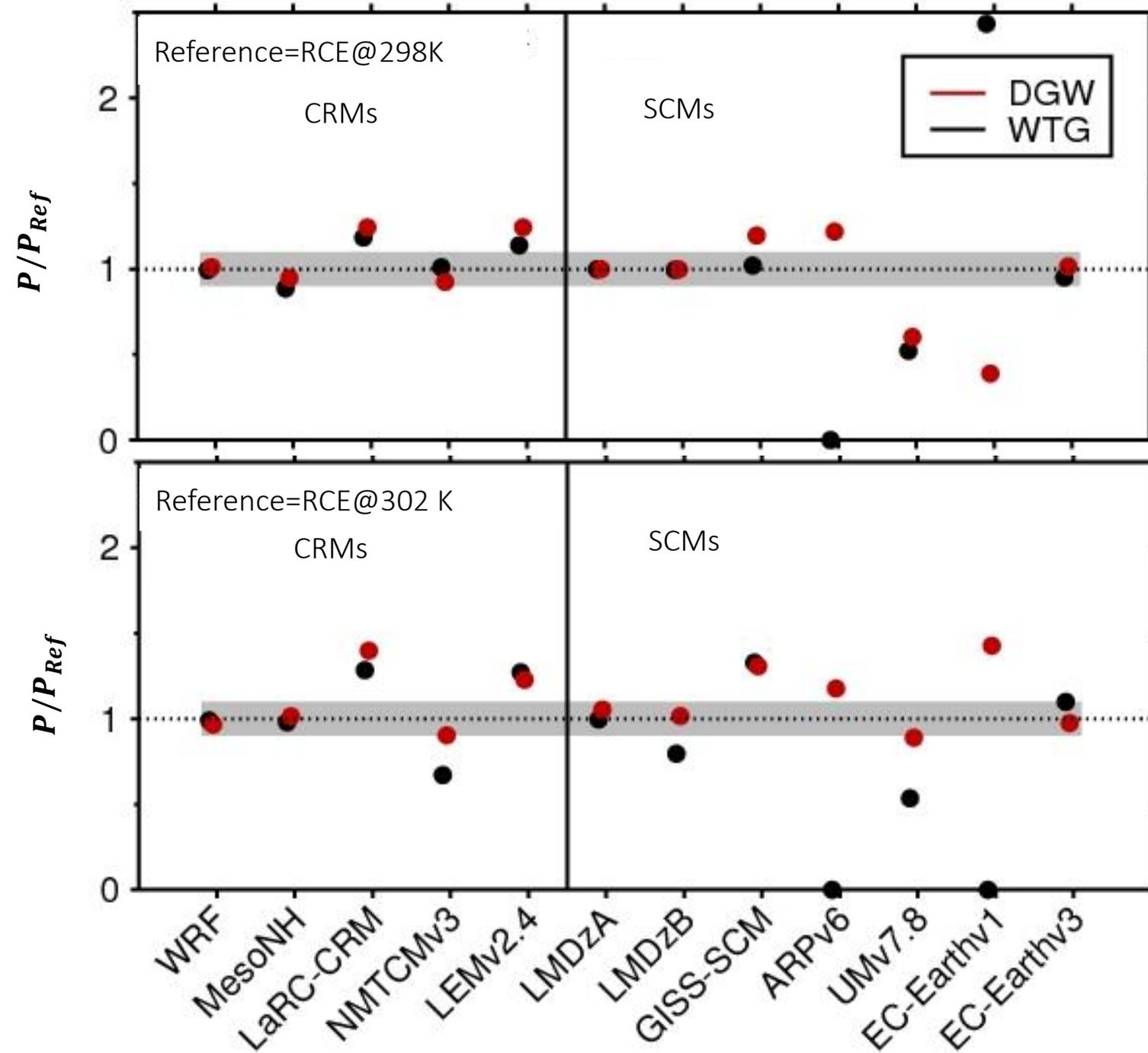


**Q1:** Can a large-scale circ develop over uniform SST? **YES**

Grey areas indicates  $0.9 < P/P_{Ref} < 1.1$

SCMs display a much wider ranges of behaviour

- Some SCMs under the WTG can produce  $P=0$  mm/day (e.g. ARPv6) within an individual SCM, a
- WTG sim and a corresponding DGW sim can produce different signs of the circulation (e.g., EC-Earthv1)

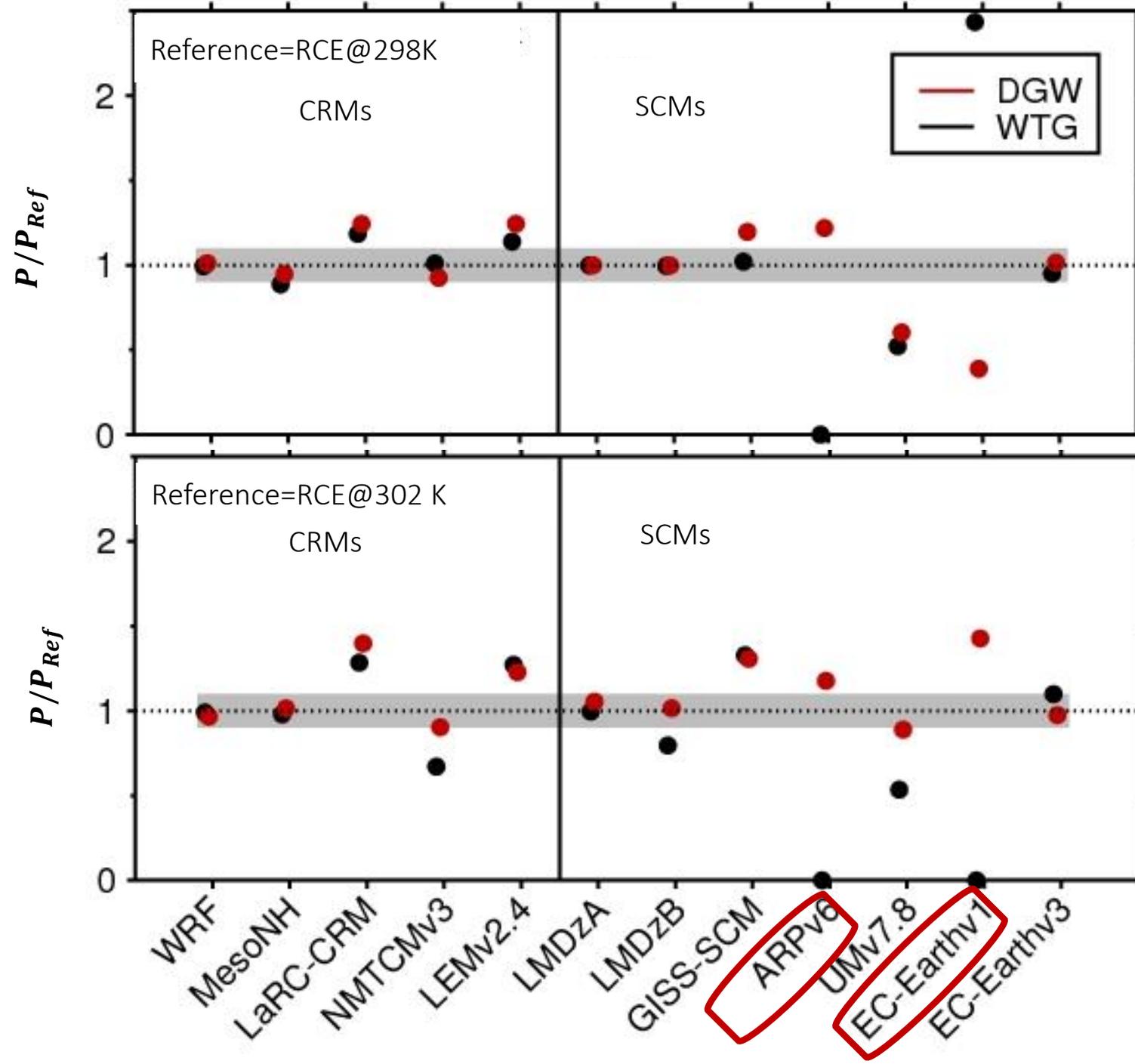


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- Some SCMs under the WTG can produce **P=0 mm/day** (e.g. ARPV6)
- within an individual SCM, a WTG sim and a corresponding DGW sim can produce different signs of the circulation (e.g., EC-Earthv1)

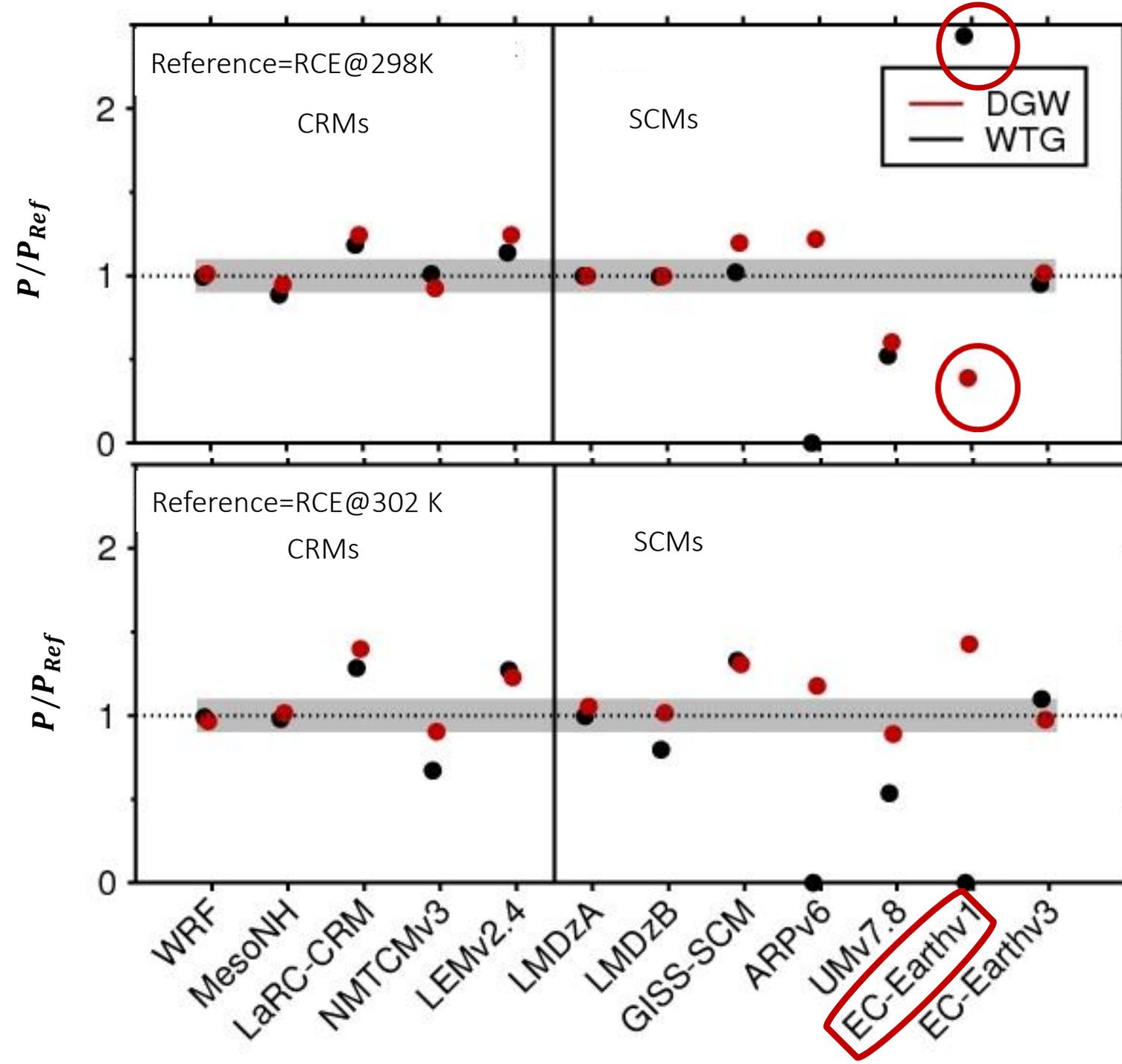


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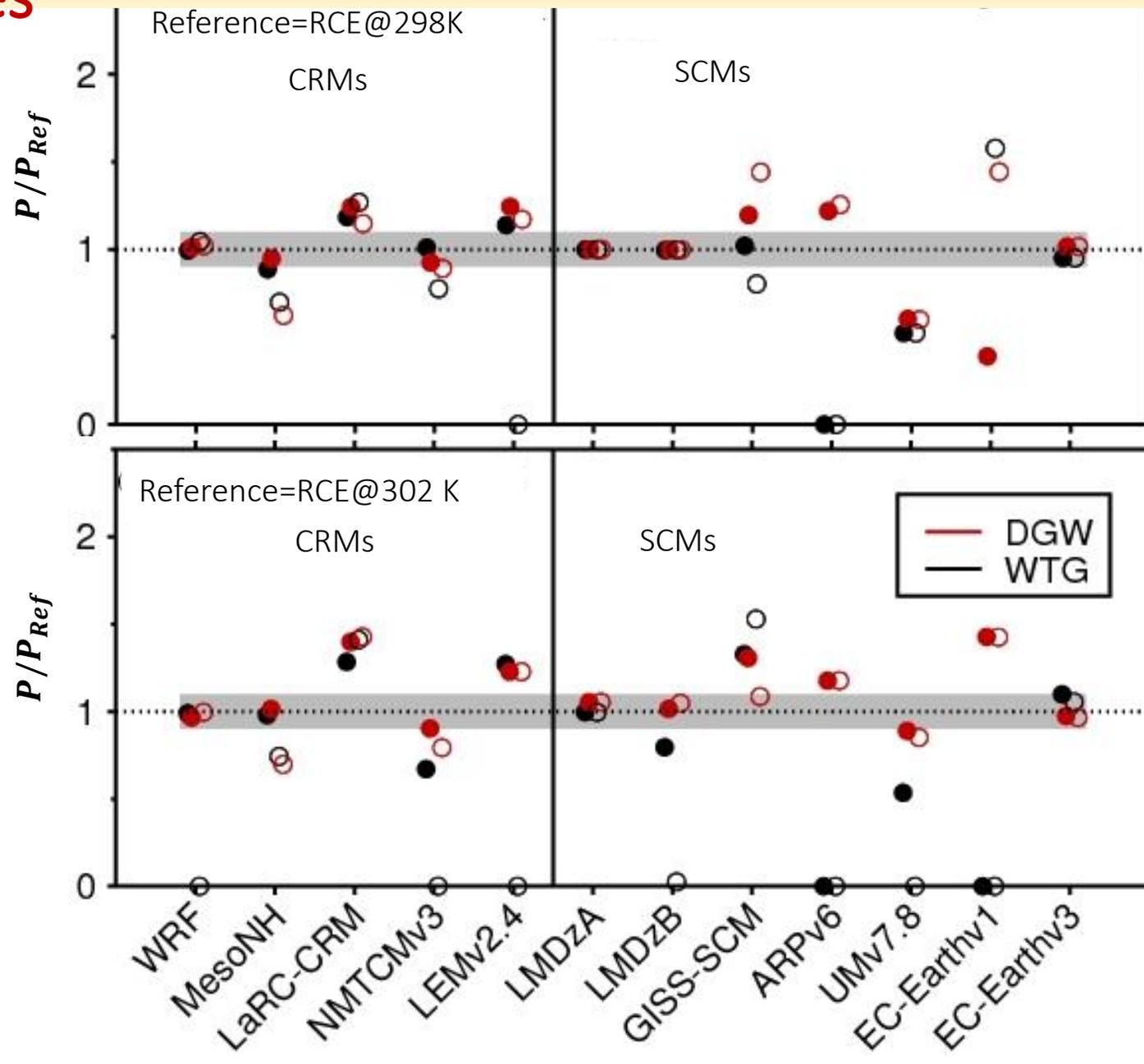
- Some SCMs under the WTG can produce  $P=0$  mm/day (e.g. AR Pv6)
- within an individual SCM, a WTG sim and a corresponding DGW sim can produce **different signs of the circulation** (e.g., EC-Earthv1)



**Q2:** Can given SST and  $T$  profile support both a rainy and dry state, depending on initial moisture? **Yes**

Sensitivity to the initial moisture conditions

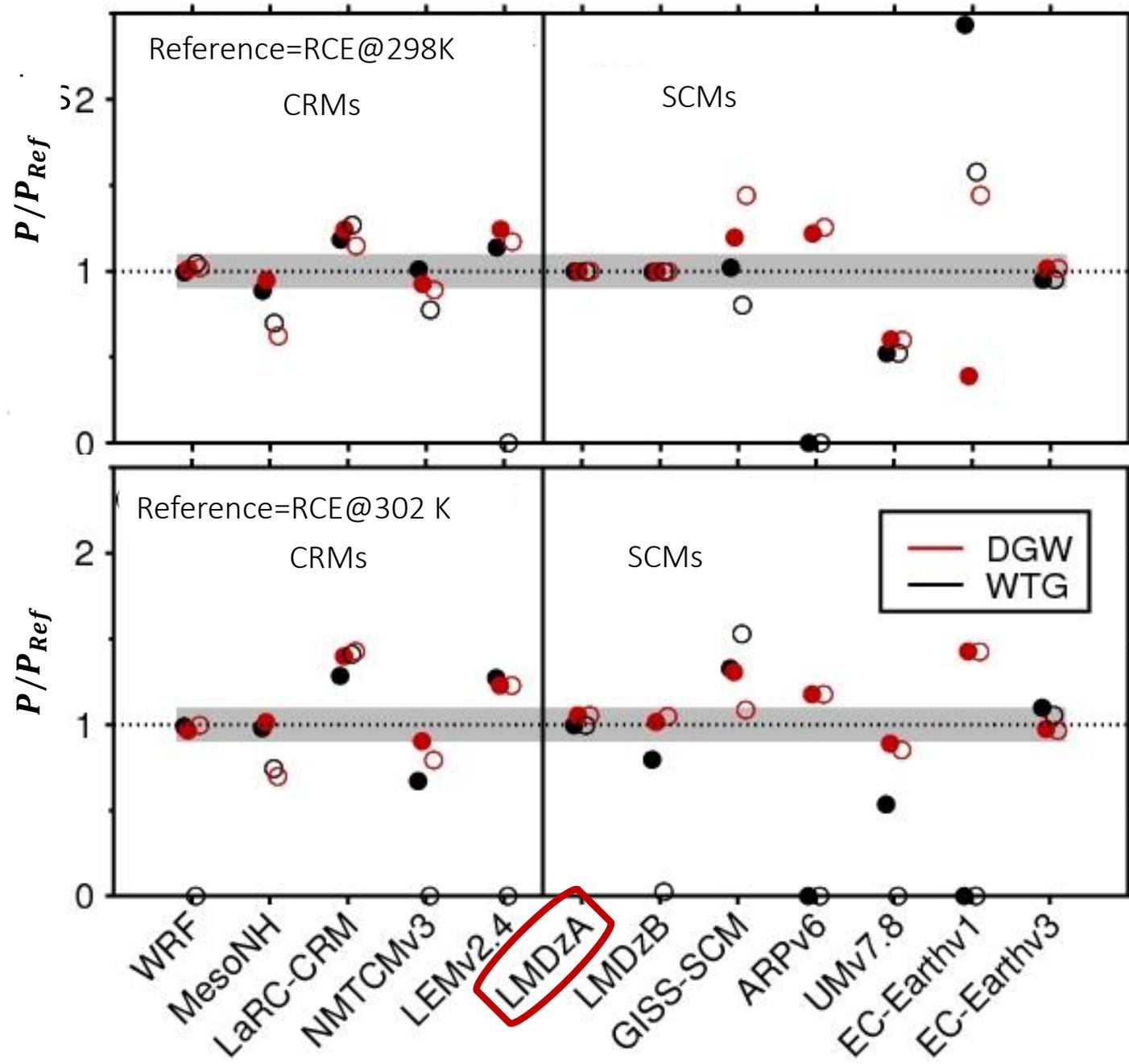
- Initialized with RH of the RCE state (full circles)
- Initialized with 0% RH (open circles)



