

ECMWF/NCEO data assimilation training course

(Partial) list of references. Compiled by J. Amezcua.

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