# Can given SST and $T$ profile support both a rainy and dry state, depending on initial moisture? **Yes**

- Initialized with RH of the RCE state (full circles)
- Initialized with 0% RH (open circles)

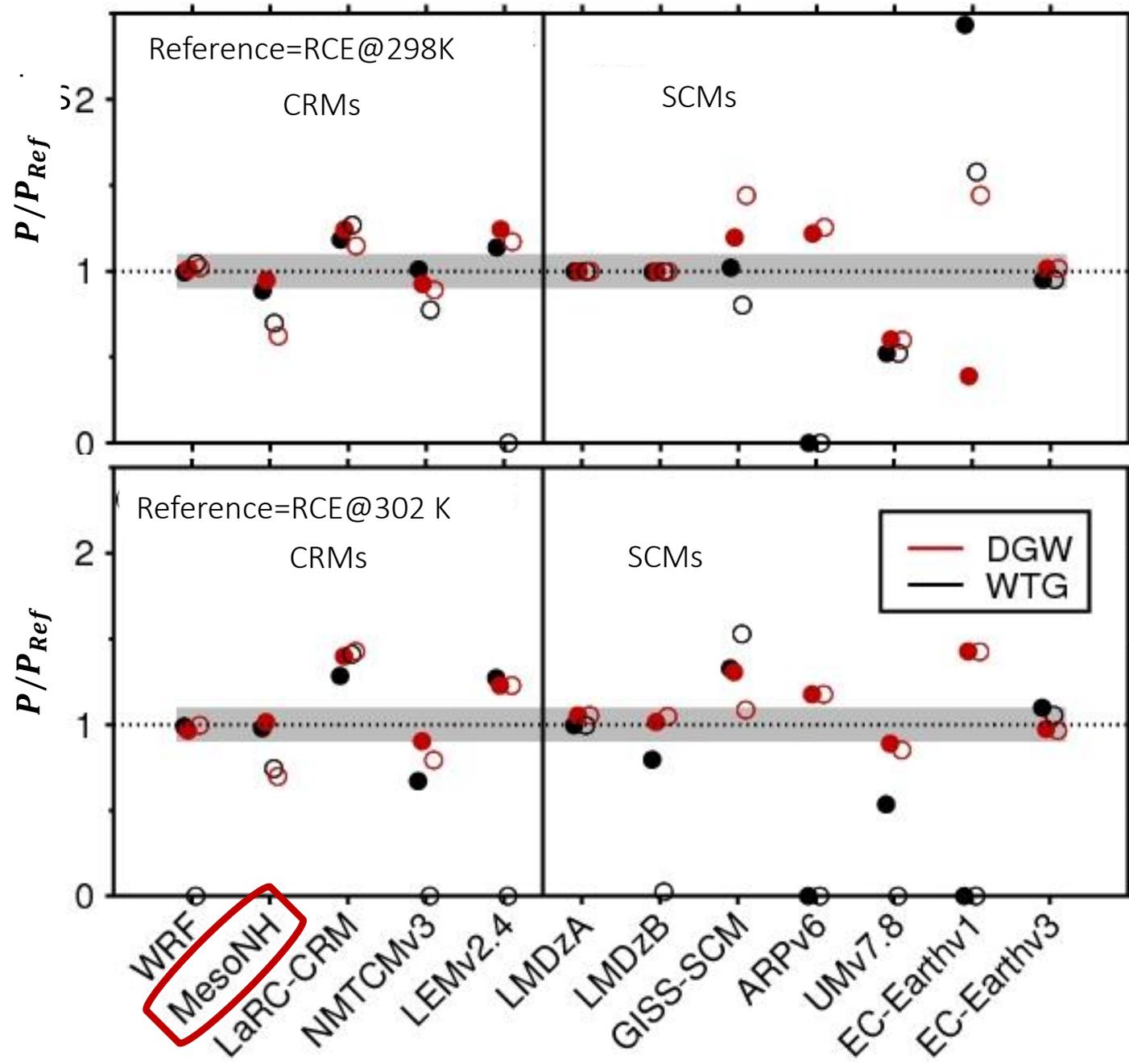
- 1-Some models are **not sensitive** to the initial RH
- 2-Some models can sustain two distinct precipitating equilibrium states (MesoNH).
- 3-Some models produce enhanced precip from the initially dry moisture
- 4-DWG simulations always produce precipitating equilibrium states.
- 5-In contrast to the DGW, some models under the WTG can sustain a state with zero precip or a state with persistent, precipitating convection depending of the initial RH. Here after called multiple equilibria (ME).
- 6-ME is more likely at higher SST.



# Can given SST and $T$ profile support both a rainy and dry state, depending on initial moisture? **Yes**

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- Initialized with 0% RH (open circles)

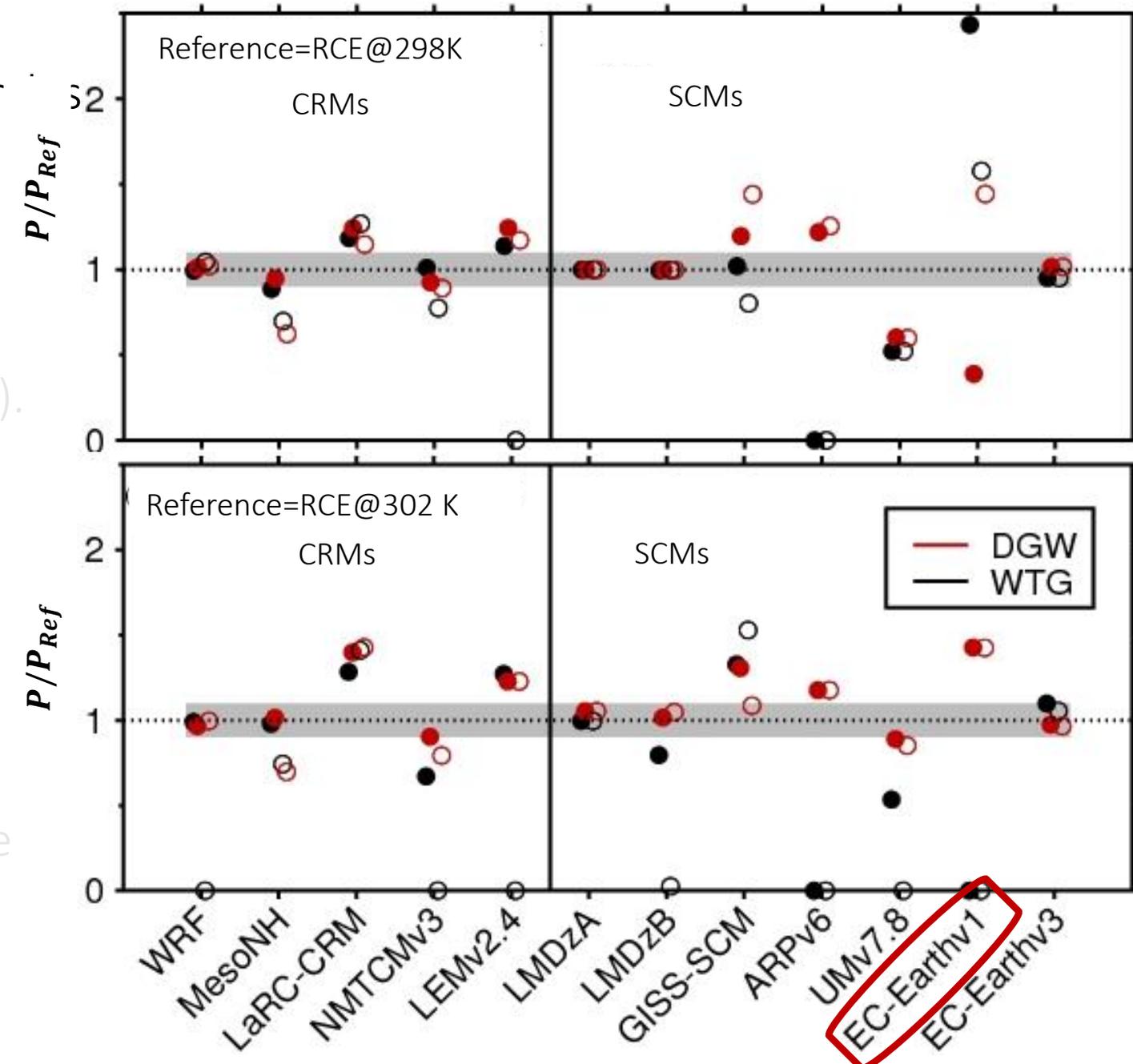
- 1-Some models are not sensitive to the initial RH
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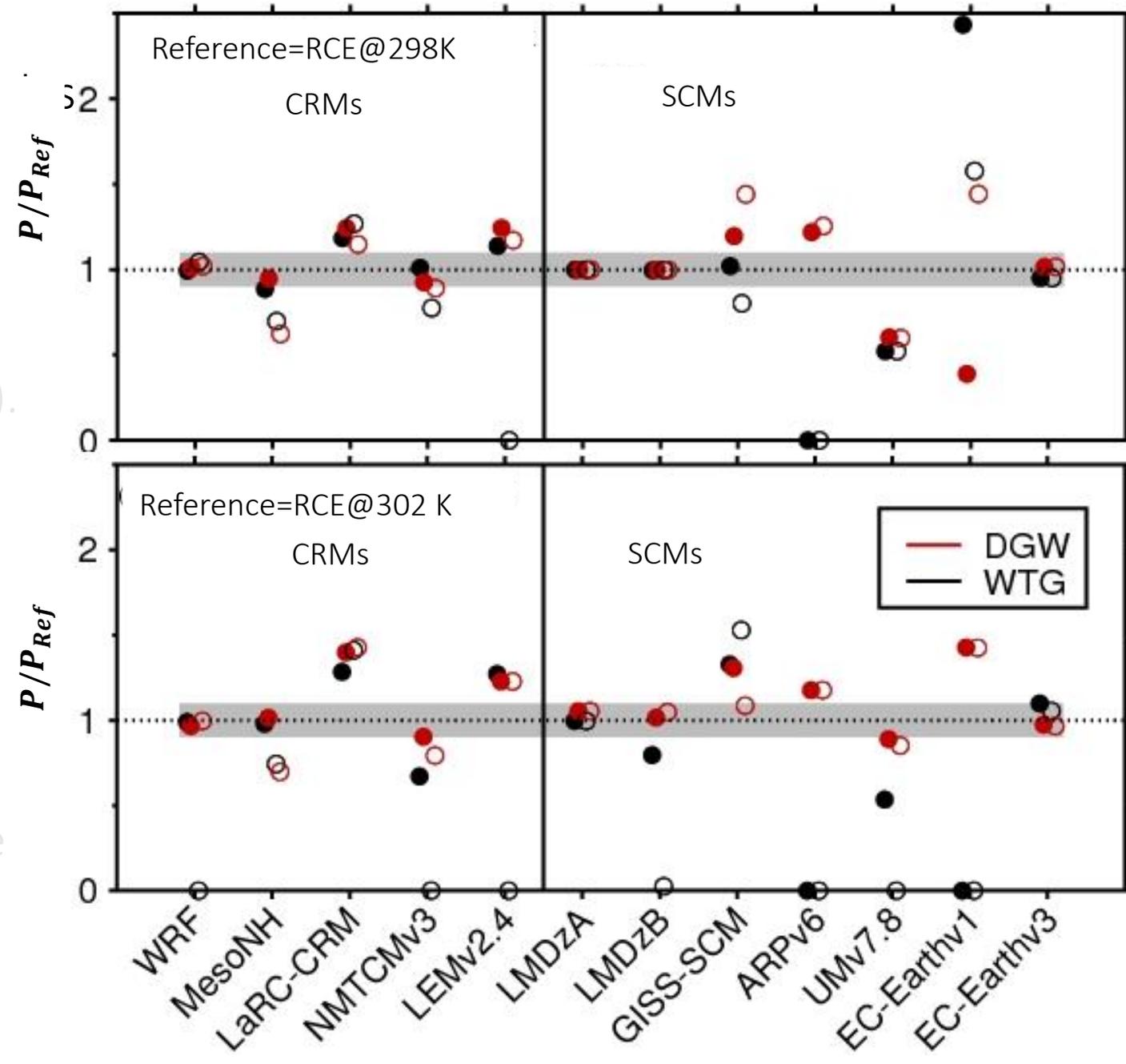
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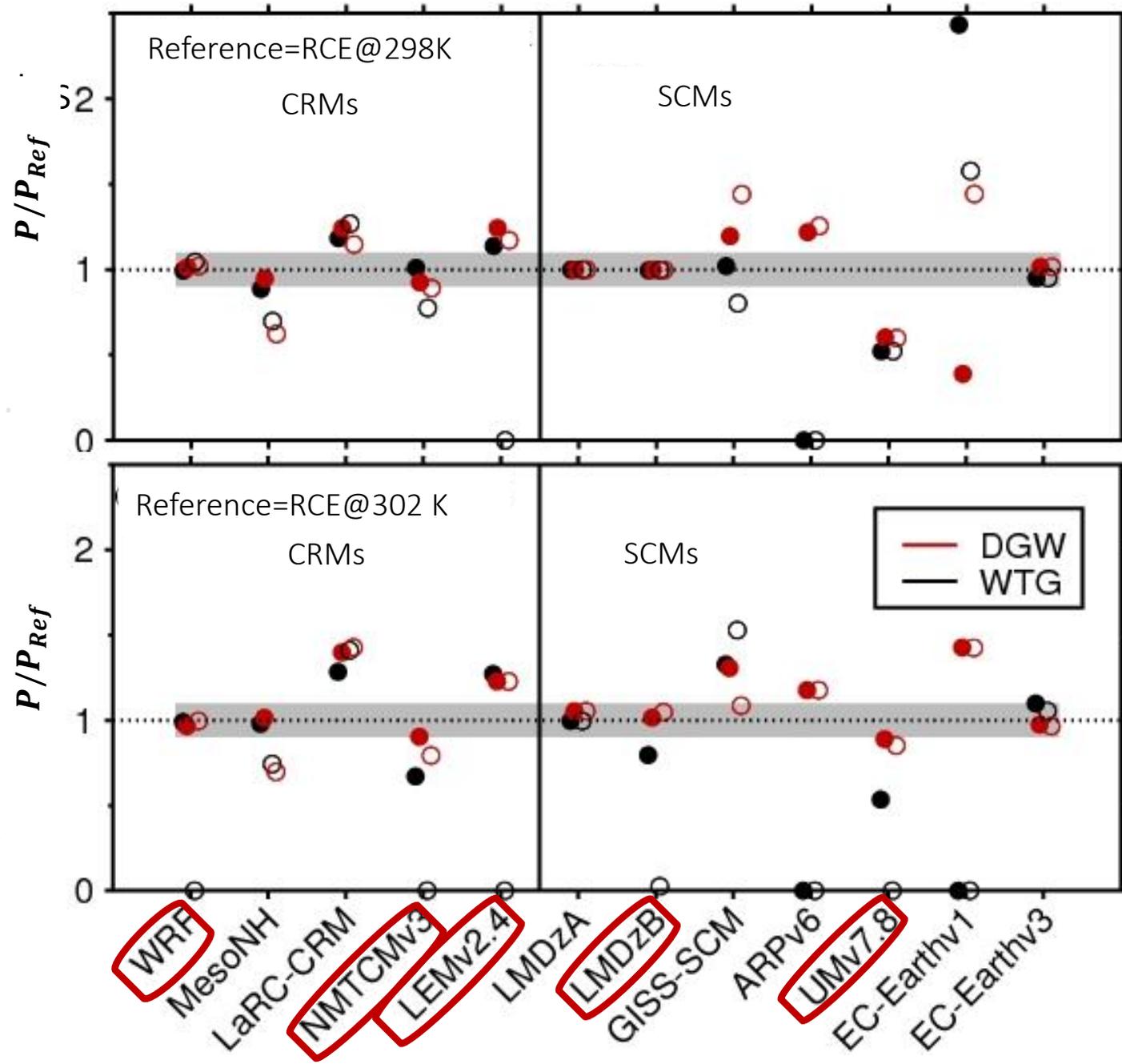


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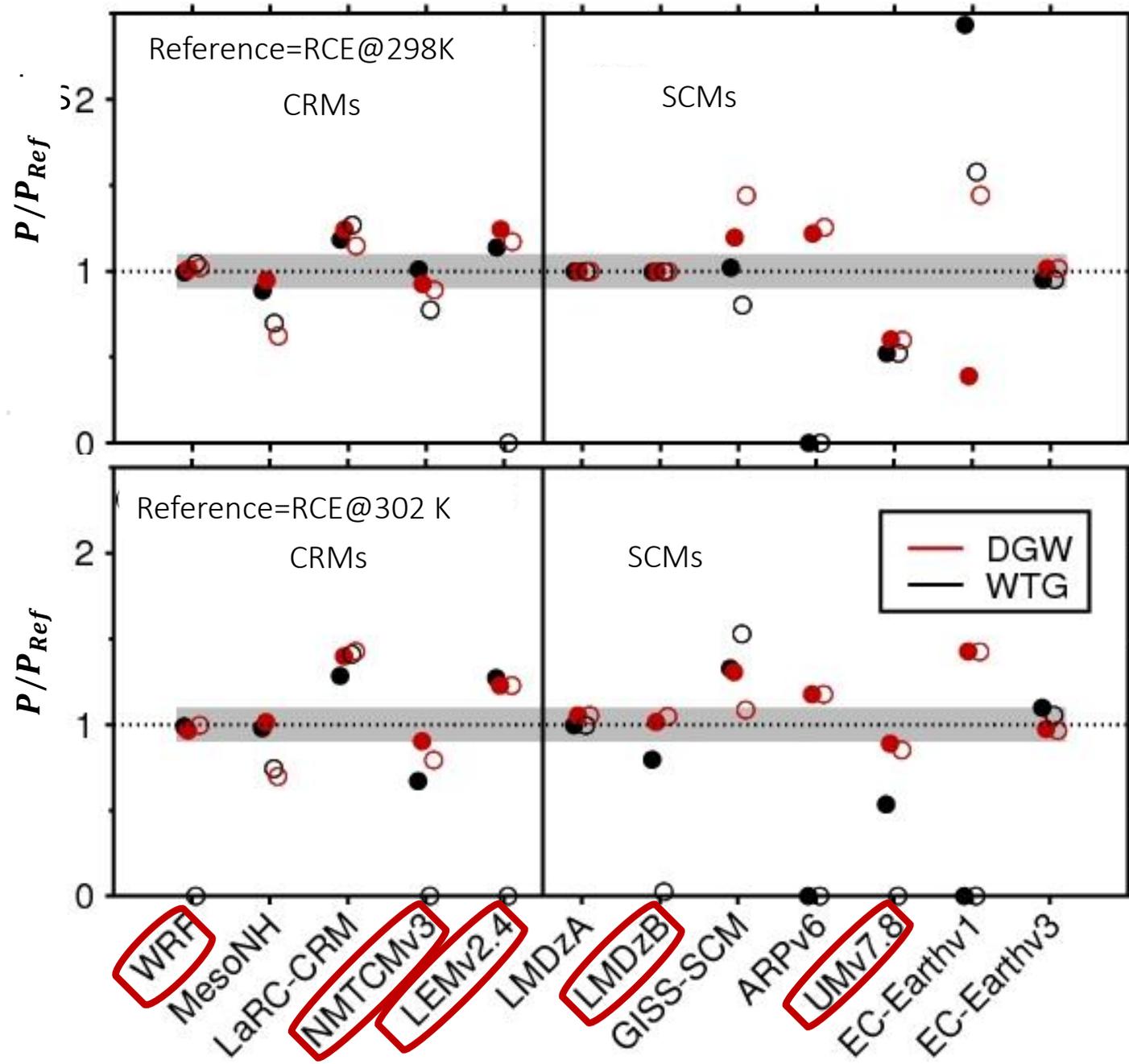


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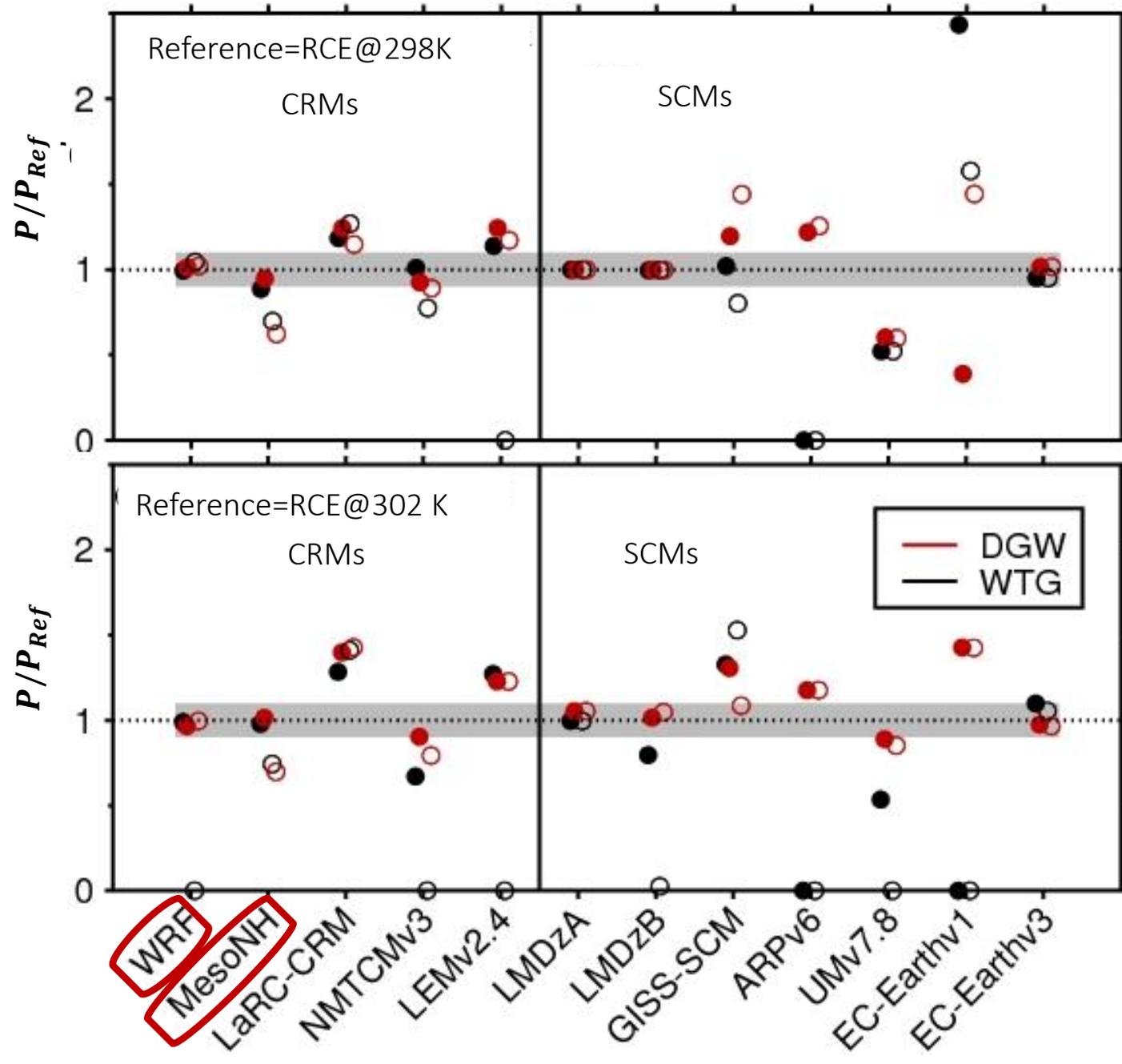


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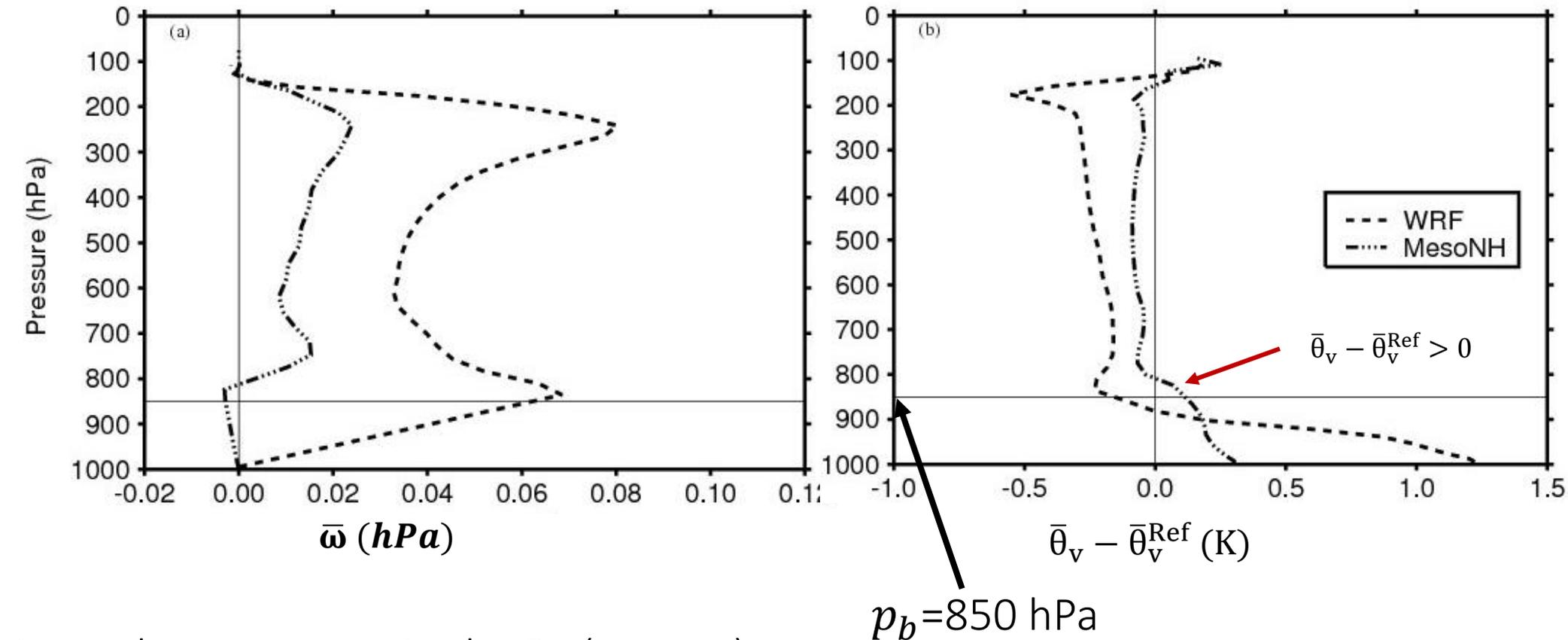
Under the WTG, some models sustain ME, while other models do not

**why ?**



# Sensitivity to initial moisture conditions

Over a uniform SST=302 K, we compared the initially dry WTG simulations of WRF and MesoNH



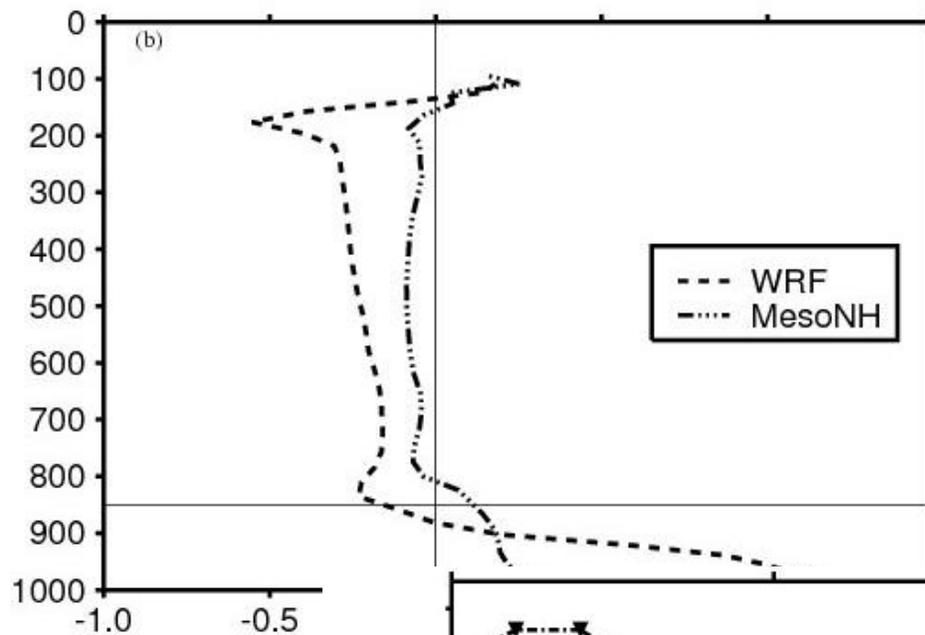
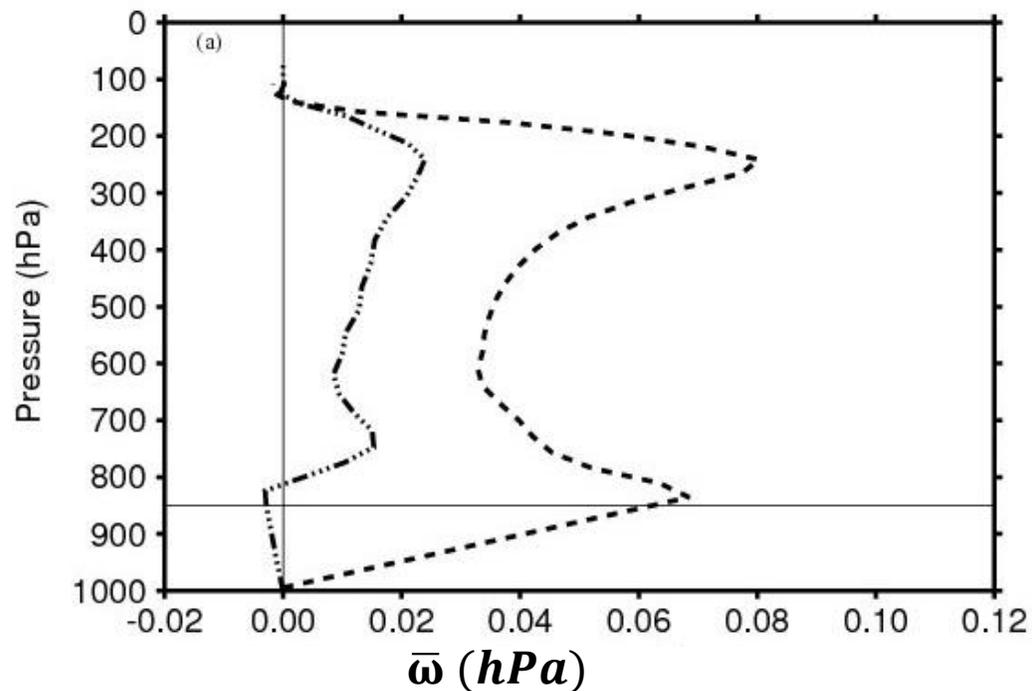
Note the treatment in the BL ( $p > p_b$ ):

The sign of  $\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}$  at the 1<sup>st</sup> model level above  $p_b$  determines the sign of  $\bar{\omega}$  in the BL.

A large-scale ascent is produced by MesoNH, consistent with  $\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}} > 0$

A large-scale descent is produced by WRF whilst  $\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}} > 0$

# ME and sensitivity to the PBL depth

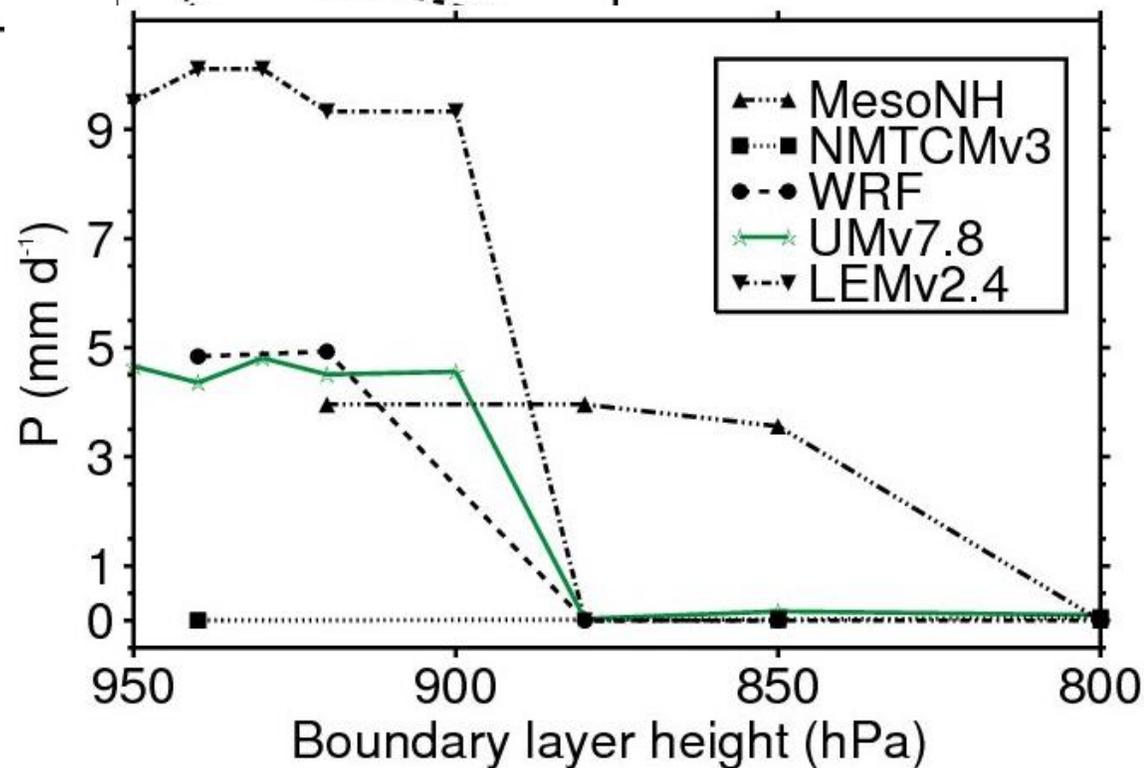


Uniform SST=302K and initial RH=0%  
 $p_0=800, 850, 900, 920, 930, 940$  and 950 hPa

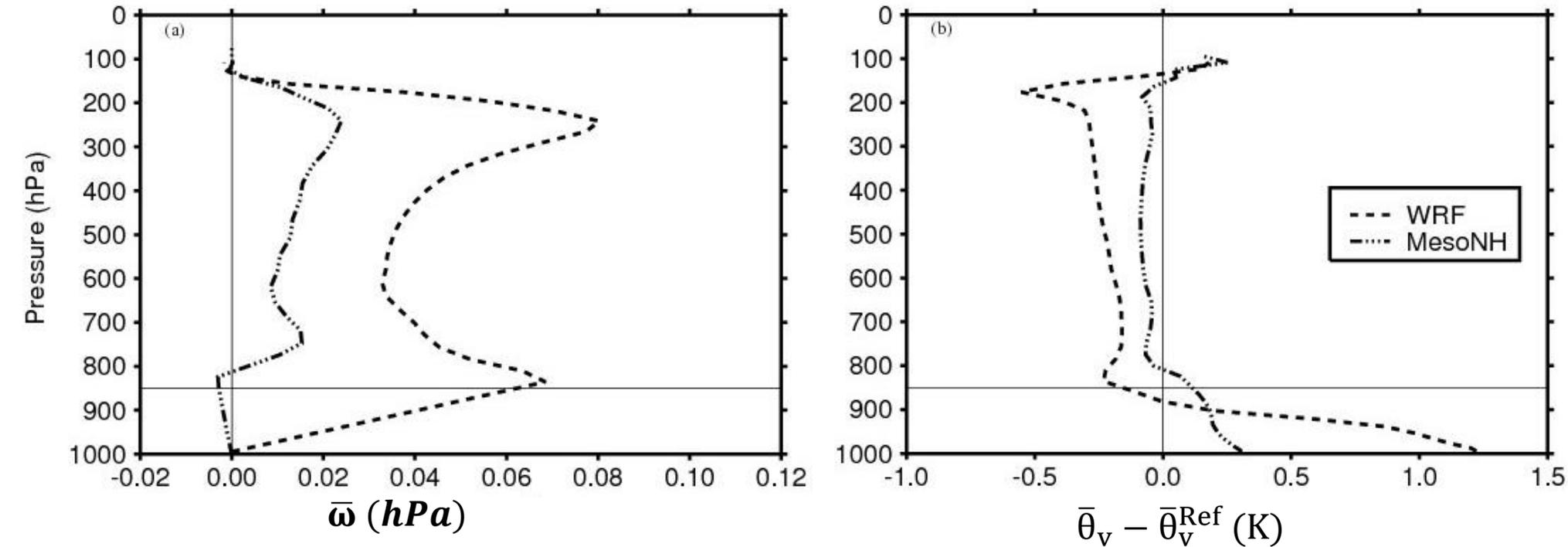
MesoNH with  $p_0=800$ hPa produces  $P=0$  mm/d

A shallower BL can result in  $P \neq 0$  (except NMTCMv3)

ME are also sensitive to other WTG parameters



# ME and sensitivity to the PBL depth



Uniform SST=302K and initial RH=0% and BL top=850 hPa

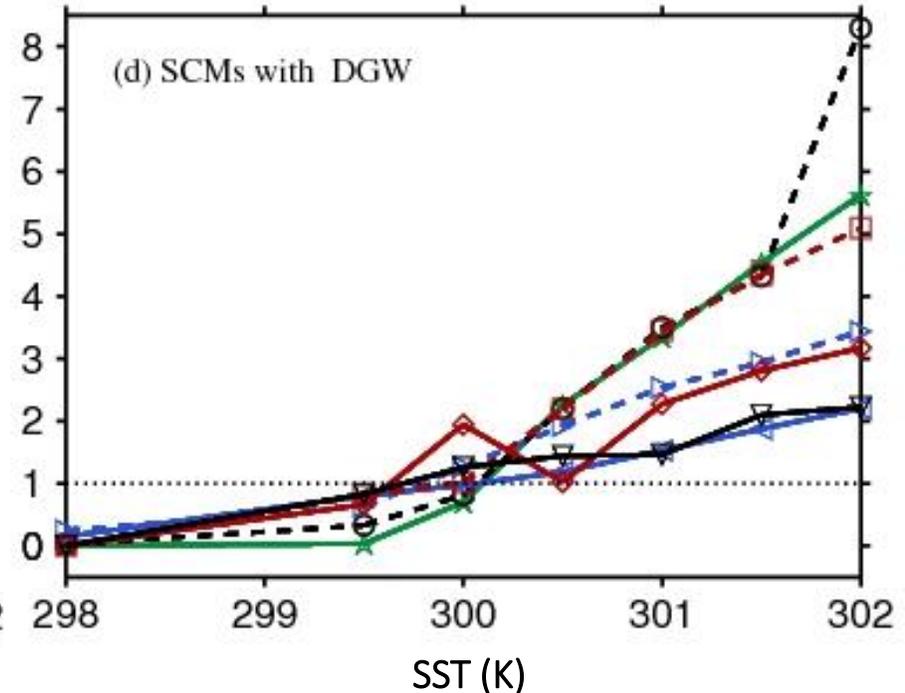
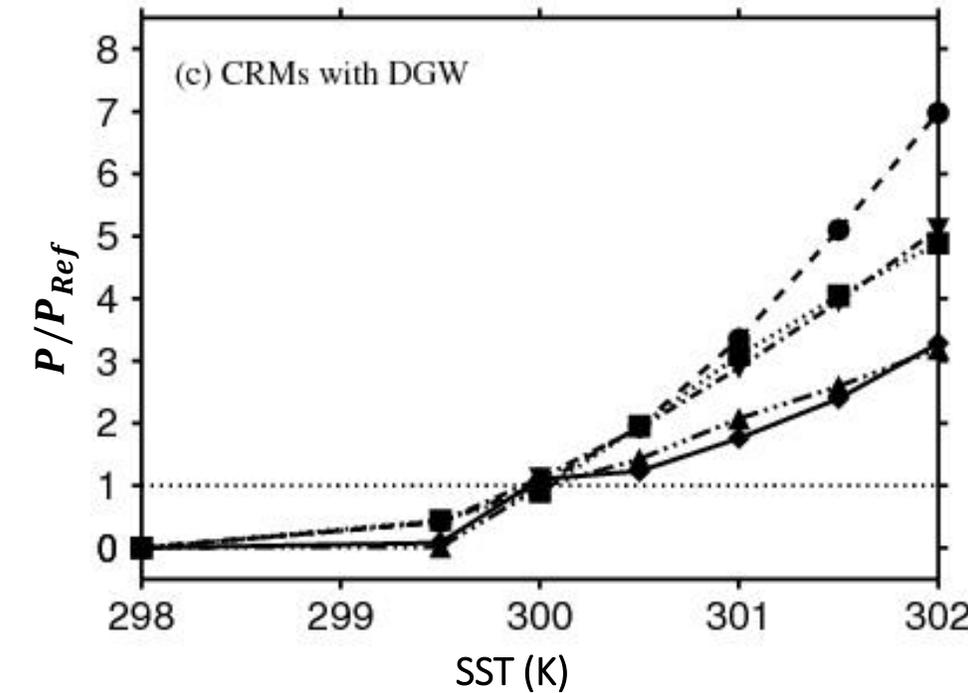
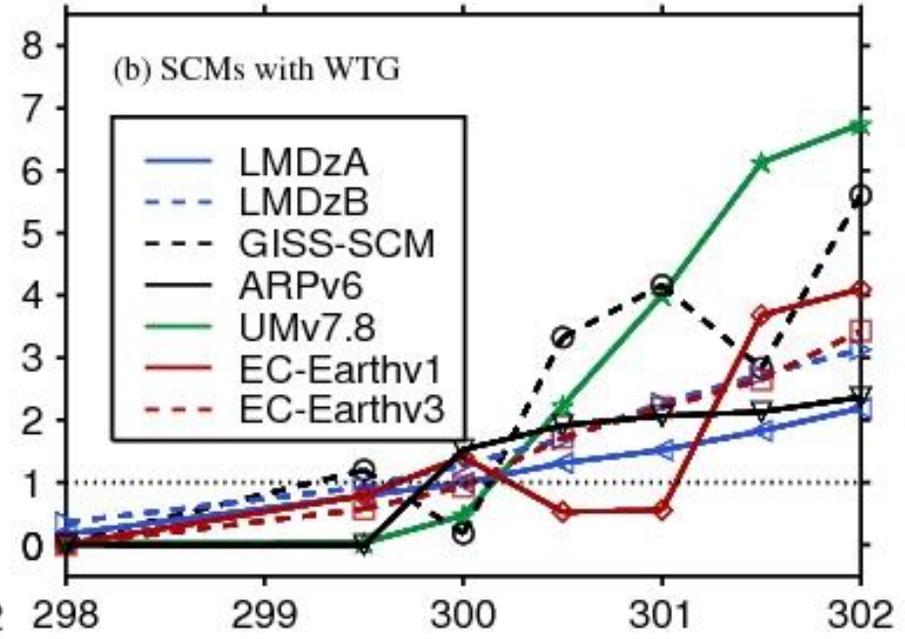
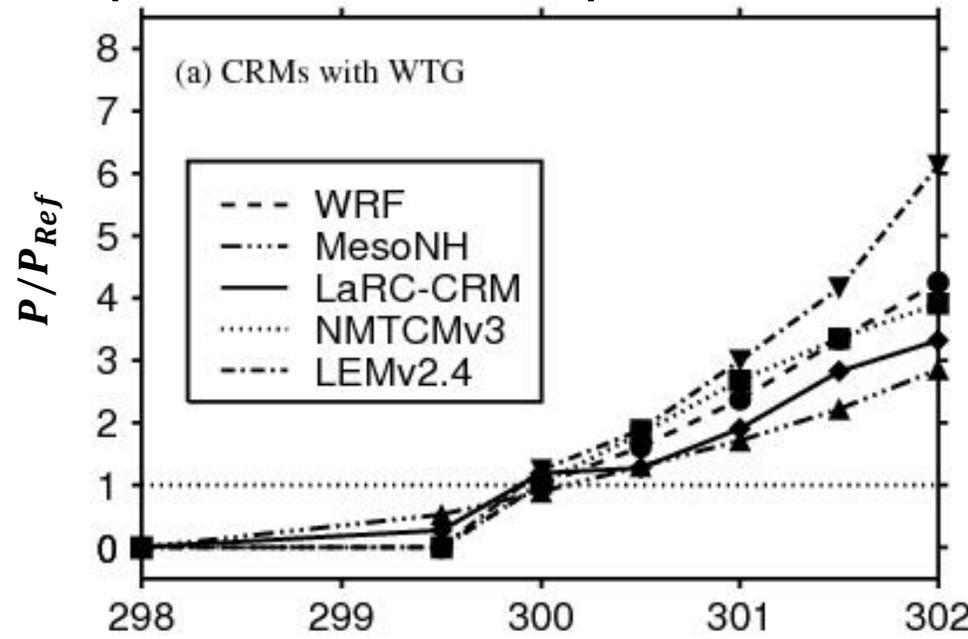
- A shallower BL can result in  $P \neq 0$  (except NMTCMv3)
- $\bar{\mathbf{W}} \frac{\partial \bar{\theta}_v^{\text{Ref}}}{\partial z} = \frac{\bar{\theta}_v - \bar{\theta}_v^{\text{Ref}}}{\tau} f(z)$ ,  $f(z) = \sin(\pi z/H)$  can result in  $P \neq 0$  (LEMv2.4, UMv7.8)
- A longer WTG adjustment time scale ( $\tau$ ) can result in  $P \neq 0$  (LEMv2.4, UMv7.8 and LMDzB)

ME is very sensitive to the details of the implementation of the WTG method

# How sensitive is a model (under the WTG/DGW method) to changes in the SST?

Ref state= RCE at 300K.

SSTs=298, 299.5, 300, 300.5, 301, 301.5, and 302 K



# How sensitive is a model (under the WTG/DGW method) to changes in the SST?

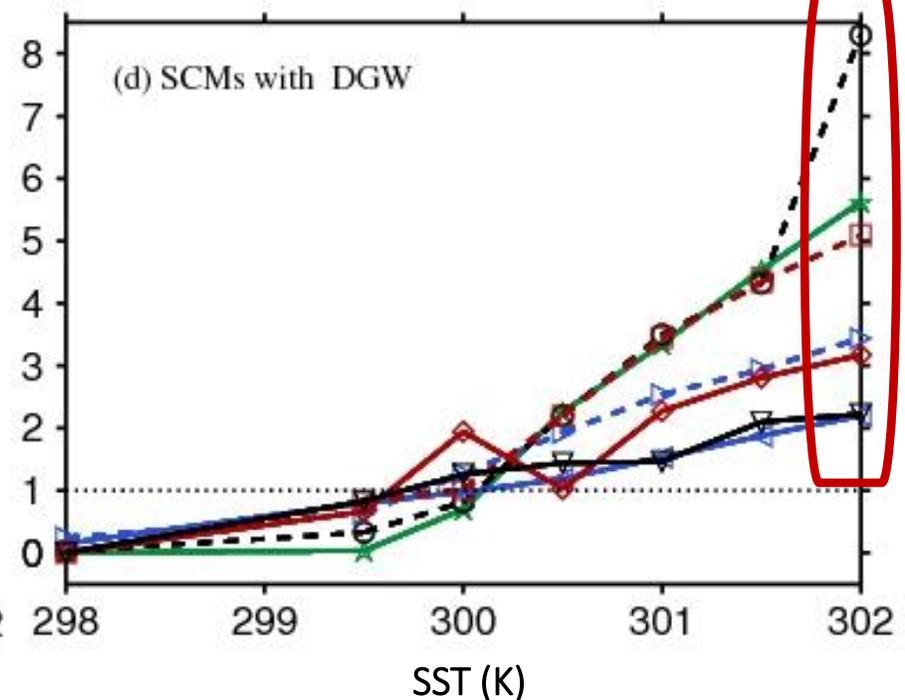
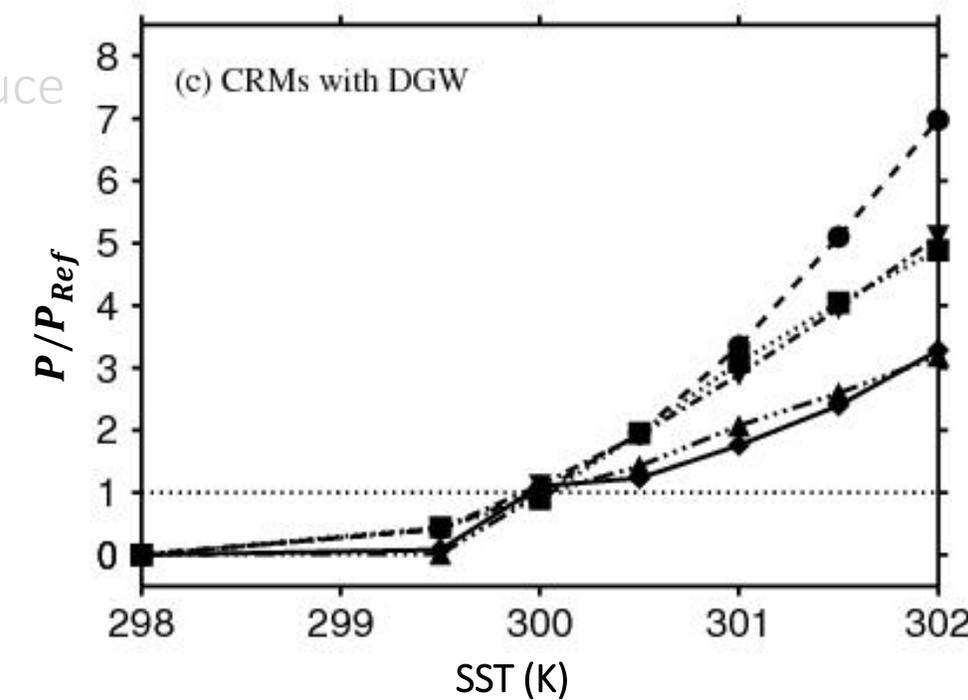
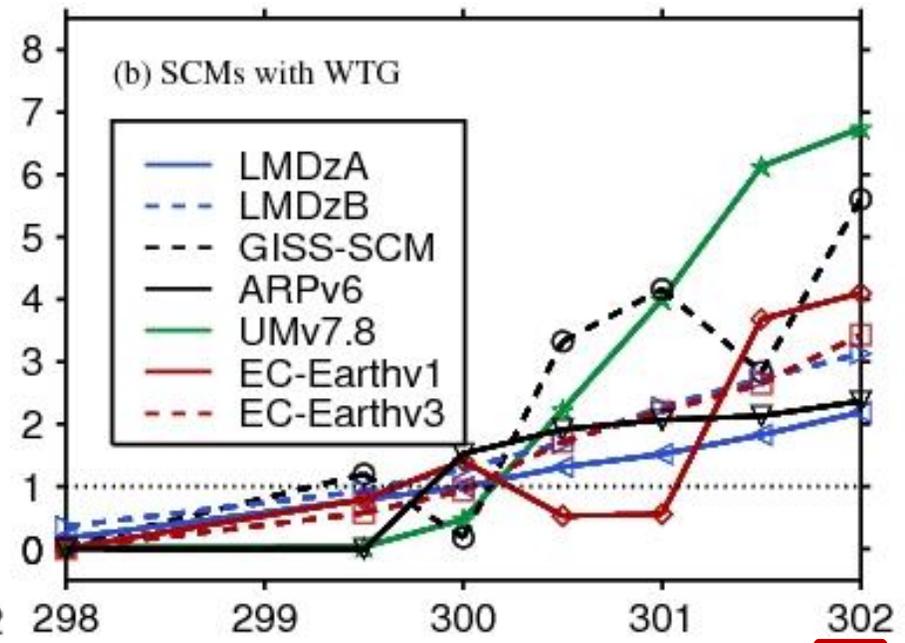
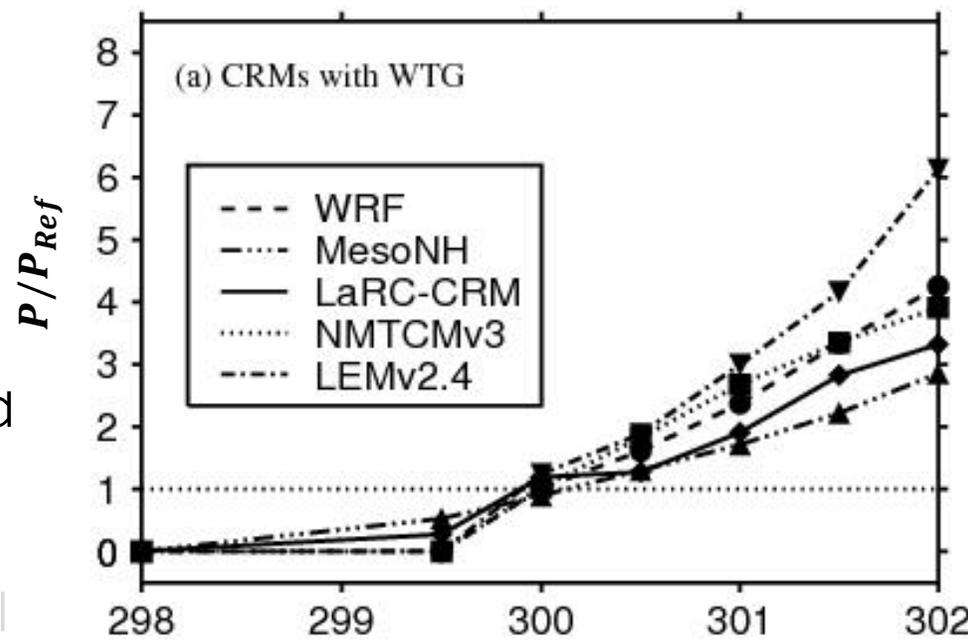
Ref state= RCE at 300K.  
Various SSTs

1-Under the same large-scale parameterization method models produce different solutions

2-within an individual model a WTG and corresponding DGW simulations can produce different solutions (e.g., EC-Earthv1)

3-for all CRMs, P increase Non-linearly with SST

4-SCMs shows sensitivity Of P to the SST which is not is not always monotonic (e.g.,, GISS-SCM).



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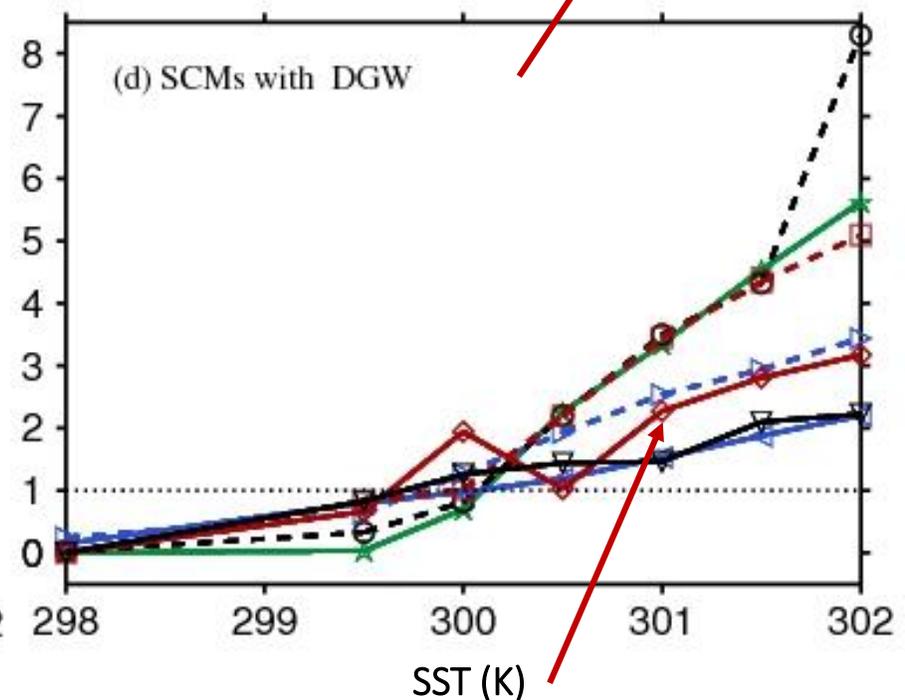
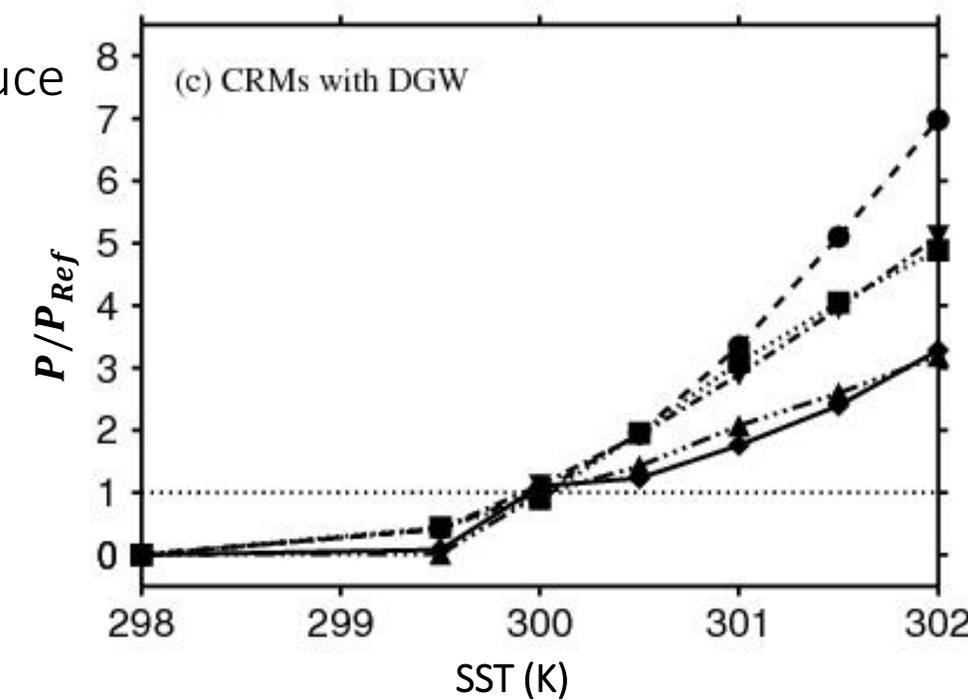
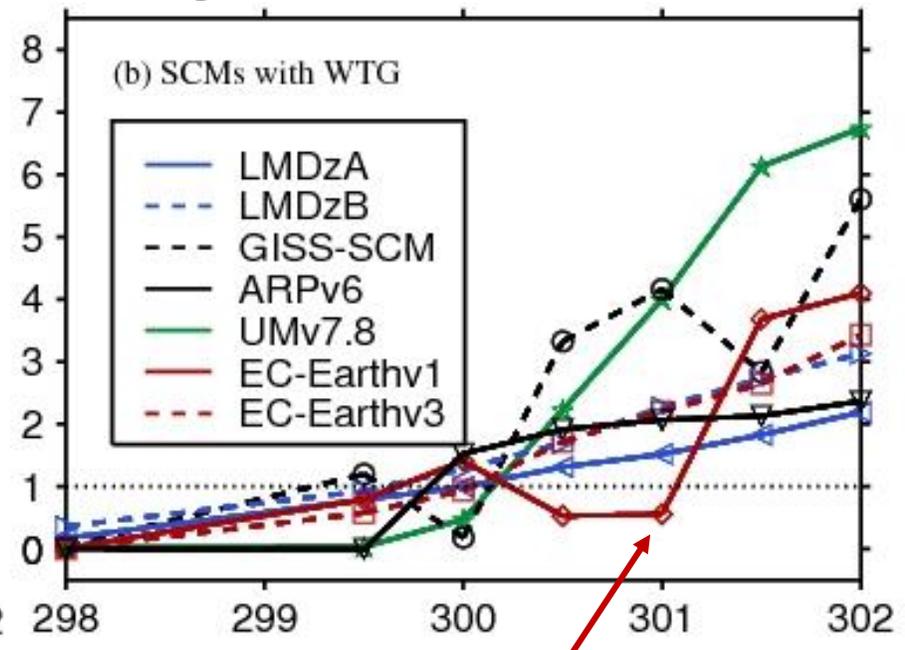
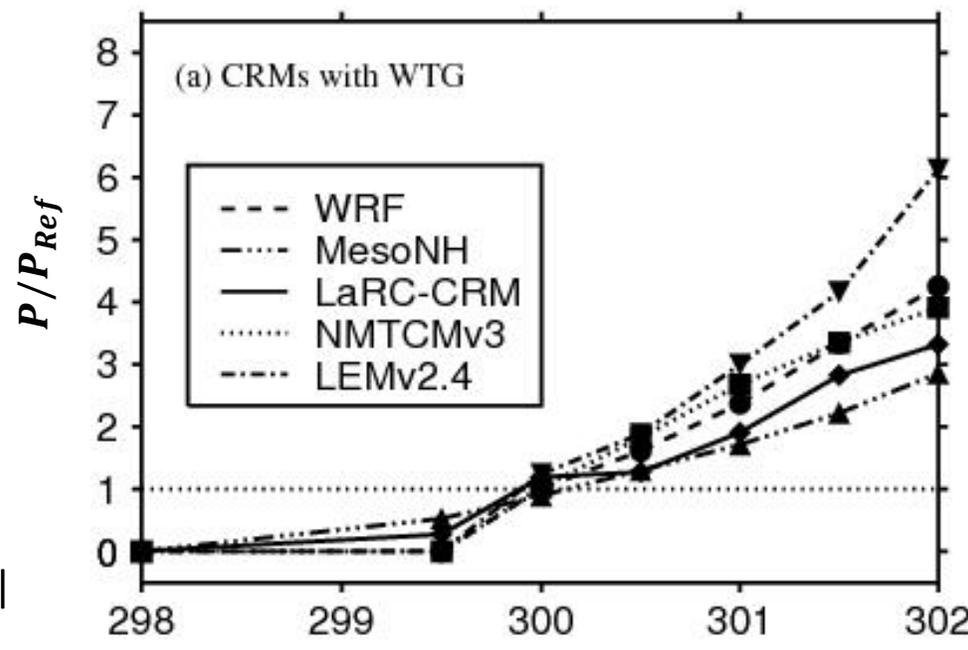
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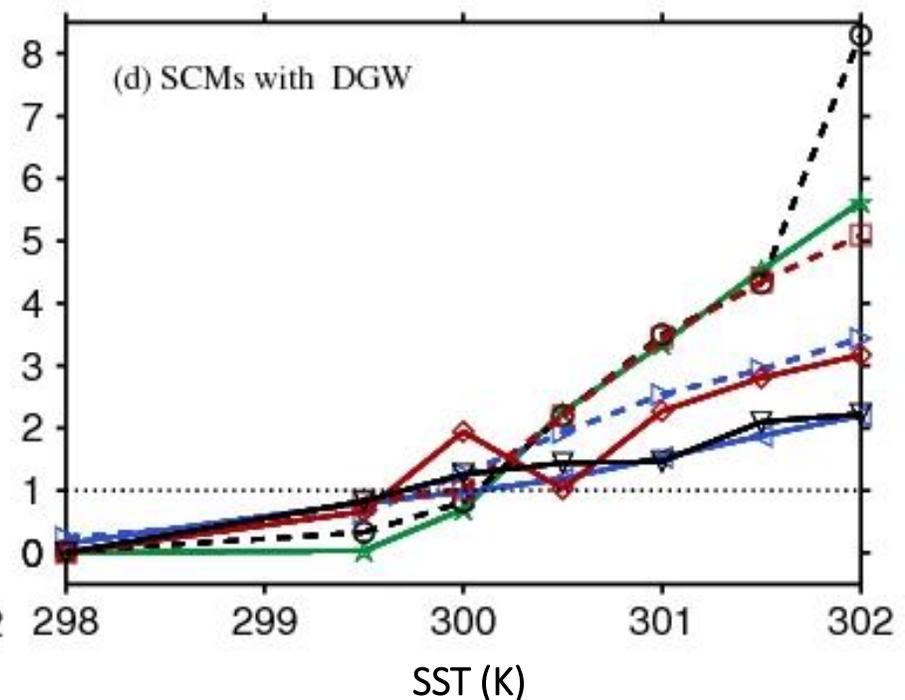
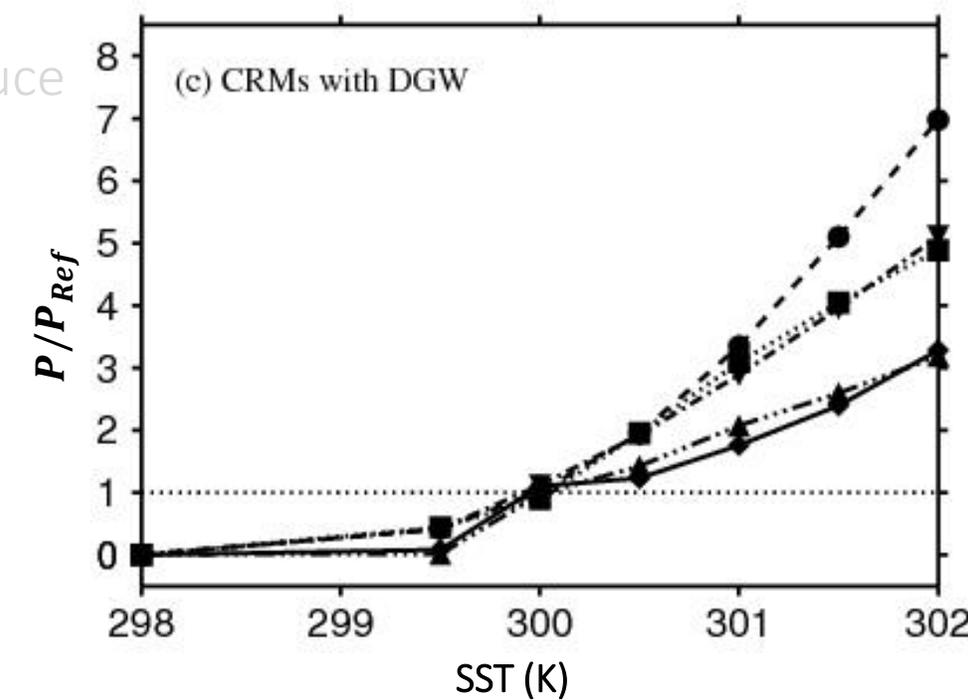
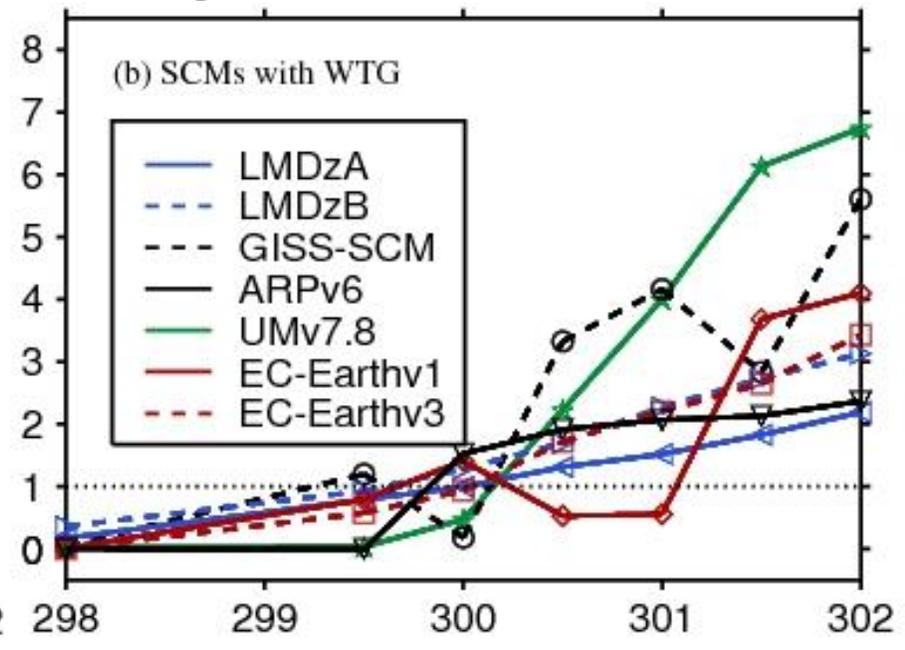
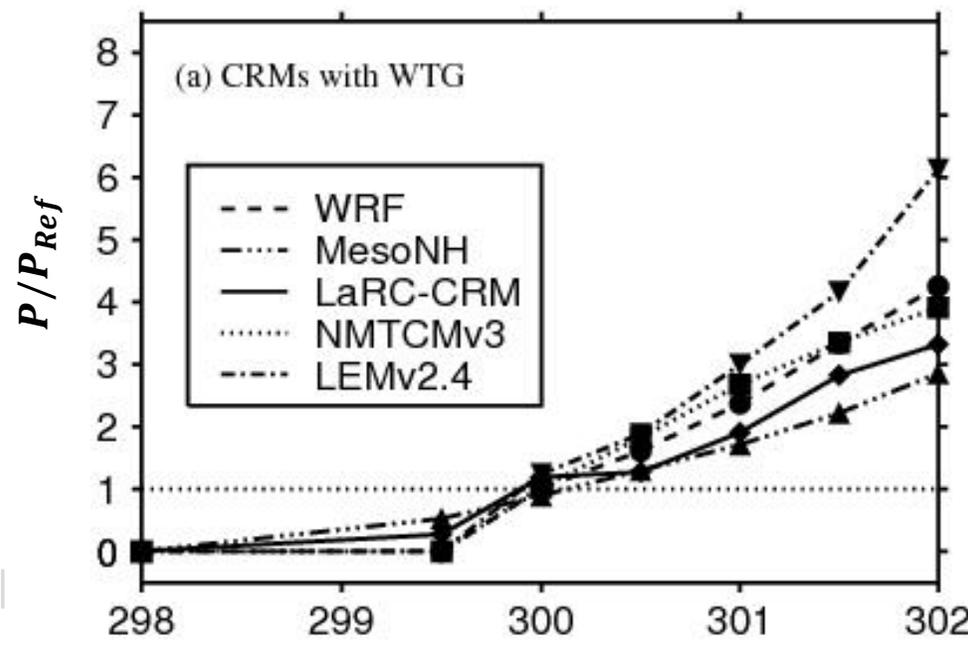
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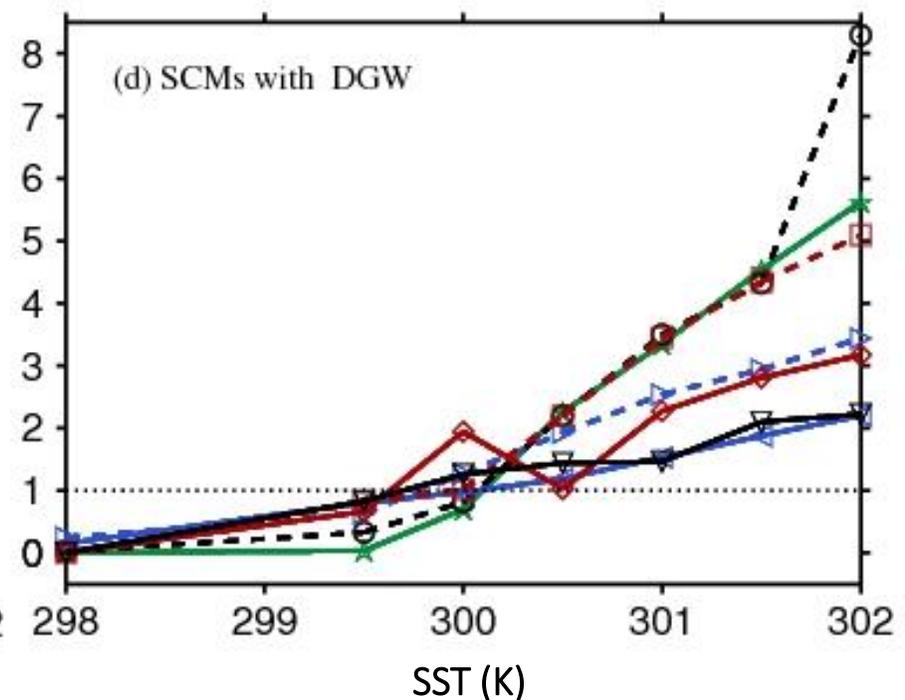
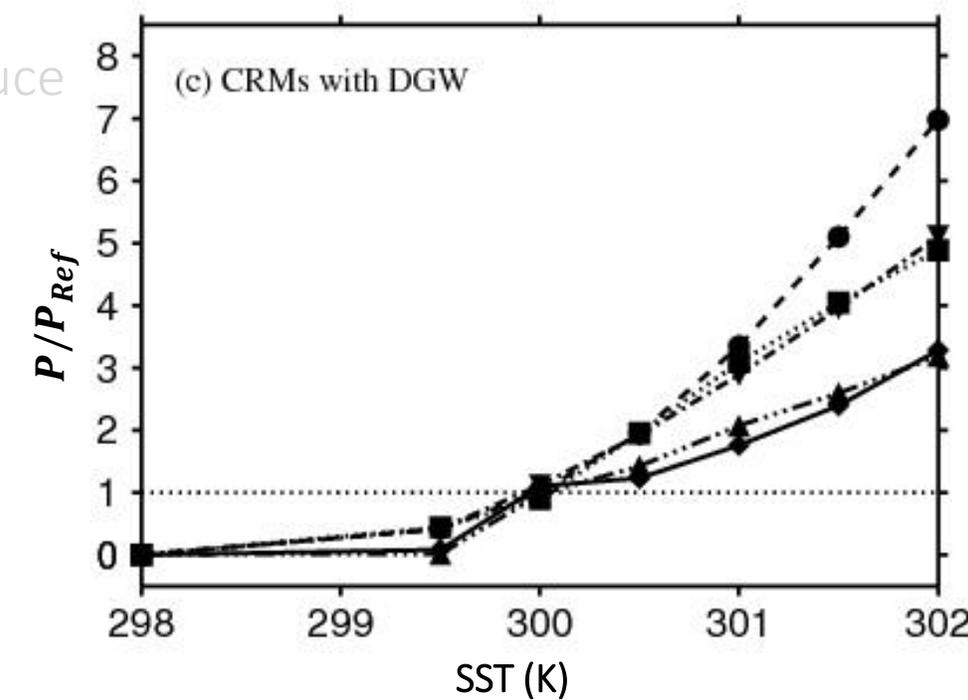
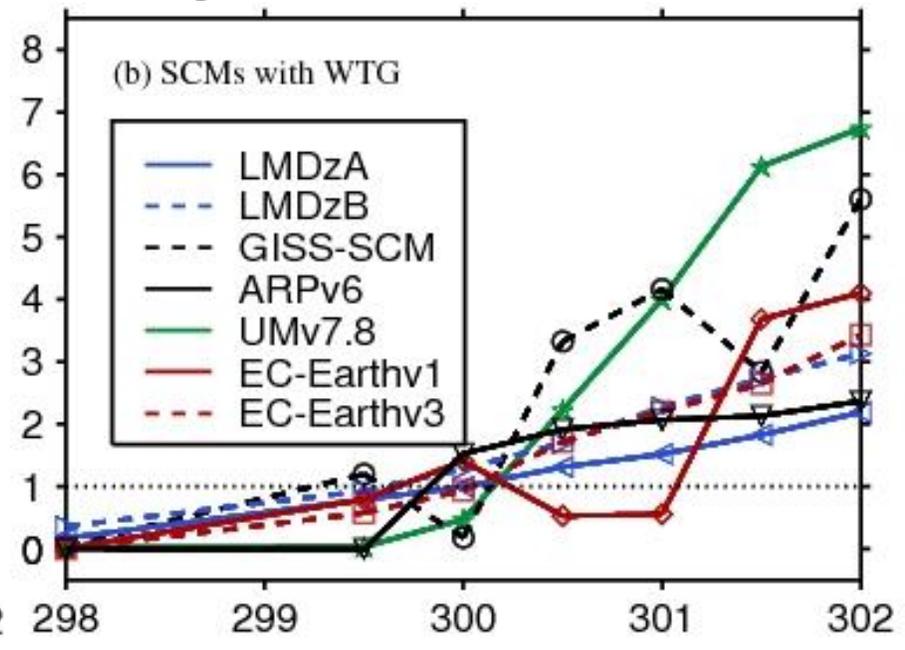
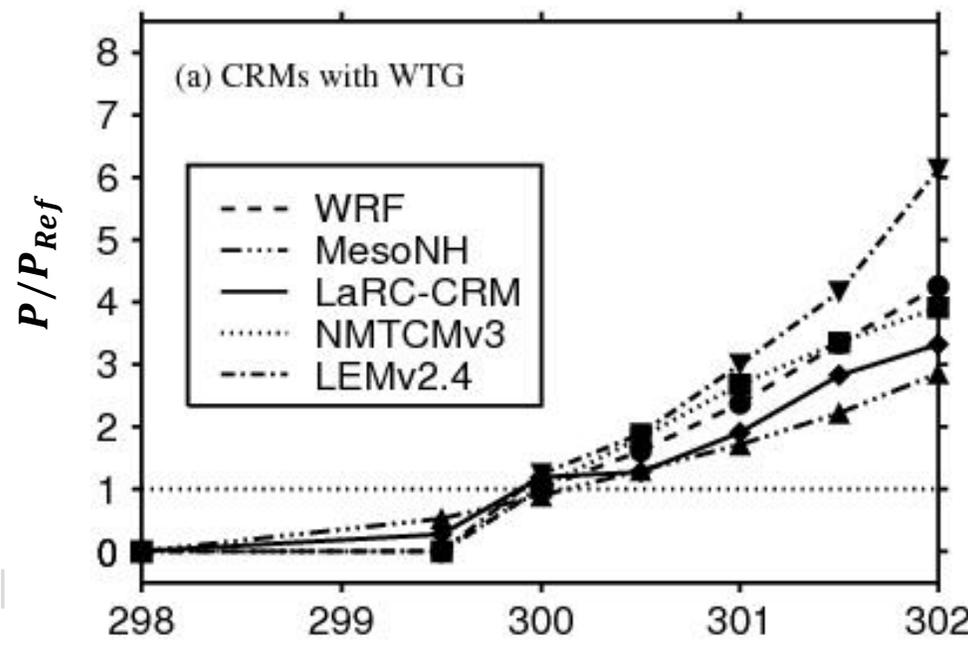
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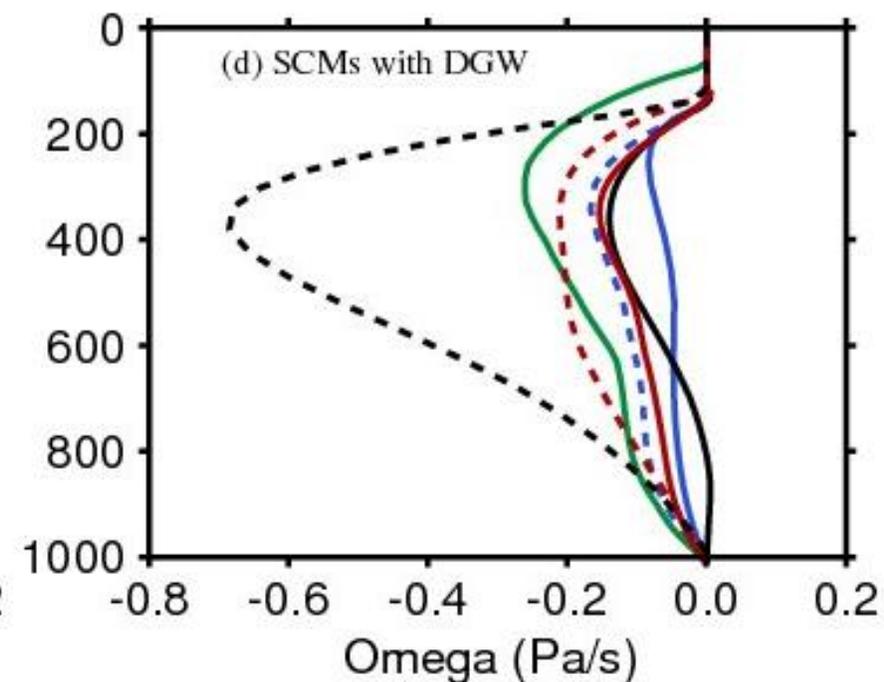
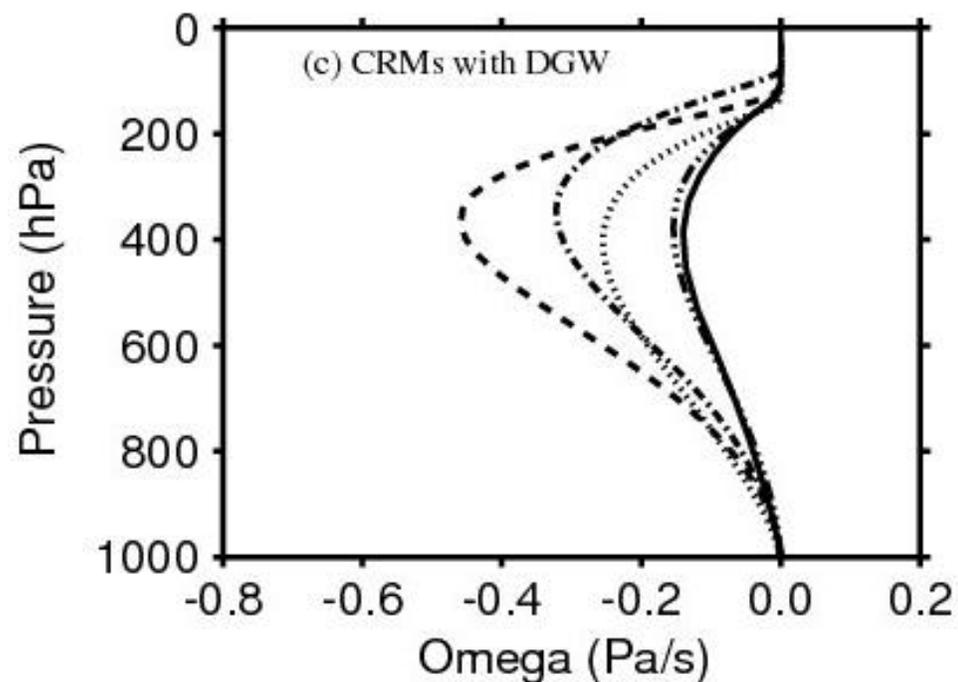
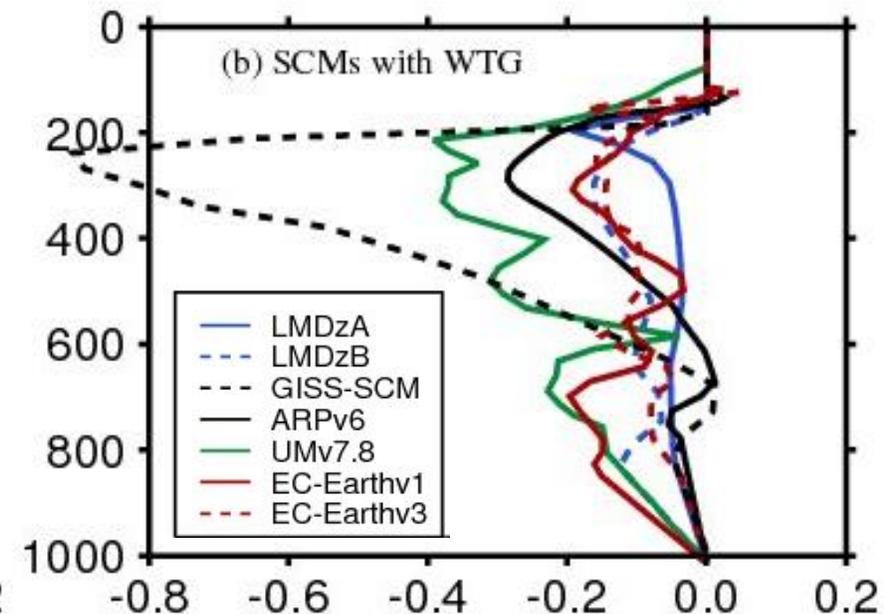
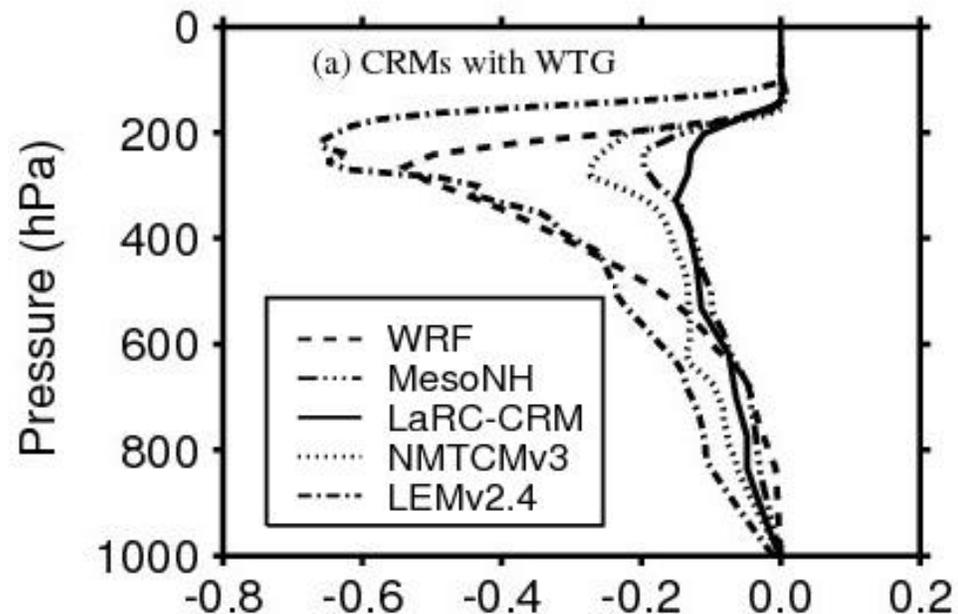
4-SCMs shows sensitivity of P to the SST which is not **not always monotonic** (e.g.,, GISS-SCM).



# WTG and DGW simulation over non-uniform SST

Ref state= RCE at 300K.

SST = 302 K

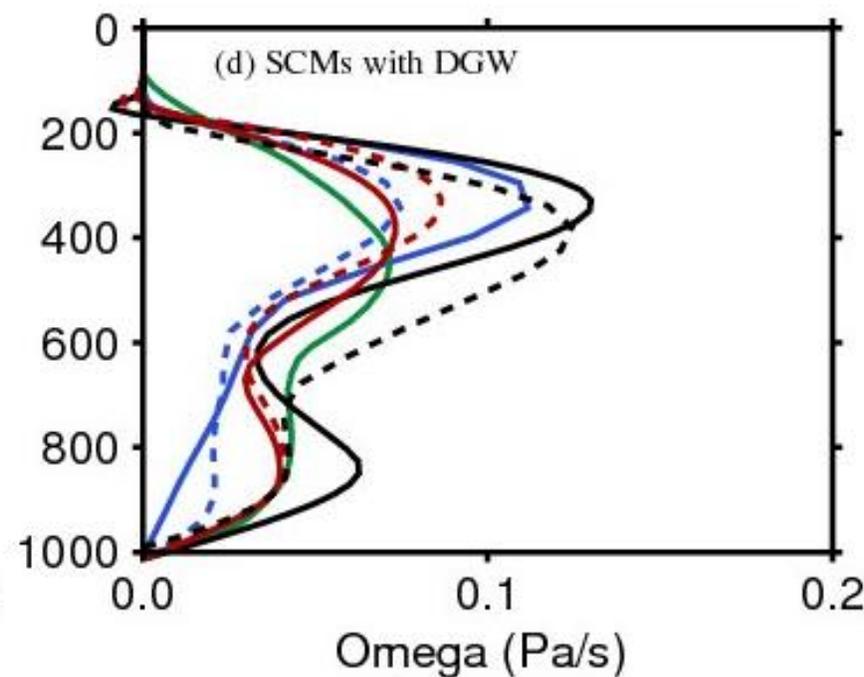
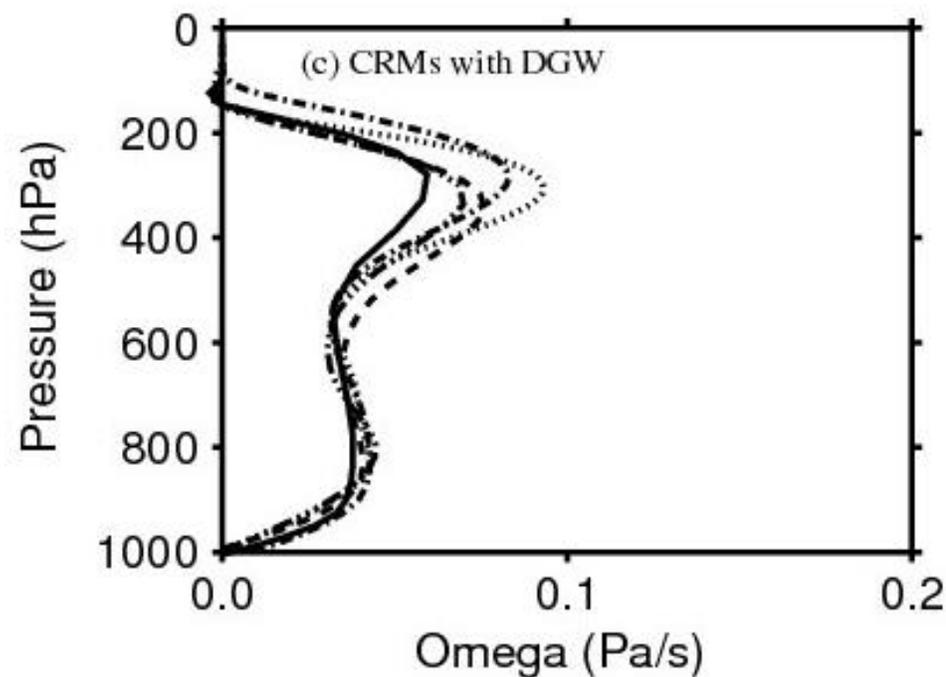
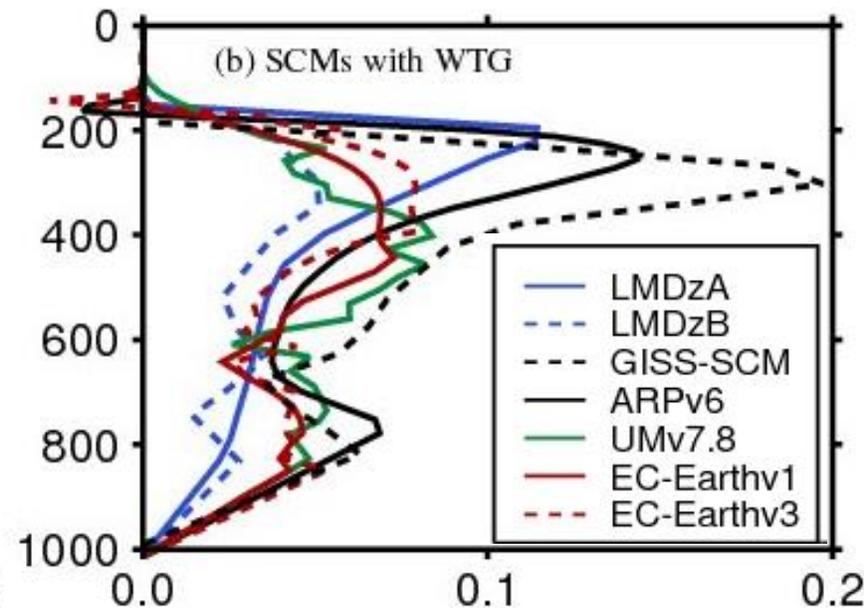
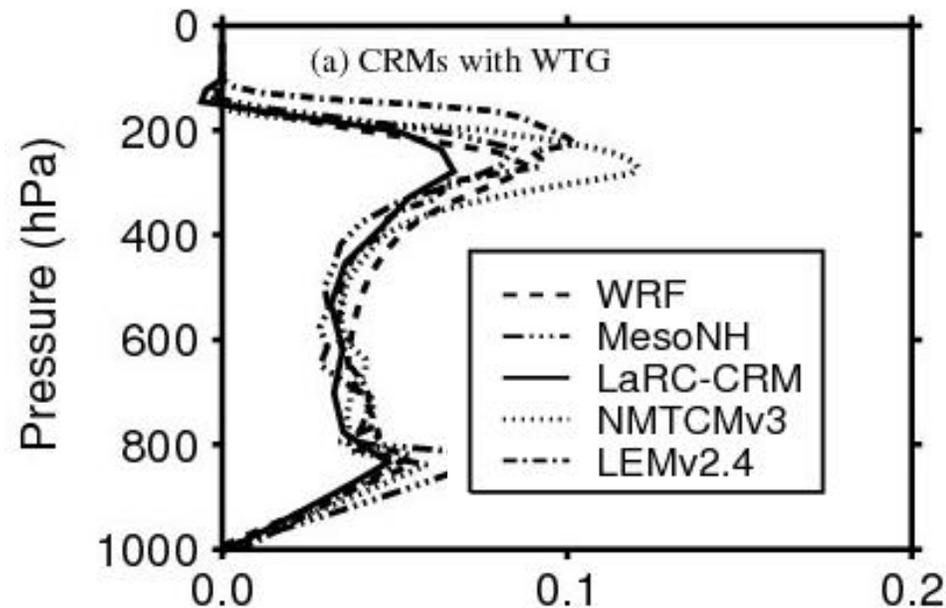


Profiles produced by  
DWG are **smoother** and  
**less top-heavy** compared  
to those produced by WTG

# WTG and DGW simulation over non-uniform SST

Ref state= RCE at 300K.

SST = 298 K



- CRMs produce very similar profiles
- SCMs under both WTG and DGW methods result in **a much wider range of behaviours**

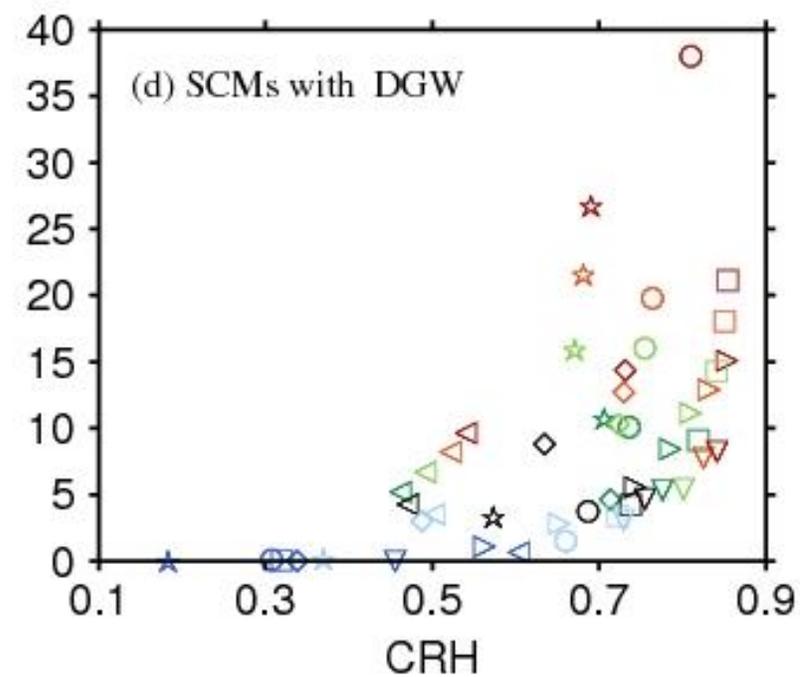
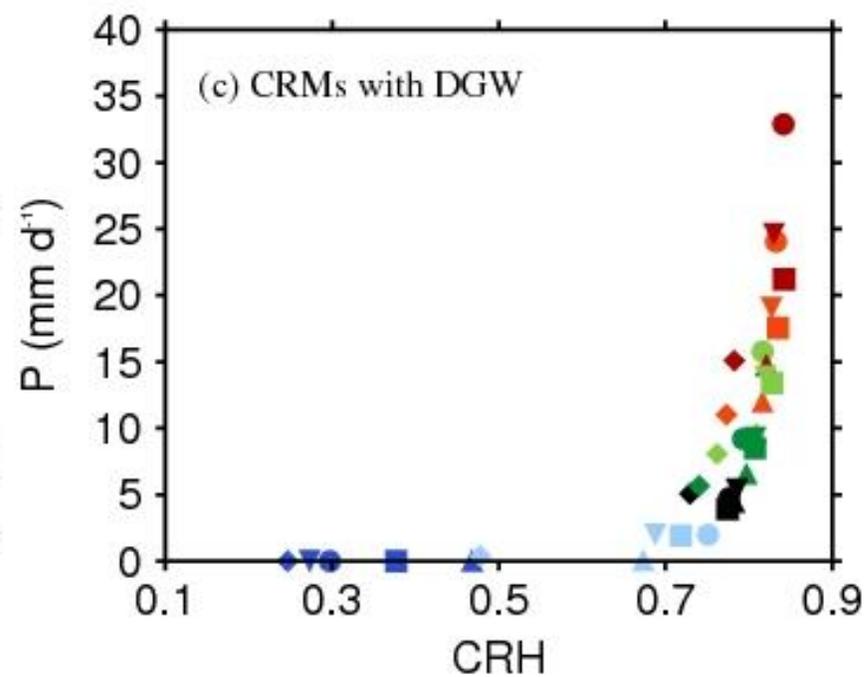
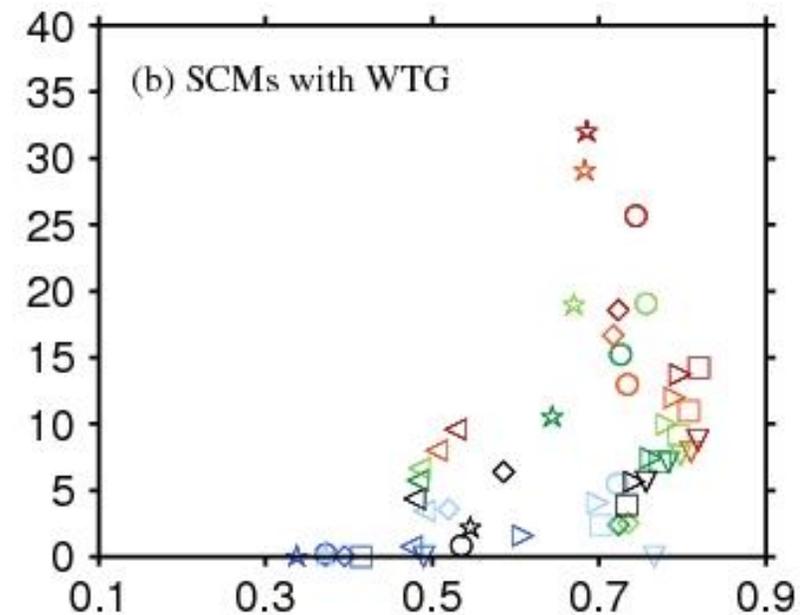
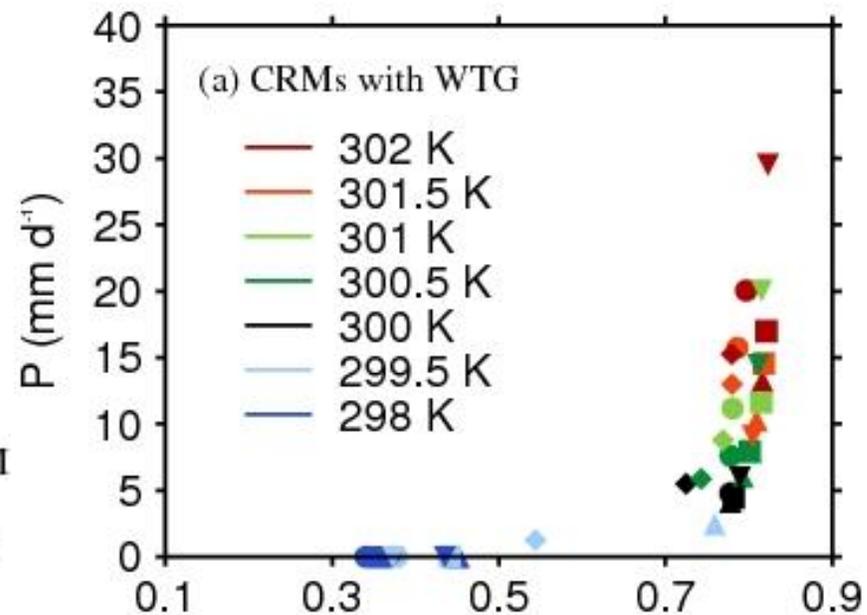
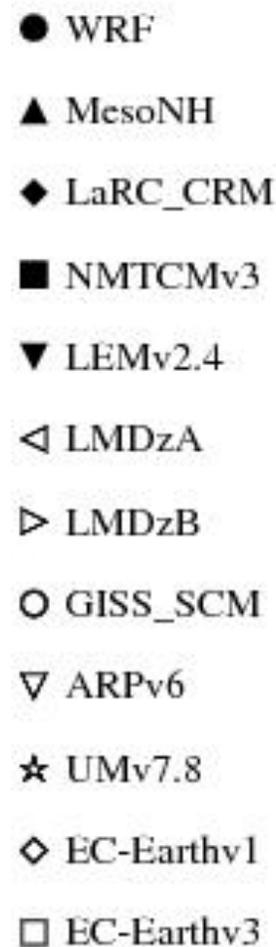
# WTG and DGW simulation over non-uniform SST

Ref state= RCE at 300K.

SST = 298, 299.5, 300, 300.5,  
301, 301.5 and 302 K

- CRMs under both WTG and DGW methods produce very similar relationship between P and CRH.

- SCMs results in a much wider range of behaviours



# Summaries

- Over uniform SST, **large-scale circ develops** under the WTG/DGW in some models but not all. More likely under the WTG than under the DGW.
- Some models sustain **multiple equilibria (ME)** under the WTG, while others do not.
- ME are more likely at higher SST, but **sensitive to PBL depth**
- No model sustain ME under the DGW.

## Overall

- The WTGs produce a wider range of behaviours than DGWs
- CRMs under the WTG/DGW method behave broadly in a similar way, while **SCMs exhibit a much wider range of behaviours.**

Comparison between CRMs and SCMs under the WTG/DGW may be a **useful tool for trying to reduce biases or improve the SCMs or a useful tool when developing and testing parameterization schemes.**

# Questions?

# Radiative-Convective Equilibrium (RCE) simulations

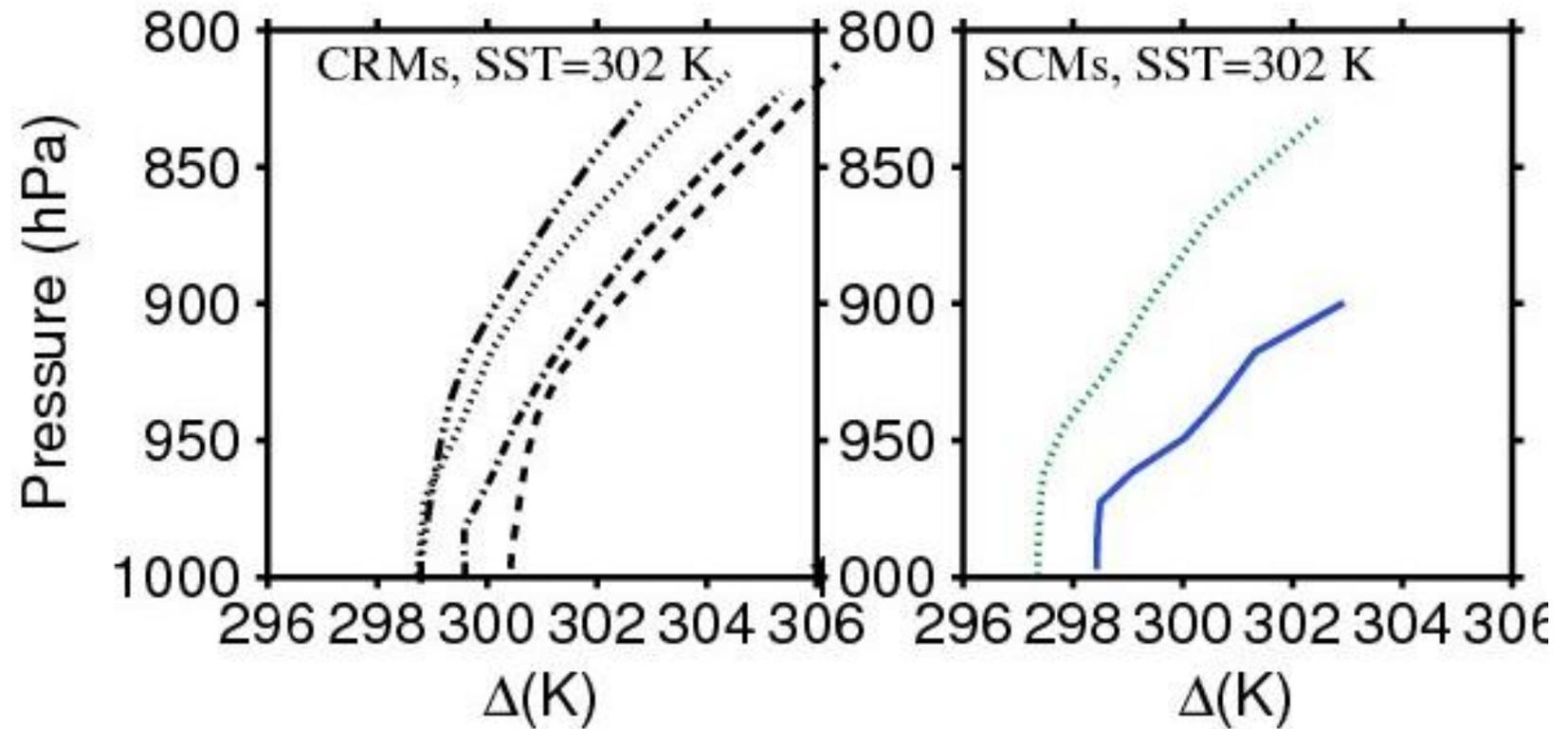
Fixed sea surface temperature (SST) and no Coriolis force is applied

Idealized radiative forcing profile:

$$\frac{\partial T}{\partial t} = \begin{cases} -1.5 & \text{if } \bar{p} \geq 100 \\ -1.5 \times \frac{\bar{p} - 100}{100} - \alpha_T \times \frac{200 - \bar{p}}{100} \times (\bar{T} - 200) & \text{if } 100 < \bar{p} < 200 \\ \alpha_T \times (\bar{T} - 200) & \text{if } \bar{p} \leq 100 \end{cases}$$

$\bar{p}(\text{hPa})$

RCE simulations with SST =298, 300 and 302 K

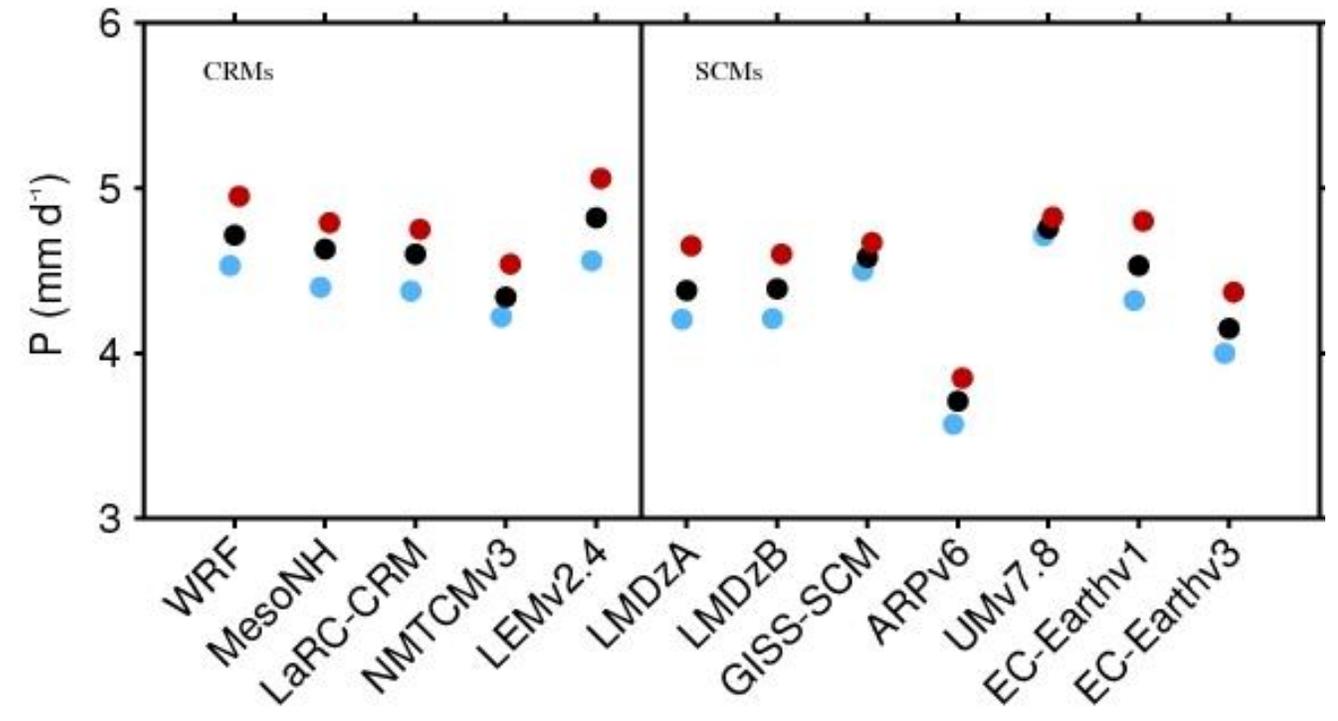


*Potential; temperature in the lowest 200 hPa.*

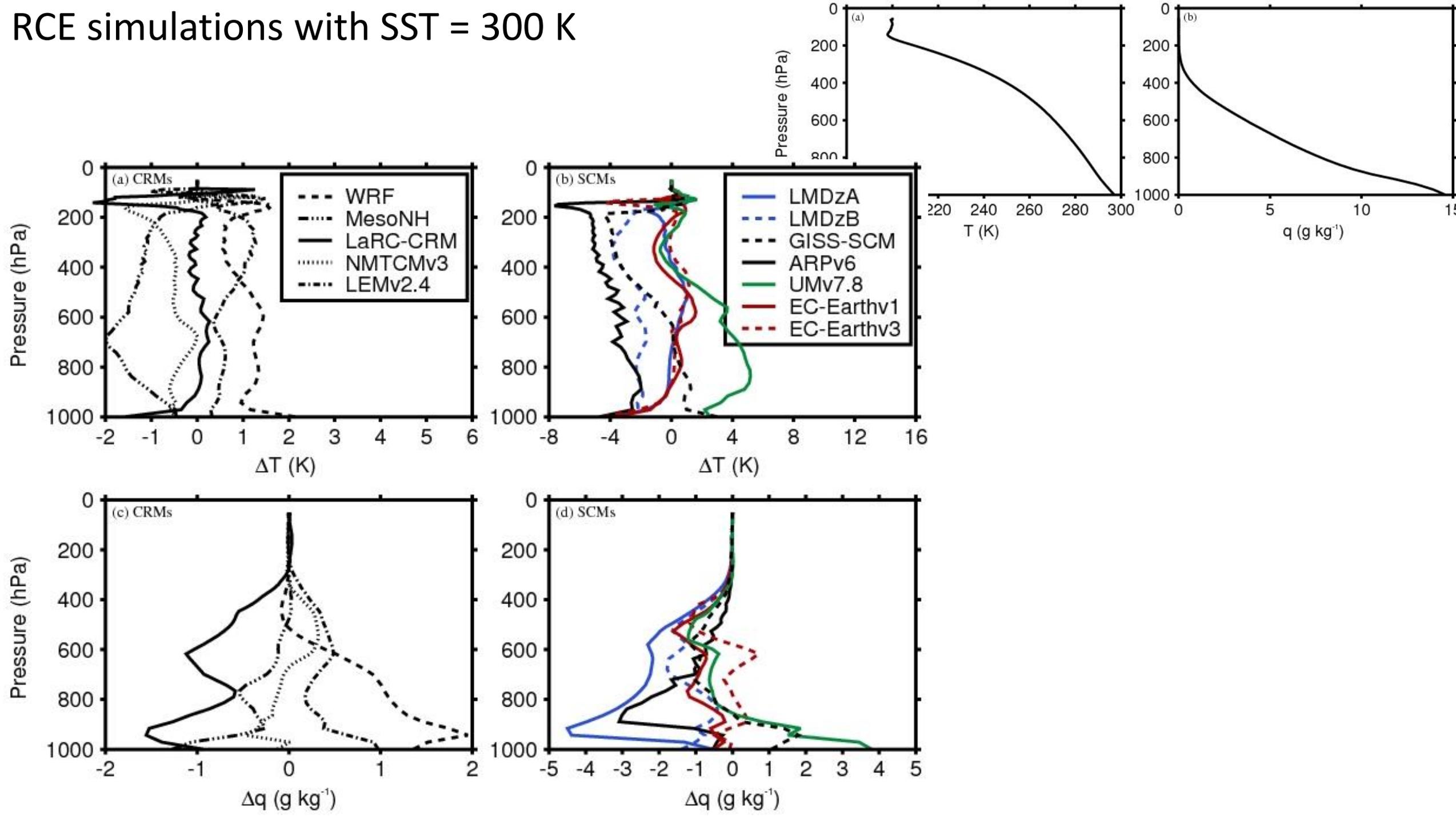
*RCE simulations with SST=302K*

RCE simulations with SST = 298, 300 and 302 K

Colour code: **298**, **300**, **302 K**



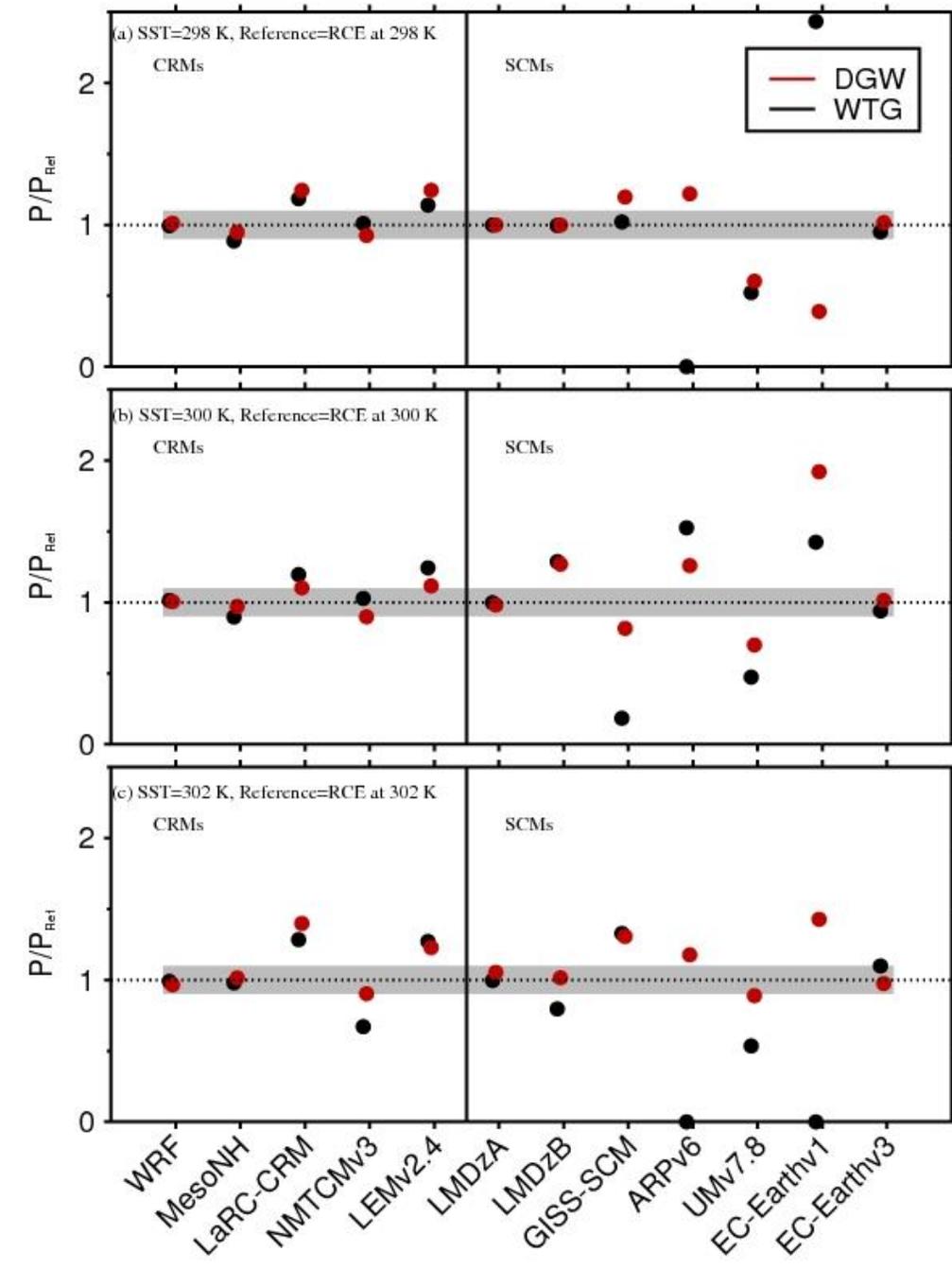
# RCE simulations with SST = 300 K



# WTG and DGW simulation over uniform SST

- The reference state of each model comes from the radiative-convective equilibrium (RCE) simulations of the same model.
- The WTG and DGW simulations are performed over uniform SST of 298, 300 and 302 K with the reference state from the same SST.
- The WTG and DGW simulations are initialized with profiles from the reference state.

Wider range of behaviours across SCMs compared to CRMs



# WTG and DGW simulation over uniform SST

- Wider range of behaviour across SCMs compared to CRMs
- The profiles produced by DGW simulations are smoother compared to those produced by WTG simulations

We defined  $\Omega = \frac{1}{\Delta p} \int \bar{\omega} dp$

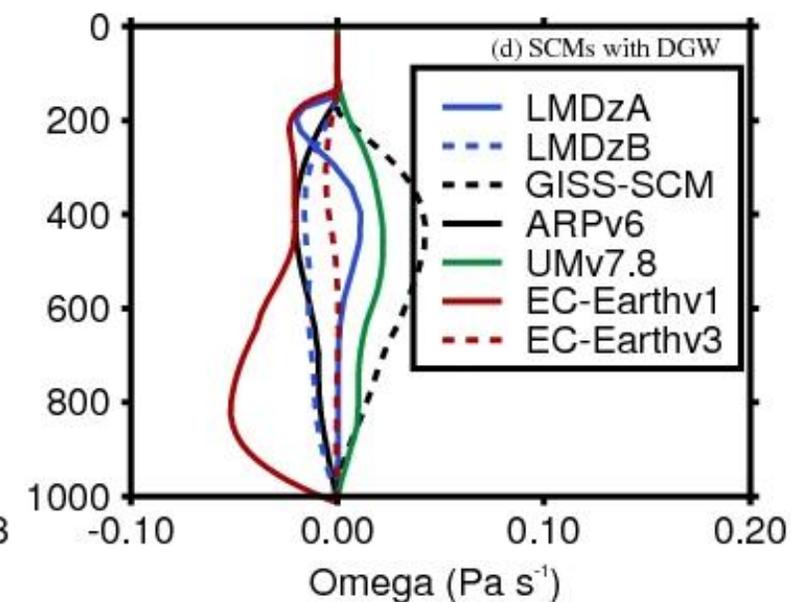
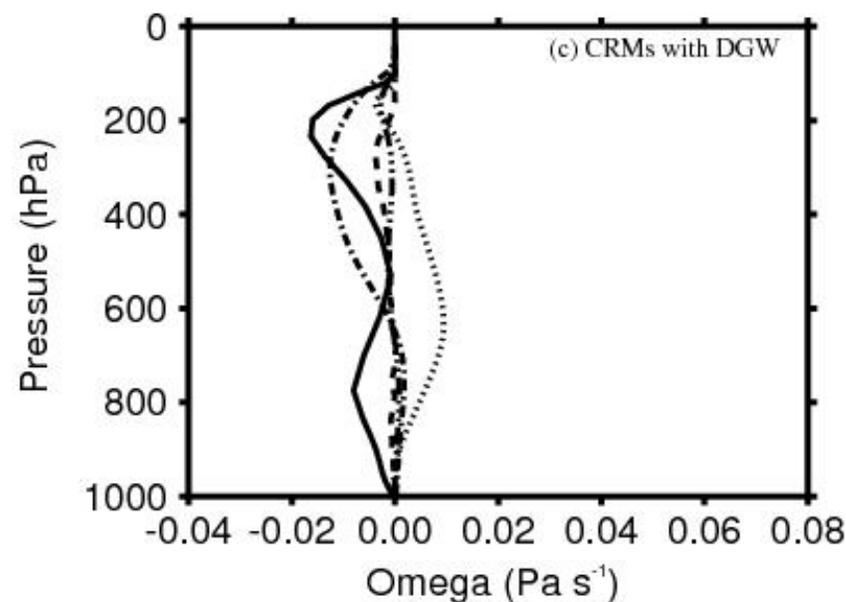
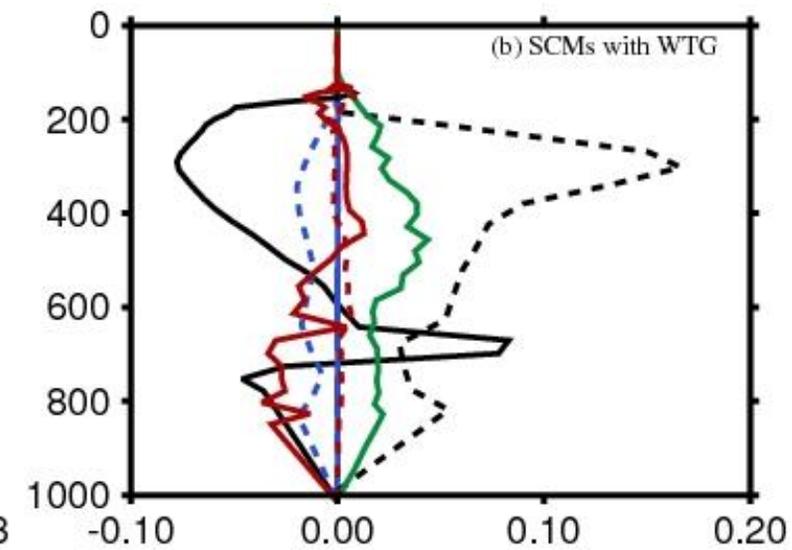
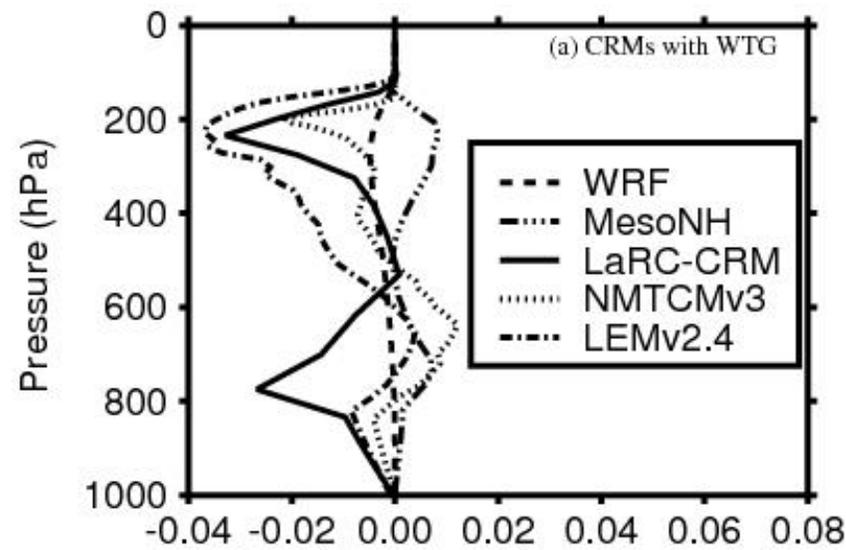
A simulation replicate the RCE State to a good approximation

If

$0.9 < \text{MRR}/\text{MRR}_{\text{RCE}} < 1.1$

and

$-4 \times 10^{-3} < \Omega < 4 \times 10^{-3}$



# Sensitivity to initial moisture conditions

- Initialized with RH from the RCE state (full circles)
- Initialized with 0% RH (open circles)

Some simulations are insensitive to the initial RH.

No dry equilibrium under the DGW method

Over a uniform SST of 302 K, we compared the profiles at equilibrium in the WTG simulations of WRF, NMTCMv3, LEMv2.4, UMv7.4, LMDzB to those obtained in the WTG simulation of MesoNH

